



# Constraining the Electron Capture Rates of Neutron-Rich Nuclei with $(d, ^2\text{He})$ in Inverse Kinematics

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## 19<sup>th</sup> Russbach School on Nuclear Astrophysics



# Constraining the Electron Capture Rates of Neutron-Rich Nuclei with $(d, {}^2\text{He})$ in Inverse Kinematics

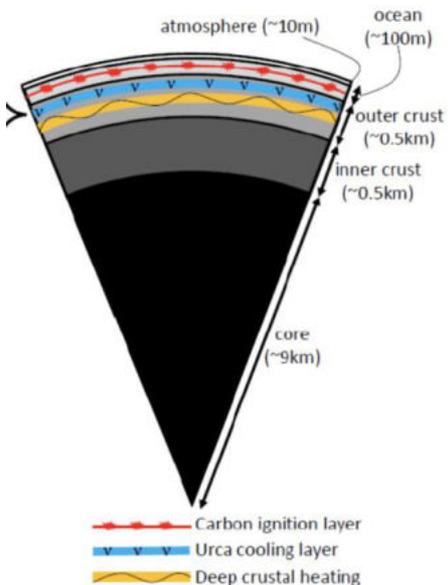
- The important role of electron captures in astrophysical simulations
- The extraction of Gamow-Teller strengths from charge-exchange experiments
- A new experimental tool for extracting Gamow-Teller strengths in the EC direction from unstable nuclei: the  $(d, {}^2\text{He})$  reaction inverse kinematics
- First application: the  ${}^{14}\text{O}$   $(d, {}^2\text{He})$  reaction in inverse kinematics
- Conclusions



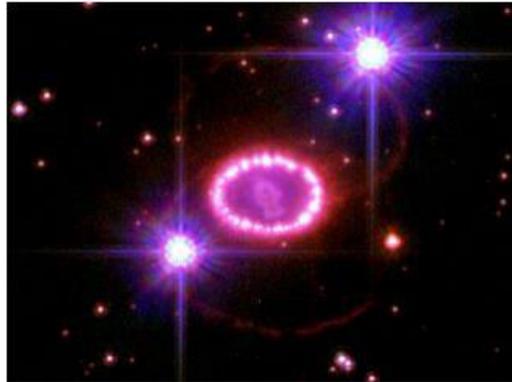
# Electron Capture Rates are Important Inputs for Astrophysical Simulation

Electron Capture (EC) Rates are important for:

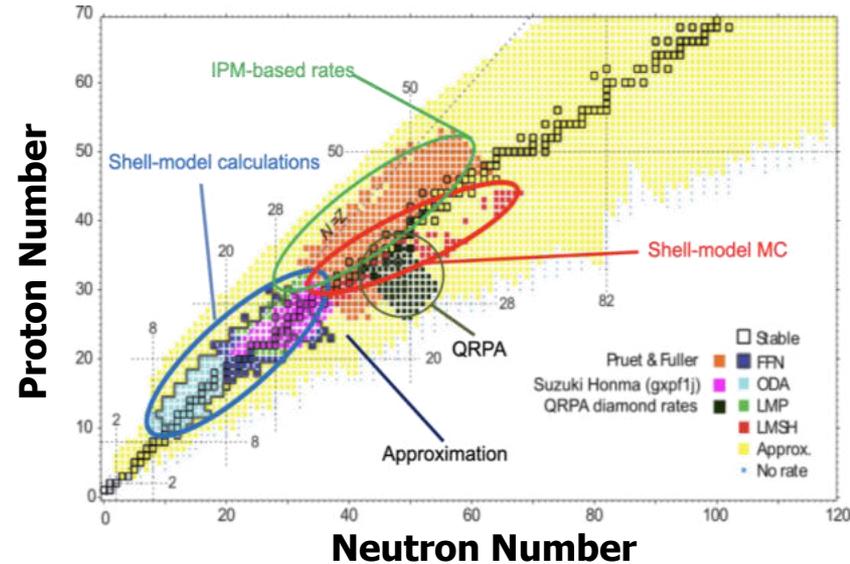
- Core-collapse and thermonuclear supernova
- Crust of accreting neutron stars in binary systems
- Final core evolution of intermediate mass stars
- ....



Courtesy Space Telescope Science Institute/NASA



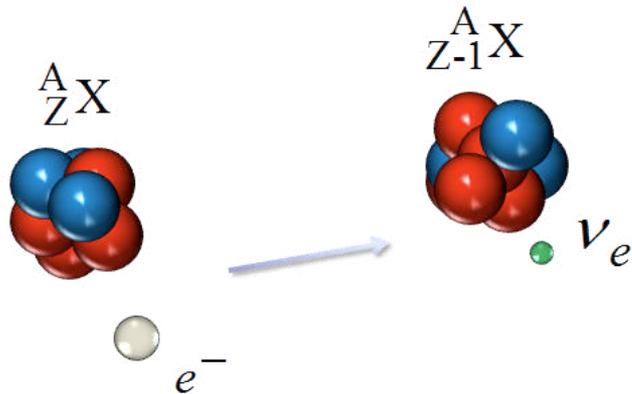
The remnant of supernova 1987a



Weak Rate Library: [https://groups.nsl.msu.edu/charge\\_exchange/weakrates.html](https://groups.nsl.msu.edu/charge_exchange/weakrates.html)  
 NuLiB: <http://www.nulib.org>

- Experimental data is needed to benchmark and guide the theoretical models.

