





(α,γ) & (α,n) key reaction studies using (⁷Li,t) alpha-transfer reactions

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Why studying (α, γ) & (α, n) reactions via α -transfer reactions?





T=0.1-1 GK \rightarrow hundreds keV- MeV << E_C $\rightarrow \sigma(E)$ very weak (0.01 fb- ~100 pb) \rightarrow Direct measurements are very challenging or impossible

In case of stable nuclei:
 Direct measurements of \(\sigma(E)\) at high energies then extrapolation at stellar energies **But:** Problems with extrapolation: resonances at very low energy, sub-threshold resonances

➢ In case of radioactive nuclei:
 Low beam intensities (~10⁵ - 10⁷ p/s)
 → direct measurements challenging

Resonant (α, γ) & (α, n) reaction cross-sections

 $A+\alpha \rightarrow C^* \rightarrow B+\gamma$ or $A+\alpha \rightarrow C^* \rightarrow B+n$



Resonant capture only possible for energies: $E_{cm}=E_R=E_x-Q$

$$\sigma(E) = \pi \lambda^2 \frac{2J_c + 1}{(2J_A + 1)(2J_x + 1)} \frac{\Gamma_x \Gamma_y}{(E - E_R)^2 + \frac{\Gamma_{tot}}{4}} \quad x = \alpha,$$

y=n or γ

$$\langle \sigma v \rangle = \left(\frac{2\pi}{\mu kT}\right)^{\frac{3}{2}} \hbar(\omega \gamma)_R \exp\left(-\frac{E_R}{kT}\right)$$

$$\rightarrow (\omega \gamma)_R = \frac{2J_c + 1}{(2J_A + 1) \cdot (2J_x + 1)} \frac{\Gamma_x \Gamma_y}{\Gamma_{tot}}$$

The resonant reaction rates can be calculated if the resonant parameters (E_R, J_i, Γ_{x,y}) are known
 w
 experiments can be performed to extract these

spectroscopic information

Transfer reactions to evaluate the decay partial widths

Let's assume a compound nucleus C in an excited state E_r which has a pure core-particle configuration $\Psi = |A \oplus \alpha \rangle$



→ For a state with a pure core-particle configuration, $\Gamma_{\alpha}{}^{s.p}$ can be calculated → In most of cases Ψ is a mixture of configurations and we have $\Gamma_{\alpha} = S_{\alpha} \Gamma_{\alpha}{}^{s.p}$ → S_{α} is a measure of the overlap between the initial and final state

 \rightarrow By determining the <u>spectroscopic factor</u> $S_{\alpha} = \langle C^* | A \otimes \alpha \rangle^2$ via transfer reactions, we can calculate Γ_{α} .

Transfer reactions: $X(=\alpha+b)+A \longrightarrow C^*(\alpha+A)+b \longleftrightarrow \alpha+A \longrightarrow C^* \swarrow C^+ \gamma$

• Populate the states of interest in the compound nucleus C* formed by α +A by transferring the particle α from a high-energy projectile X assumed to be composite (X= α +b) (typical E ~ few tens of MeV >> V_{coul}) to the target nucleus A

What do we measure by detecting b?

- By measuring the energy and angle of the emitted particle b
 - \Rightarrow Excitation Level energies of the populated states in C^{*}: $\mathbf{E}_{\mathbf{x}}$ (kinematics calculations)
- Differential cross-sections of each populated state: $d\sigma/d\Omega$

$$\left(\frac{d \sigma}{d \Omega}\right)_{lab}^{exp} = \frac{Yield (\theta_{lab})}{N_p N_T \Delta \Omega}$$

- Yield = Number of **b** particles measured at each θ
- N_p= number of projectile ions
- N_T = number of target atoms/cm², $\Delta\Omega$ = Solid angle



Transfer reactions: $X(=\alpha+b)+A \longrightarrow C^*(\alpha+A)+b \longleftrightarrow \alpha+A \longrightarrow C^* \swarrow^{C+\gamma}$

- From the shape of the angular distribution & comparison to a theoretical calculation

 → Angular momentum of the transferred particle
 ⇒ Orbital angular momentum *l* of the single particle bound state
 - From the normalisation of the calculations to the data
 → Alpha spectroscopic factor

$$\frac{d\sigma}{d\Omega}\Big|_{\exp} = C^{2}S'_{\alpha}S_{\alpha}\frac{d\sigma}{d\Omega}\Big|_{Th}$$