# Gamow-Teller Transition Strength Necessary for Estimating EC Rates in Stellar Environments

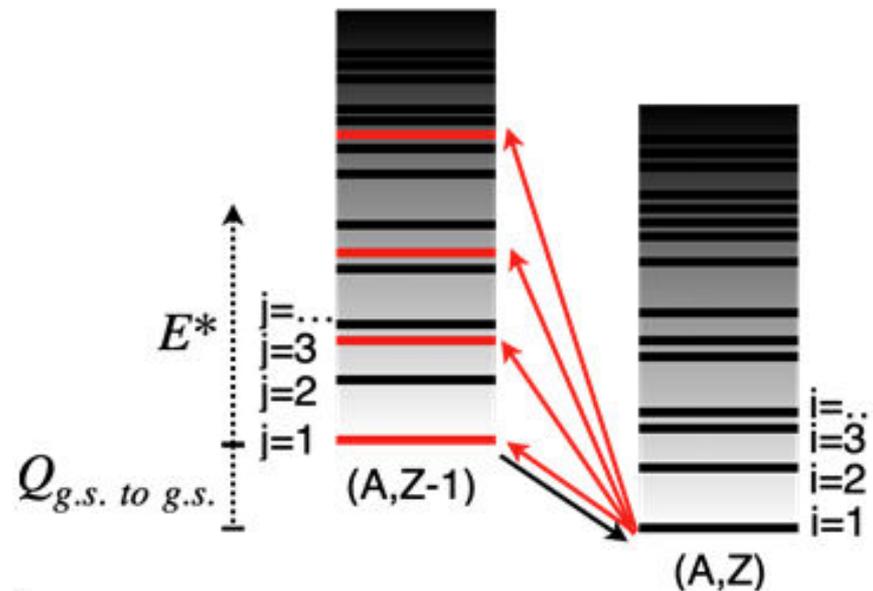


$$\lambda_{EC} = \ln 2 \sum_{ij} f_{ij}(T, \rho, U_F) B(GT)_{ij}$$

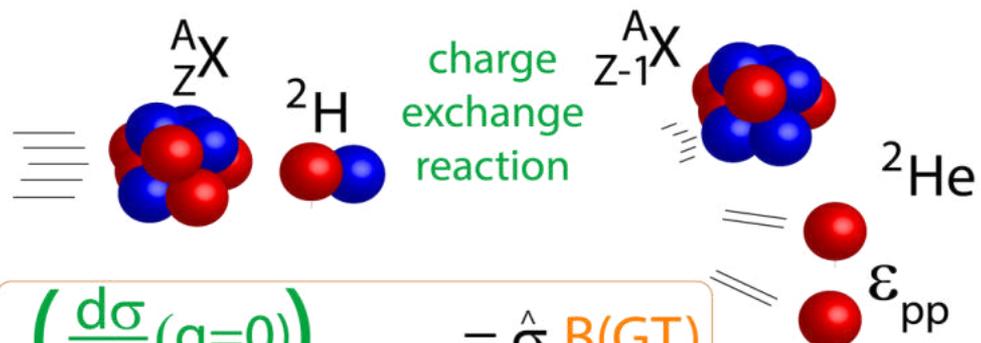
↓  
phase space factor

- EC from ground state
- $\beta^-$  from ground state

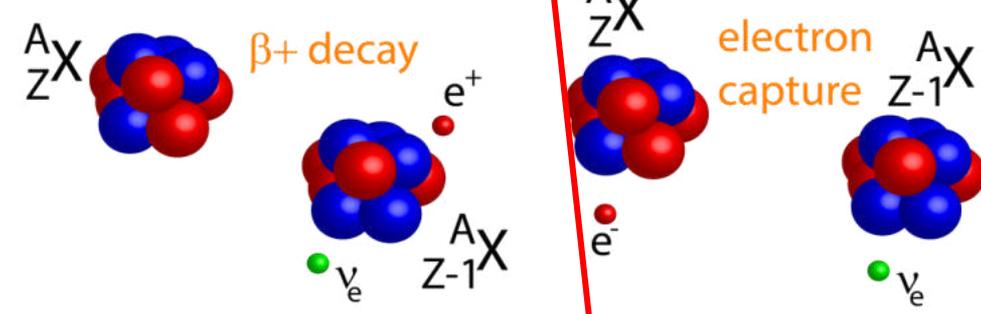
- Electron capture is mediated by the weak nuclear force
- EC Rates are dominated by allowed Gamow-Teller (GT) transitions at relatively low temperatures ( $\Delta L = 0, \Delta S = 1, \Delta T = 1$ )
- Direct measurement possible only for g.s. to g.s. and low-lying states transition through EC/ $\beta$  decay data.



# Charge-Exchange Reactions can Extract $B(GT)$



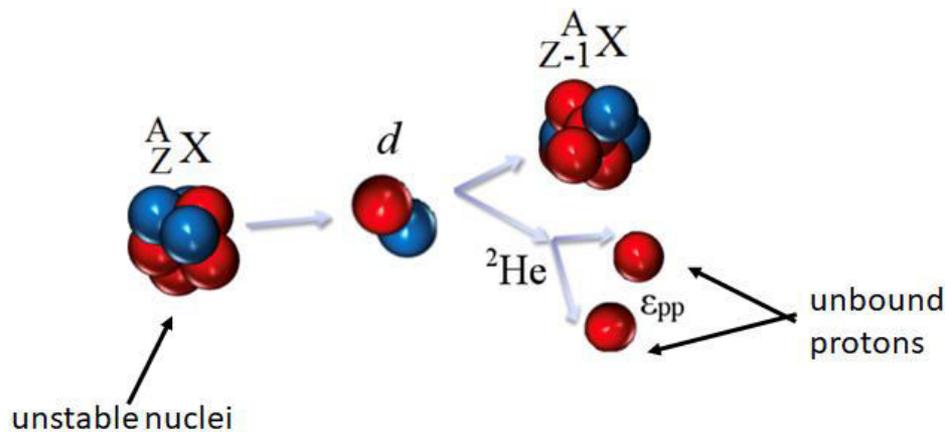
$$\left( \frac{d\sigma}{d\Omega}(q=0) \right)_{(d, {}^2\text{He})} = \hat{\sigma} B(GT)$$



unit cross-section

- Indirect measurement of  $B(GT)$  with  $(n,p)$ -type charge-exchange reactions at  $E_{beam} \sim 100$  MeV/u.

# $(d, {}^2\text{He})$ Reaction in Inverse Kinematics can be Used Across the Chart of Nuclei



${}^2\text{He}$  = a pair of protons coupled to  ${}^1\text{S}_0$  state:

- Incident deuteron is in  ${}^3\text{S}_1$  state, and the  $(d, {}^2\text{He})$  reaction proceeds almost exclusively by spin transfer ( $\Delta S = 1$ ), if  $\epsilon_{pp} < 2$  MeV.
- The proportionality between differential cross section and  $B(\text{GT})$  for the  $(d, {}^2\text{He})$  reaction in forward kinematics is well established.

[[GT) transitions ( $\Delta L = 0, \Delta S = 1, \Delta T = 1$ )]

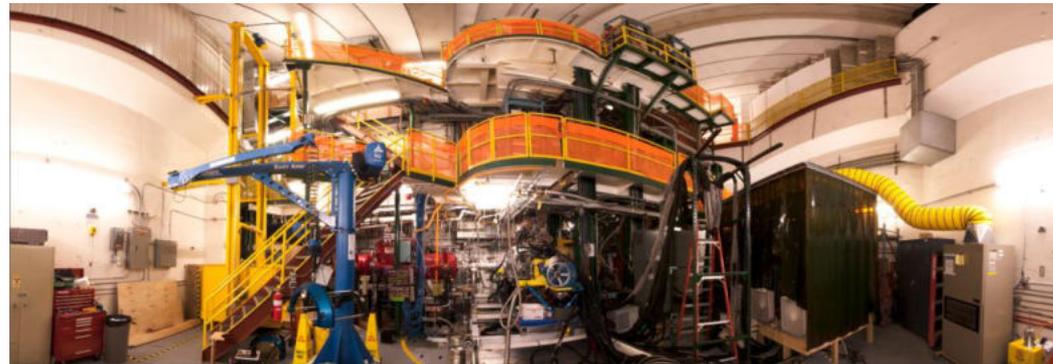
# First Experiment: $^{14}\text{O}(d,^2\text{He})$ Reaction in Inverse Kinematics

$^{14}\text{O}(d,^2\text{He})^{14}\text{N}$  reaction primary focus of the experiment (Giraud *et al.*)

- Novel use of an Active Target Time Projection Chamber to detect low-energy recoils from inverse kinematics experiment at low momentum transfer ( $q=0$ )
- Magnetic Spectrometer is used to detect reaction products ( $^{14}\text{N}$ , or one of its decay products after decay by particle emission)
- Technique can also be used for other reactions in inverse kinematics, e.g.,  $(p,p')$ ,  $(\alpha,\alpha')$ , etc.