 $S'_{\alpha} = \langle {}^{7}Li | t \otimes \alpha \rangle = 1$ Kubo et al PRC 1978)

$$S_{\alpha} = \langle C | A \otimes \alpha \rangle$$



Theoretical description of transfer reaction

$X(=\alpha+b)+A \longrightarrow C^{*}(\alpha+A)+b$

The Model used to describe transfer reactions in general is: **DWBA** (Distorted Wave Born Approximation) & beyond

DWBA main assumptions:

- Nucleon or cluster transfer occurs directly between the two active channels X+A and C+b: the transferred nucleon or cluster is directly deposited on the final state (no rearrangement in the final nucleus)
- The entrance and exit channels processes are dominated by the elastic scattering \rightarrow Distorted waves
- The transfer process is weak enough to be treated as a first order perturbation \rightarrow Born Approximation

DWBA cross section for a transfer reaction can be written as :

$$\sigma_{tra} \propto \left\| \left\langle \chi_{f} I_{\alpha A}^{C} \middle| \hat{V} \middle| I_{b \alpha}^{X} \chi_{i} \right\rangle \right\|^{2}$$

 $\chi_{i,f}$ The distorted wave functions of the initial and final state

$\hat{\lambda}$ Transition operator

 $\varphi_{\alpha A}$

 $I_{\alpha A}^{C}(r_{\alpha A}) \& I_{b\alpha}^{X}(r_{b\alpha})$ the overlaping functions of the bound states C/X formed by α and A/b

The radial part $I_{\alpha A}^{C}$ is approximated : $I_{\alpha A}^{C}(r_{\alpha A}) = S_{\alpha A}^{1/2} \varphi_{\alpha A}(r_{\alpha A})$ S is the spectroscopic factor

Is the radial part of the bound state wave function describing the relative motion α +A in C

From a spectroscopic factors to a-decay reduced widths γ_{α}^{2} **or ANCs** \tilde{C}^{2}

DWBA calculations

• Codes: FRESCO, DWUCK, Thomson, Compt. Phys. Rep. 7, 167 (1988), P.D. Kunz spot.Colorado.edu/~kunz/DWBA.html)

• DWBA ingredients:

- > Appropriate choice of **optical potential** parameters to describe the **entrance** & **exit** channels
- → Elastic scattering measurements $\rightarrow X(A,A)X$, C(b,b)C or global optical model parametrizations for a given range of mass & energy (Perey & Perey Atom. nucl. Data Tabl. 17 (1976), Daehnick et al. PRC 21,6 (1980),...)
- Binding potential parameters describing the interaction of the transferred particle with the core in the final & initial nucleus
 - \rightarrow The depth V is adjusted to reproduce the binding energy of the bound state

 \rightarrow Geometry of potential ($\mathbf{r}_i, \mathbf{a}_i$) \rightarrow uncertainty on spectroscopic factor

Wood-Saxon
$$\longrightarrow V(r) = -\frac{V_0}{1 + \exp(\frac{r - r_i}{a_i})}$$
 $V_0: \text{ depth of the potential (MeV)}$
 $r_i: \text{ radius}$
 $a_i: \text{ diffusivity}$ $v_{0} = -50 \text{ MeV}$
 $r_{i} = 3.3 \text{ fm}$
 $a_i = 0.65 \text{ fm}$

Which alpha transfer reactions?

> (⁷Li,t), (⁶Li,d) alpha transfer reactions: \rightarrow to evaluate (α ,n) & (α , γ) reactions by extracting $S_{\alpha} \rightarrow \Gamma_{\alpha}$

<u>Note:</u> - $(^{7}\text{Li},t) \rightarrow \text{less}$ affected by multi-step effects F.H and N. de Séréville, fphy.2020.602920 & references therein

- \rightarrow cross-sections to low spin states enhanced because of the non-zero α -angular momentum in ⁷Li: J^{π}(⁷Li)=1/2⁺ J^{π}(t)=3/2⁺ \Rightarrow L_{α}=1 \rightarrow less momentum mismatch
- \rightarrow angular distributions \rightarrow stronger direct features: more forward pronounced maxima

 \rightarrow populate more selectively states with α structure

- e.g : ${}^{13}C({}^{7}Li,t){}^{17}O$ for ${}^{13}C(\alpha,n){}^{16}O$ Pellegriti et al. PRC (R) 2008 ${}^{12}C({}^{7}Li,t){}^{16}O$ for ${}^{12}C(\alpha,\gamma){}^{16}O$ Oulebsir et al. PRC 2012 ${}^{7}Li({}^{22}Ne,t){}^{26}Mg$ (ANC) for ${}^{22}Ne(\alpha,n){}^{25}Mg$ Jayatissa et al. PRC 2020
- → Cluster transfer \Rightarrow Describe the interaction potential of $<\alpha+t$ |⁷Li> overlaps for (⁷Li,t) transfer \rightarrow Finite range DWBA (FR-DWBA)



(E) 1 0.9

0.8

0.6 0.5

0.4 0.3 0.2 0.1

s-process in rotating metal-poor massive stars

²²Ne(α ,n)²⁵Mg

- s-process nucleosynthesis \rightarrow half of the abundance of heavy elements in Universe
- 60 < A < 90 (weak s-process component) \rightarrow massive stars M>8M_{\odot}

Core He burning $(T \sim 3.10^8 \text{ K}, \text{ N}_{\text{n}} = 10^6 \text{ cm}^{-3})$ & shell Carbon burning $(T \sim 10^9 \text{ K}, \text{ N}_n = 10^{11} \text{ cm}^{-3})$

- Metal-poor massive stars \rightarrow negligible *s*-process production (low ²²Ne & Fe seed abundance)

.



With fast rotation induced mixing \longrightarrow ²²Ne production in He core strongly enhanced Nishimura+16, Choplin+18

large production of *s*-elements between Strontium & Barium 90 < A < 140

- Enhanced weak s-process (es-process) Frischknecht+16
- \rightarrow Important impact on chemical enrichment in early galaxies.

 \rightarrow Source of heavy elements such as Barium in early universe? Barbuy+14 \rightarrow Origin of the observed enhanced s-elements in globular cluster NGC6522 **Barbuy+09** & in CEMP stars **Beers+05** ?



s-process in rotating metal-poor massive stars

But the final abundances of the enhanced weak *s*-process strongly depends on: ${}^{16}O(n,\gamma){}^{17}O$ neutron poison effect & ${}^{17}O(\alpha,n)/{}^{17}O(\alpha,\gamma)$ reaction rate ratio

 \rightarrow neutron recycling efficiency



Calculation with ¹⁷O(α ,n)²⁰Ne Nacre adopted rate & ¹⁷O(α , γ)²²Ne CF88 rate

Present status on ¹⁷O(α ,n)²⁰Ne and ¹⁷O(α , γ)²¹Ne

- Core He burning: T ~0.2-0.3 GK \rightarrow E_{c.m}~ 0.297-0.646 MeV \rightarrow E_x=7.64-8.00 in ²¹Ne
- Shell Carbon burning: T~1 GK \rightarrow E_{c.m}~ 0.783-1.5 MeV \rightarrow E_x=8.13-8.85 in ²¹Ne

$\frac{17O(\alpha,n)^{20}Ne \& 17O(\alpha,\gamma)^{21}Ne}{17O(\alpha,\gamma)^{21}Ne}$ direct measurements:

- Denker+1994, Best+2013 \rightarrow 0.63 \leq E_{cm} \leq 1.8MeV
- Best +2011, Taggart+2019
- Williams+2022

0.63≤E_{cm}≤1.33MeV

- No direct measurements @ $E_{cm} < 0.63$ MeV (Core He burning)
- Spectroscopy of ²¹Ne: E_x , S_α or Γ_α , J^π , $\Gamma_\gamma/\Gamma_{tot}$, Γ_n ... $\stackrel{\text{(a,n)}}{\Rightarrow}$ ¹⁷O(α ,n) and ¹⁷O(α , γ) rates (core He burning)
- → Unknown or poorly known $S_{\alpha}(\Gamma_{\alpha})$ & Γ_{n} , $\Gamma_{\gamma}/\Gamma_{tot}$ → Few have spin-parity assignments
- Neutron transfer reaction $\rightarrow S_n \rightarrow \Gamma_n$ Frost-Schenk+MNRAS2022 • α -transfer reaction $\rightarrow S_n \rightarrow \Gamma_n$ (present work/MLL-exp)