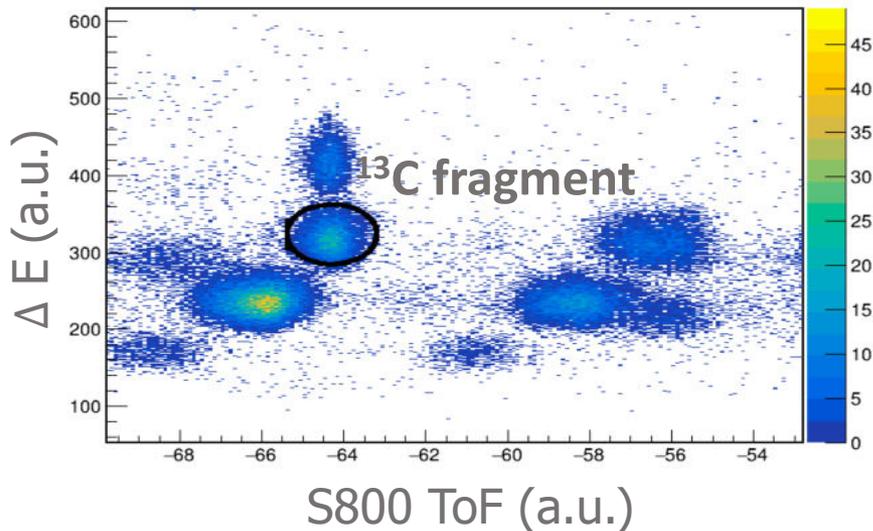
AT-TPC (Active-Target Time Projection Chamber) at the target location of the S800 for the experimental setup (before cabling).



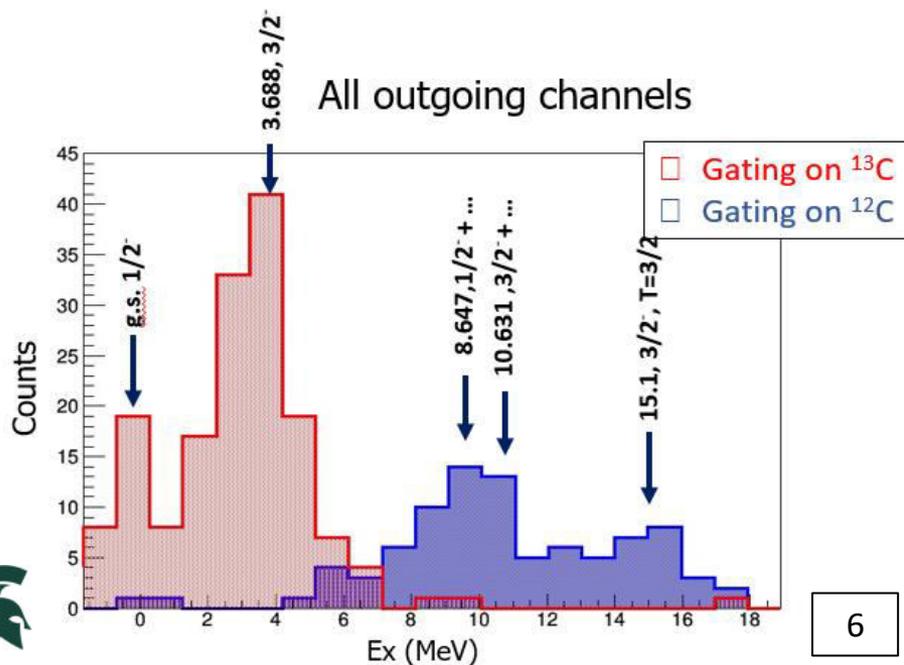
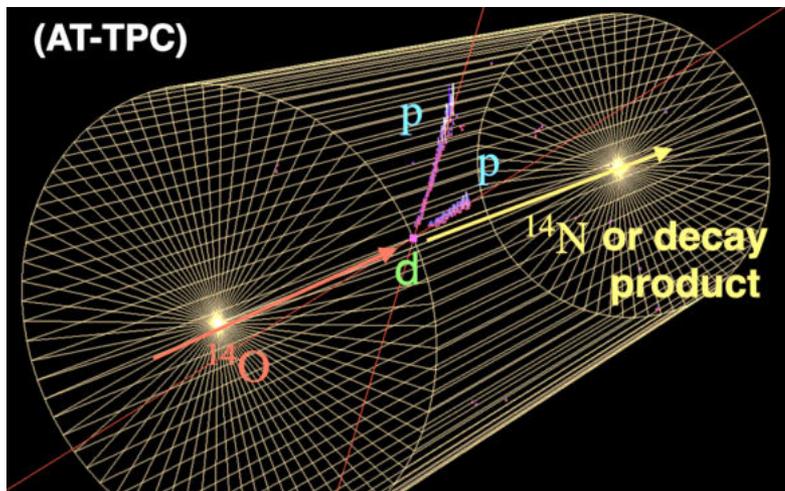
S800 without the AT-TPC in its target location.

# Reconstruction of Excitation Energy from PID and Analysis of Tracks in the AT-TPC

## Fragment Identification

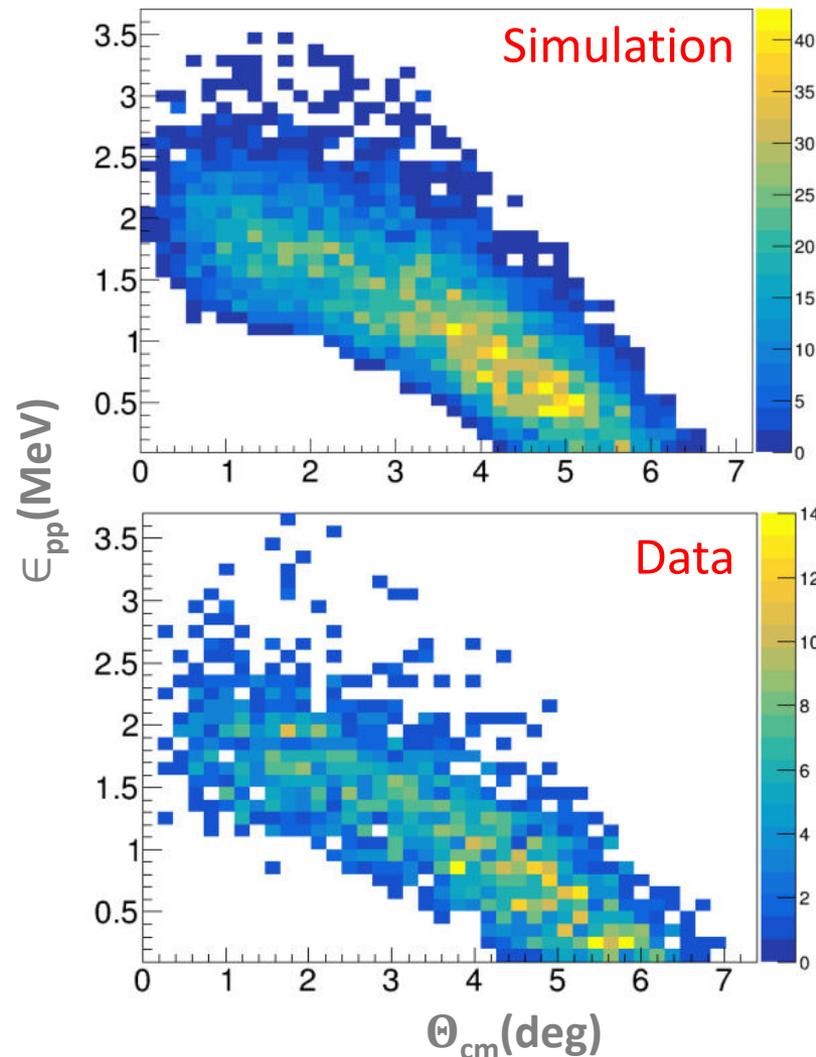


- AT-TPC readout provides the momentum vector of the two protons.
- Momentum and scattering angle of  $^2\text{He}$  is reconstructed.
- Excitation energy of the residual  $^{13}\text{C}$  and center of mass scattering angle is reconstructed.



# Simulation is Important for Understanding the Detector Response and Correction for Limited Acceptances

- FairRoot framework (GEANT4 + ROOT)
- Simulation is done in three main stages- event generator, digitalization, and reconstruction.
- Same analysis framework used for data and simulation.
- $\epsilon_{pp}$  acceptance depends on  $^2\text{He}$  scattering angle
- S800 momentum acceptances also included



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Full Length Article

Simulations and analysis tools for charge-exchange ( $d, ^2\text{He}$ ) reactions in inverse kinematics with the AT-TPC

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ABSTRACT

Charge-exchange ( $d, ^2\text{He}$ ) reactions in inverse kinematics at intermediate energies are a very promising method to investigate the Gamow-Teller transition strengths in unstable nuclei. A simulation and analysis software based on the `ARMCORR` package was developed to study this type of reactions with the active-target time projection chamber (AT-TPC). The simulation routines provide a realistic detector response that can be used to understand and benchmark experimental data. Analysis tools and correction routines can be developed and tested from simulations in `ARMCORR`, because they are processed in the same way as the real data. In particular, we study the feasibility of using coincidences with beam-like particles to unambiguously identify the ( $d, ^2\text{He}$ ) reaction channel, and to develop a kinematic fitting routine for future applications. More technically, the impact of space-charge effects in the track reconstruction, and a possible correction method are investigated in detail. This analysis and simulation package constitutes an essential part of the software development for the fast-beams program with the AT-TPC.

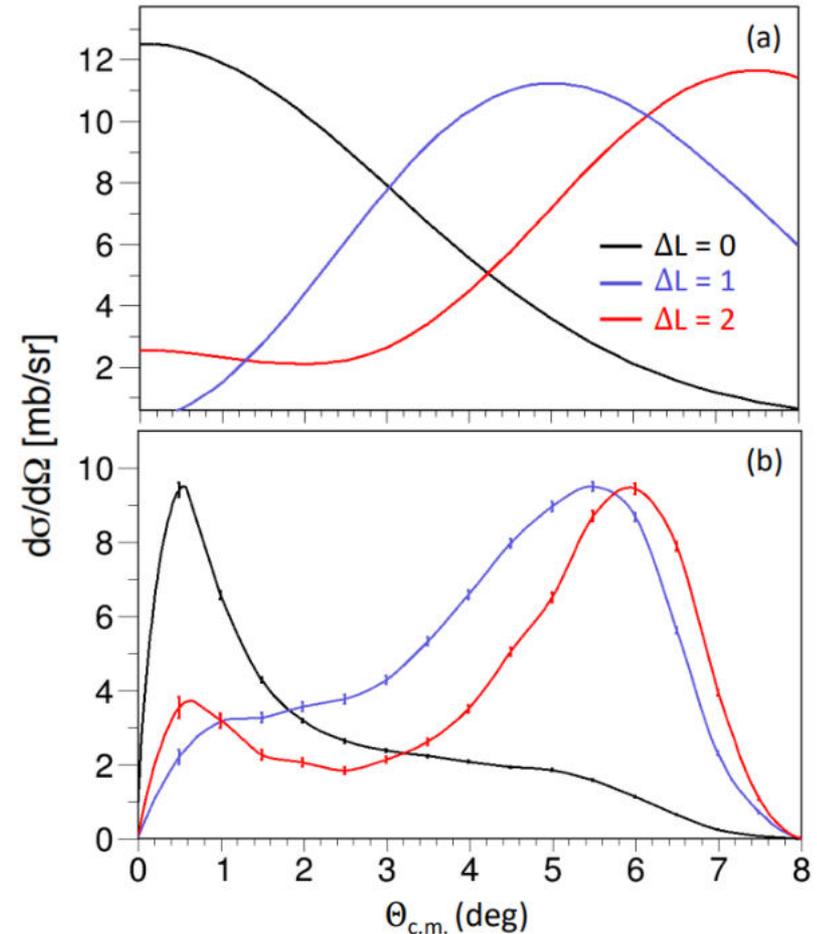
# Extraction of the GT ( $\Delta L = 0$ ) Component is Performed Through a Multipole Decomposition Analysis

[(GT) transitions ( $\Delta L = 0, \Delta S = 1, \Delta T = 1$ )]

$\Delta L = 0$  component extracted with Multipole Decomposition Analysis (MDA) on identified peaks:

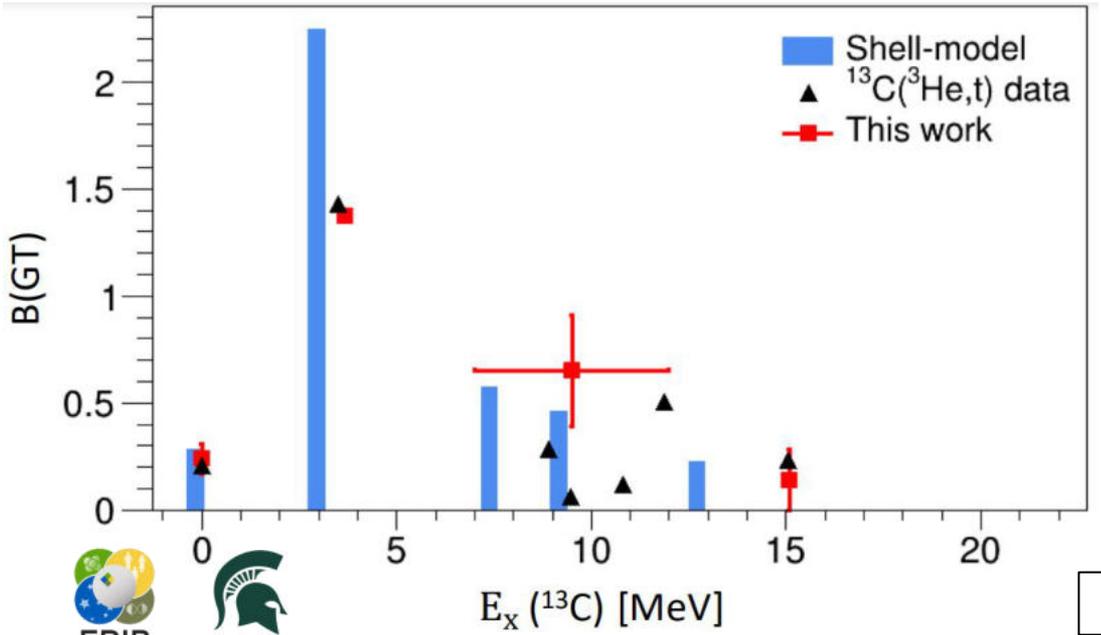
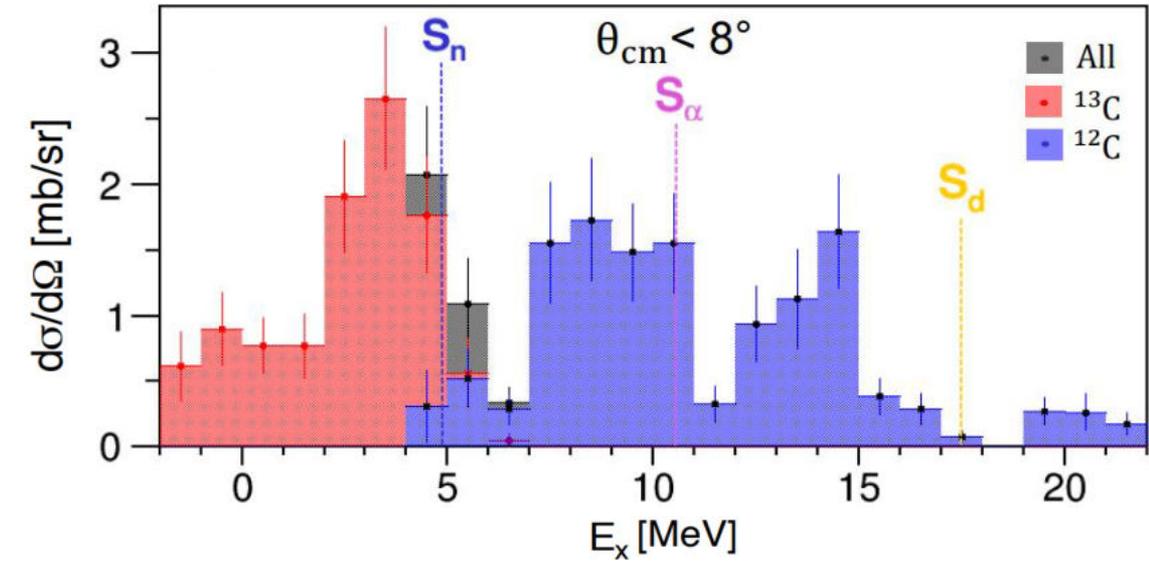
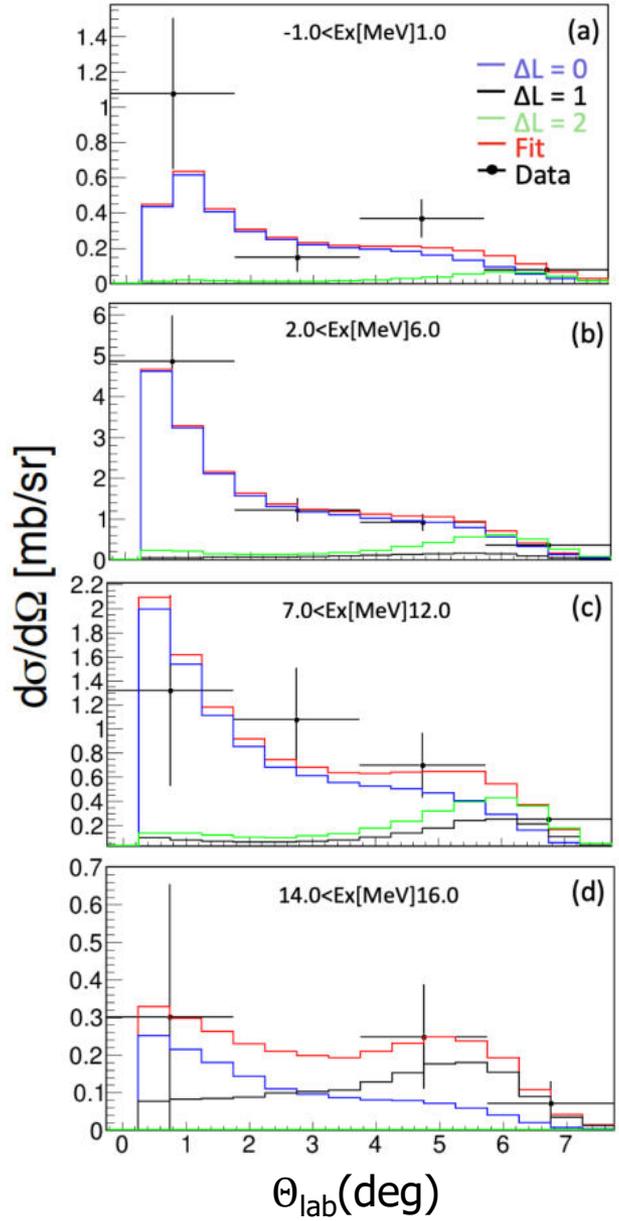
$$\frac{d\sigma}{d\Omega} = a_0 \left. \frac{d\sigma}{d\Omega} \right|_{\Delta L=0} + a_1 \left. \frac{d\sigma}{d\Omega} \right|_{\Delta L=1} + a_2 \left. \frac{d\sigma}{d\Omega} \right|_{\Delta L=2}$$

- ACCBA (Adiabatic Coupled-Channels Born Approximation) code is used to calculate theoretical differential cross-section. (H. Okamura (1999))
- $\frac{d\sigma}{d\Omega}$  from ACCBA is used in simulation to account for detector response as a function of  $\epsilon_{pp}$  and  $\theta_{c.m.}$ .



# Extracted Differential Cross Section

Multipole Decomposition Analysis



# Extracted GT Strengths: $^{14}\text{O}(d,^2\text{He})$

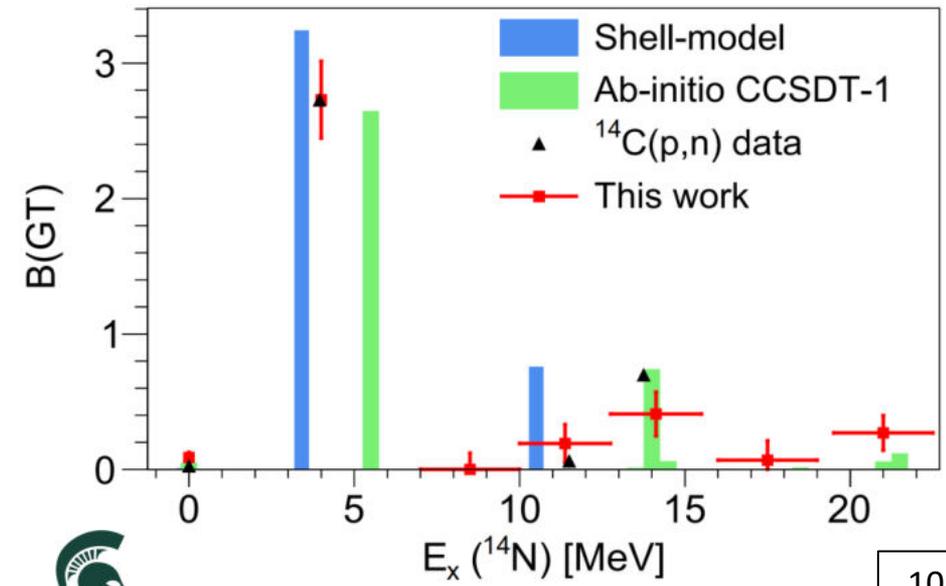
- Unit cross section calibrated to the strong transition to 3.95 MeV, known from  $\beta$ -decay
- Results consistent with  $^{14}\text{C}(p,n)$  for  $E_x < 15$  MeV
- Shell-model calculations reproduce strength-distribution reasonably well after application of a phenomenological quenching factor of 0.67, but does not predict strength for  $E_x > 15$  MeV
- CC calculation reproduced strength distribution well, without additional quenching, including high-lying strength  $E_x > 21$  MeV)