Study of ²¹Ne states via ¹⁷O(⁷Li,t)²¹Ne α-transfer reaction

Q3D spectrometer (MLL)

- Beam ⁷Li: E=28 MeV I=100 nAe
- Targets:

 W¹⁷O₃ (41 μg/cm²) enriched at 35% on ^{nat}C
 W^{nat}O₃ (39 μg/cm²) on ^{nat}C
- Solid angle: 6 to 12.4 msr
- Energy resolution $\Delta E/E \sim 2 \times 10^{-4}$

$d\sigma/d\Omega$ measurements:

- 9 angles $\theta_{lab} = 6^{\circ} 36^{\circ} \Rightarrow \theta_{cm} \rightarrow 7.5^{\circ} 45^{\circ}$
- on $W^{17}O_3$ & on $W^{nat}O_3$ for calibration & background evaluation
- At 3 different times at 6° to check the stability of the target



Position

Excitation energy spectrum of ²¹Ne



• Fit with multiple skewed gaussians with common width & exponential factor

Experimental energy resolution (FWHM) : ~ 30 keV (6°) - 71 keV (36°)

FR-DWBA calculations



 Good description of the data by DWBA → Direct transfer mechanism

• <u>Triplet 8.160/8.155/8.146</u>: Fit with 3 components $\rightarrow S_{\alpha}$ of 8.146 & 8.160 MeV derived from Γ_{α} Best+2013 $\Rightarrow S_{\alpha}(8.155 \text{ MeV})=0.15$ (present work)

• <u>Doublet 7.980/7.982 MeV</u>: Fit with 2 components $\rightarrow S_{\alpha}$ of 7.98 MeV deduced using $\omega\gamma(\alpha, n)$ Denker+94 $\Rightarrow S_{\alpha}(7.982 \text{ MeV})=0.005$ (present work)

• <u>7.820 MeV</u>

 \rightarrow Best χ^2 for L_{α}=0,1 & good for L_{α}=2

$$\rightarrow L_{\alpha} = 0 \rightarrow S_{\alpha} = 0.61$$
 (unlikely)

$$S_{\alpha} \rightarrow \Gamma_{\alpha} = 2P_l \frac{\hbar^2 R}{2\mu} S_{\alpha} |\phi(R)|^2$$

@ R=7.5 fm

• Γ_{α} uncertainty: 3- 40% (stat), 35% (optical pot)

¹⁷O(α ,n) & ¹⁷O(α , γ) reaction rates & (α ,n)/(α , γ) rate ratio

Rates calculations:

RateMC code Longland+2013

□ For Er < 721 keV & Er=807 keV: Γ_{α} (present work) Γ_{α} (7.82MeV) for L_{α} =1 (L_{α} =0 in Best+2013)

 Γ_{α} (7.74 MeV) for L_{α}=0 (as in Best+2013)

 $\rightarrow \Gamma_n$ Frost-Schenk+2022

□ For Er≥ 721 keV : → Γ_{α} & Γ_{n} (Best+2013 direct measurement)

 $\Box \Gamma_{\gamma}$ from:

→ systematics of $\langle \tau \rangle_{\text{meas}}$ (Rolfs+72) → $\omega\gamma(\alpha,\gamma)$ Williams+2022 combined with present Γ_{α} & Γ_{n} (Frost Schenk+22) → when no $\Gamma_{n} \rightarrow \Gamma_{\gamma}/\Gamma_{n}$ Best+2013

→ Better neutron efficiency recycling with a factor of about 20 with the present rates than Best+2013 rates



Resonances contribution to the rates



Impact on the s-process in rotating poor-metal massive stars

• One-zone nucleosynthesis calculation mimicking the core He-burning phase of a low metallicity rotating massive star (Z=0.001, M=25 M_{\odot})



 \rightarrow Large enhancement (>1.5 dex (>1.3 dex)) of elements 40 < Z < 60 with the present new rates in comparison to Best+13 rates

 \rightarrow Two order of magnitude (~1.5 dex (case2)) on Barium : largest effect

F. H, P. Adsley, L.Lamia+submitted to PRL

Case II:

¹⁵O(α,γ)¹⁹Ne & X-ray burst nucleosynthesis



¹⁵O(α, γ)¹⁹Ne:

Present Status & strategy



Experimental characteristics for α -transfer reactions with **RIB**

 $Y=N/t=N_{proj} \times N_{target} \times d\sigma/d\Omega \times \Delta\Omega$

 $(^{7}Li,t)$ with stable beam

- $I_{\text{beam}} \sim 100 \text{ pnA}, q = 3 \rightarrow N_{\text{proj}} \sim 2.10^{11} \text{ pps}$
- target thickness~ $100 \,\mu g/cm^2 \rightarrow N_{target} \sim 4.10^{18} \, at/cm^2$
- $\Delta \Omega \sim 5 \text{ msr}$ (e.g. Split-pole, Q3D magnetic spectrometers)

(⁷Li,t) with RIBs

- Beam intensity: Typical 10^5 pps $[^{15}O \sim 10^7 \text{ pps}] \rightarrow 6$ orders of mag. less wrt stable beams

 $\rightarrow N_{\text{proj}} \times N_{\text{target}} \times \Delta \Omega \sim 4 \text{ s}^{-1} \text{ mb}^{-1} \text{ sr}$

Light particle detection system (tritons)

 \rightarrow need of large coverage detection system : silicon array $\Delta \Omega \sim 2\pi$ sr

- \rightarrow 3 orders of mag. higher wrt stable beams \bigcirc
- Target thickness
 - \rightarrow Typical ~ mg/cm² (one order of mag. higher)

 \rightarrow Compromise between statistics and energy resolution \bigcirc

 $\rightarrow N_{\text{proj}} \times N_{\text{target}} \times \Delta \Omega \sim 0.04 \text{ s}^{-1} \text{ mb}^{-1} \text{ sr}$

Very challenging experiments... but feasible!

- \blacktriangleright Relatively long: ~10 days
- Relatively "low" statistics

¹⁵O(α,γ)¹⁹Ne case:

Experiment & results

 \Rightarrow Studied via ⁷Li(¹⁵O,t)¹⁹Ne*(γ)¹⁹Ne @ **SPIRAL1/GANIL**

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MUST2

DSSSD 300 μm + Csl

128+128 strips

128+128 strips

Triple coincidence: AGATA – HPGe for prompt-γ & MUGAST-DSSDE for light particle t & VAMOS-Spectrometer for ¹⁹Ne recoil



VAMOS @ $0^{\circ}2$ • $\Delta\Theta \pm 7^{\circ}$

ΔBρ ± 10° (~)

¹⁵O(α,γ)¹⁹Ne case:

Experiment & results

 \Rightarrow Studied via ⁷Li(¹⁵O,t)¹⁹Ne*(γ)¹⁹Ne @ **SPIRAL1/GANIL**

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Summary

Advantages of alpha-transfer reactions

- High cross sections
- Can be used to extract alpha partial widths (spectroscopic factors), angular momenta, resonance energy of key resonant reaction cross-sections

Limitations & warnings

- Sensitivity of the spectroscopic factors to potential parameters \rightarrow 30-40% uncertainty
- Be aware about other possible reaction mechanisms:
 - \rightarrow Multi-step transfer
 - \rightarrow Compound nucleus : Hauser-Feschbach calculations (statistical model) needed

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Collaboration

¹⁷O(⁷Li,t)²¹Ne experiment

FH, P. Adsley (Texas AM), L. Lamia (LNS-Catania), D. S. Harrouz (IJCLab-Orsay), N. de Séréville (IJCLab-Orsay), B. Bastin (GANIL), A. Choplin (ILB-Brussels), T. Faestermann (MLL), C. Fougères (GANIL), R. Hertenberger (MLL), R. Hirschi (Keele), M. La Cognata (LNS-Catania), A. Meyer (IJCLab-Orsay), S. Palmerini (Perugia), R. G. Pizzone (LNS-Catania), F.de Oliveira Santos (GANIL), S. Romano (LNS-Catania), A. Tumino (LNS-Catania) and H.-F. Wirth (MLL)

¹⁵O(7Li,t)¹⁹Ne experiment

J.Sanchez Rojo (York), C. Diget (York), N. de Séréville (IJCLab-Orsay) & AGATA-MUGAST-VAMOS collaboration

THANK YOU FOR YOUR ATTENTION