$\beta^+$  Gamow-Teller strengths from unstable  $^{14}\text{O}$  via the  $(d,^2\text{He})$  reaction in inverse kinematics

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(Dated: May 7, 2023)



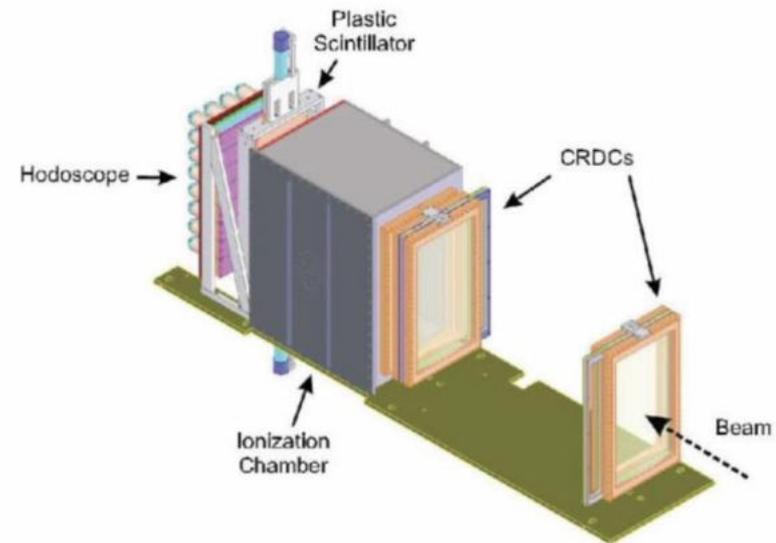
# Conclusions and Outlook

- The  $(d, ^2\text{He})$  reaction in inverse kinematics was developed successfully and used to extract Gamow-Teller strength from an unstable nucleus of to high excitation energies
- The use of an Active Target Time Projection Chamber in combination with a magnetic spectrometer is an effective tool for inverse kinematics experiments with fast beams in which the low-energy recoil particle is used to reconstruct the reaction kinematics
- For  $^{14}\text{O}$  It was confirmed that Coupled Cluster calculations based on first principles are able to reproduce Gamow-Teller strength distribution up to high excitation energies without phenomenological quenching -> promising path for heavier nuclei and nuclei far from stability
- The next  $(d, ^2\text{He})$  experiment in inverse kinematics is planned at FRIB – the goal is to perform experiment with gradually increase A and Z, of importance for electron captures in nuclear astrophysics

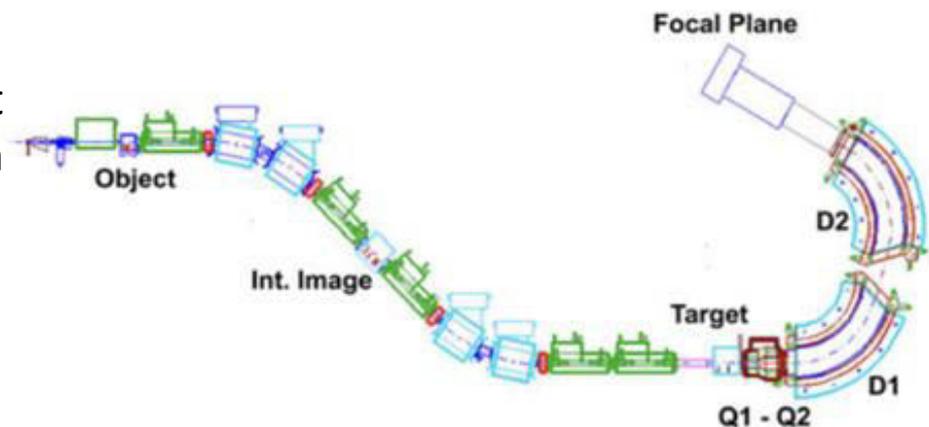


# The S800 Spectrometer is Used for Measuring Ejectiles and Triggering the AT-TPC Data Readout

- Cathode Readout Drift Chambers (CRDC) measure the position and angle at the focal plane, providing momentum and scattering angle
- A plastic scintillator gives the trigger for the data acquisition system and is used for particle identification by ToF measurement
- The ionization chamber allows indirect measurement of atomic number based on energy deposition



The S800 spectrometer



# ACKNOWLEDGEMENTS

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- R. G. T. Zegers<sup>1,2,3</sup>, S. Giraud<sup>1,2,3</sup>, J. C. Zamora<sup>2,5</sup>, D. Bazin<sup>1,2,3</sup>, Y. Ayyad<sup>2,6</sup>, S. Bacca<sup>7,8</sup>, S. Beceiro-Novo<sup>1,2,3</sup>, J. Chen<sup>3,4</sup>, G. Hagen<sup>9,10</sup>, M. DeNudt<sup>1,2,3</sup>, M. Cortesi<sup>1,2,3</sup>, C. Maher<sup>1,2,3</sup>, W. Mittig<sup>1,2,3</sup>, F. Ndayisabye<sup>1,2,3</sup>, S. Noji<sup>1,2,3</sup>, S. J. Novario<sup>9,10</sup>, J. Pereira<sup>1,2,3</sup>, J. M. Schmitt<sup>1,2,3</sup>, M. Serikow<sup>1,2</sup>, J. Surbrook<sup>1,2,3</sup>, L. Sun<sup>1,2</sup>, N. Watwood<sup>1,2</sup>, T. Wheeler<sup>1,2</sup>.

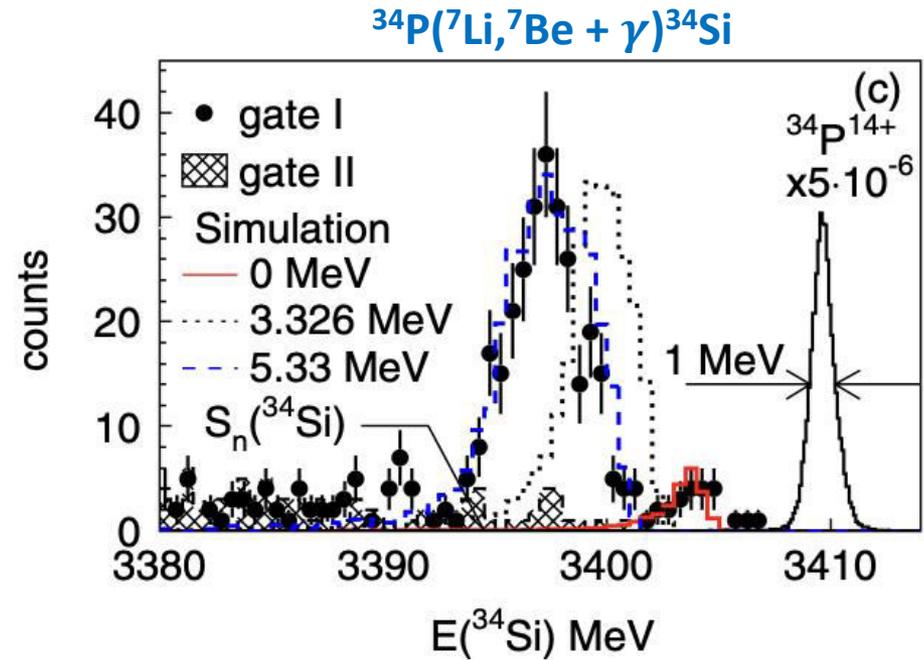
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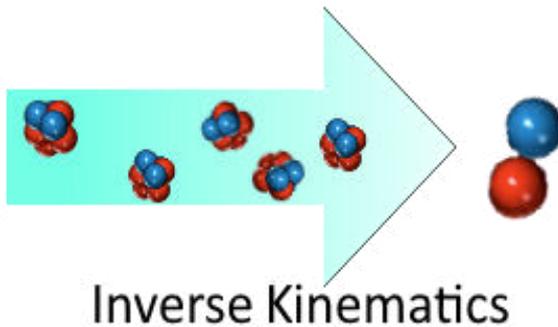
# Inverse Kinematics in Charge-Exchange Reactions for Studying Rare Isotope

$({}^7\text{Li}, {}^7\text{Be})$  probe has been successfully used to extract  $B(\text{GT})$  in inverse kinematics for studying unstable nuclei.

**Limitation:** Method relies on high precision momentum-tracking of the heavy ejectile and is limited to light ( $A < 35$ ) nuclei and excitation energies up to the particle separation energy



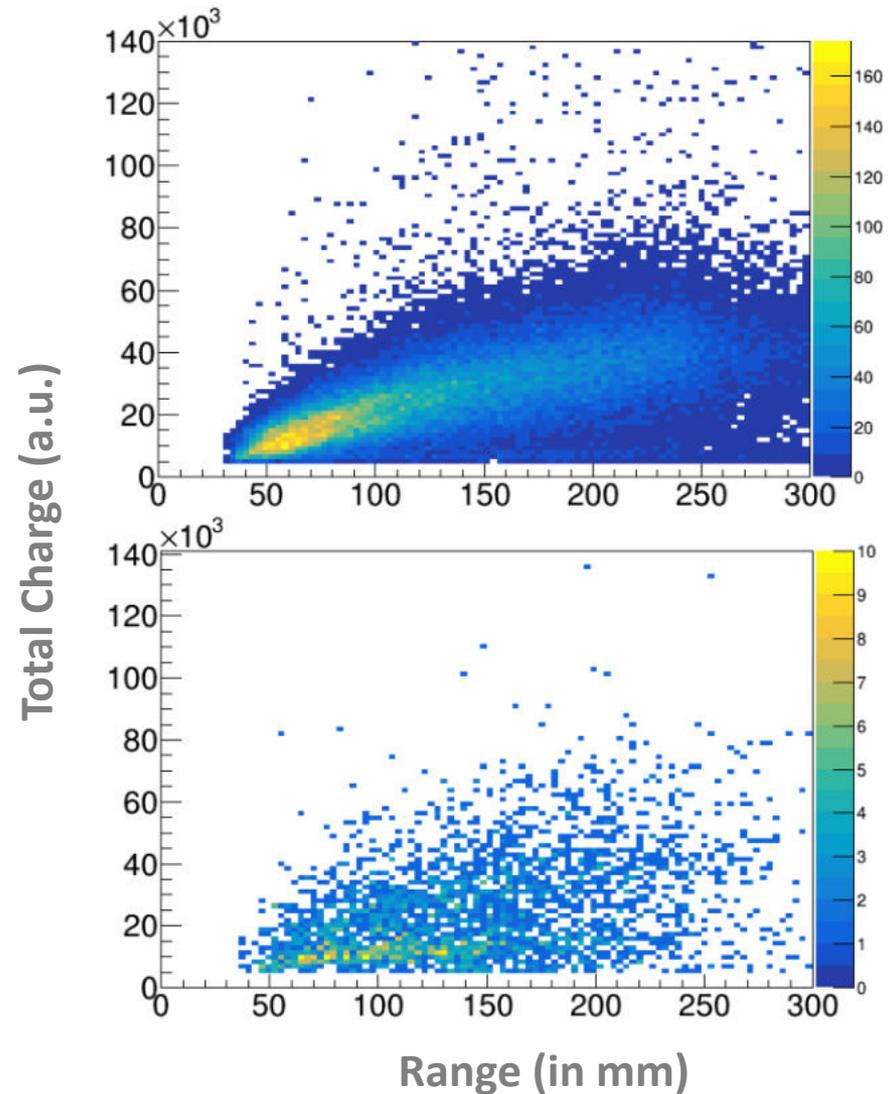
R. G. T. Zegers et al., Phys. Rev. Lett. 104, 212504 (2010)



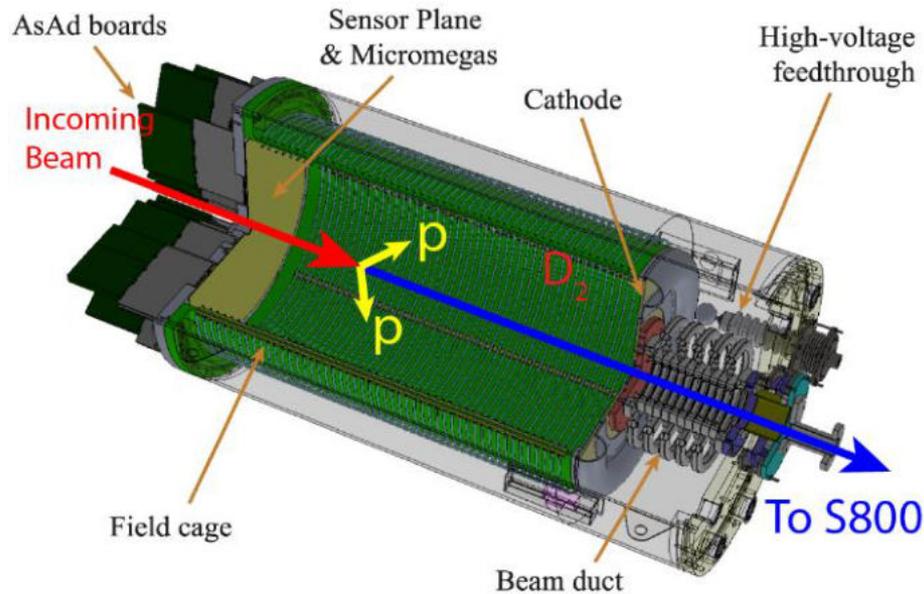
- $(n, p)$  ?
- $(t, {}^3\text{He})$  ?

# Background is Suppressed by Several Conditions in the Code

- The code identifies the beam-like particles in coincidence with two protons generated from the vertex.
- Electron events are removed by adding a threshold for total charge.
- A 2D gate on the distribution of the total charge against the particle range in the AT-TPC helps select proton tracks.
- The probability of two (d,p) events with a nearby vertex is in the order of 1% of the probability of a (d,<sup>2</sup>He) event.
- The combination of all conditions results in a nearly background free spectrum.



# AT-TPC is Used for Tracking the Two Protons From Unbound $^2\text{He}$



Allows Target Medium as a Target-Detection System

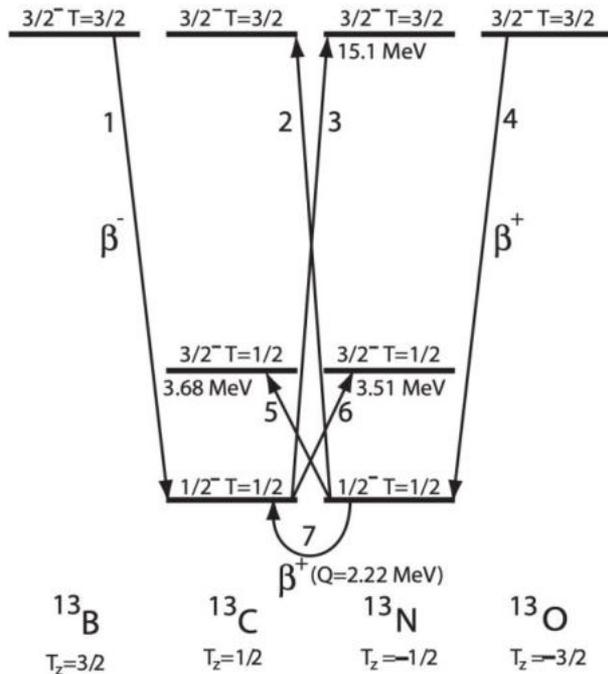
- Central region of the AT-TPC is insensitive so the beam intensity can be relatively high (0.2-0.7 Mpps).
- Energetic particles react with the gas ionizing it and strip off electrons from the target gas  $\text{D}_2$  as they travel.
- The electrons drift with uniform velocity towards the MicroMegas detector.
- Signals transmitted to the AsAd boards via high-density connectors feed the laboratory computer network for analysis.
- X and Y track information is reconstructed based on the location of the activated pad.
- The Z coordinate is the product of the drift velocity and the flight time.

# SUMMARY

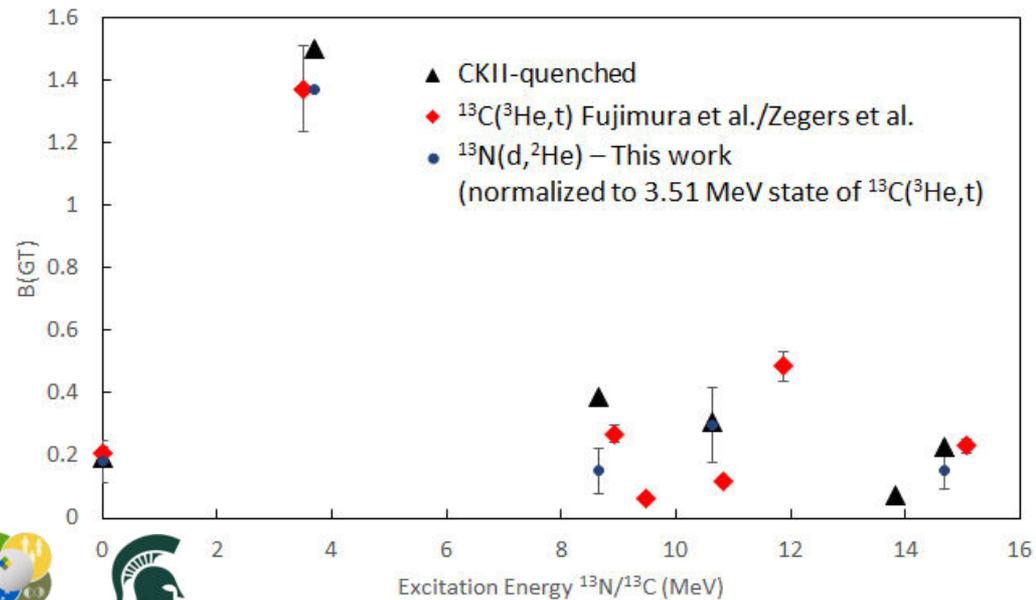
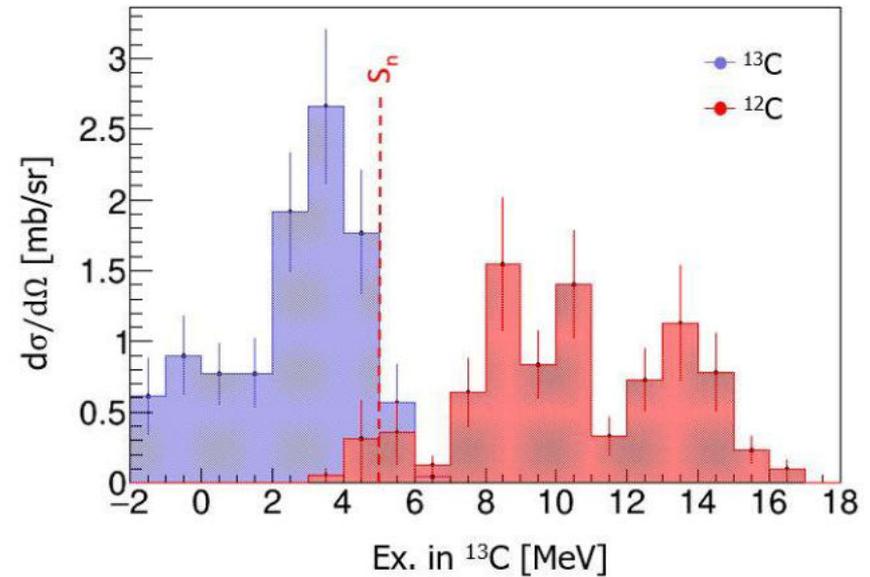
- EC rates are important for astrophysical phenomena such as core-collapse and thermonuclear supernovae, the crust of accreting neutron stars in binary systems, and the final core evolution of intermediate mass stars.
- Experiments needed to guide and benchmark the theoretical models.
- Accurate Gamow-Teller strength is necessary to estimate the EC rates in stellar environment.
- $(d, ^2\text{He})$  in inverse kinematics is the only probe for studying GT strength in unstable nuclei at all excitation energy and across the chart of nuclei.
- First  $(d, ^2\text{He})$  experiment in inverse kinematics was successfully run at the NSCL in 2020 using the AT-TPC and S800 spectrometer.
- Proposal for next  $(d, ^2\text{He})$  reaction in inverse kinematics has been accepted at FRIB.



# $^{13}\text{N}(d, ^2\text{He})$



Schematic of isospin analogous transitions in the  $A=13$  and  $T_z = \pm 1/2, \pm 3/2$ .



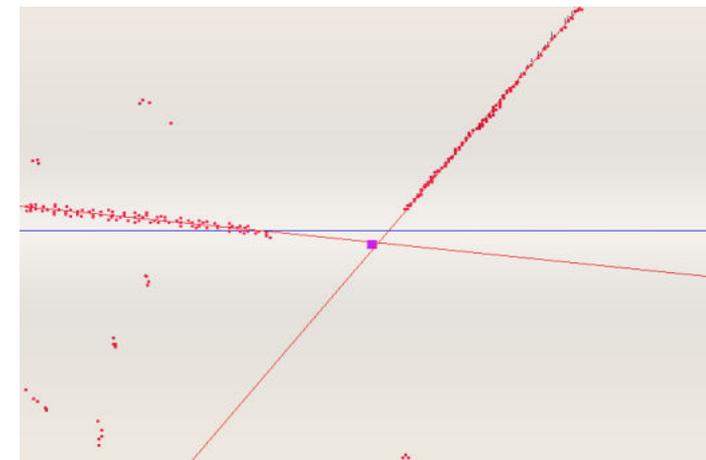
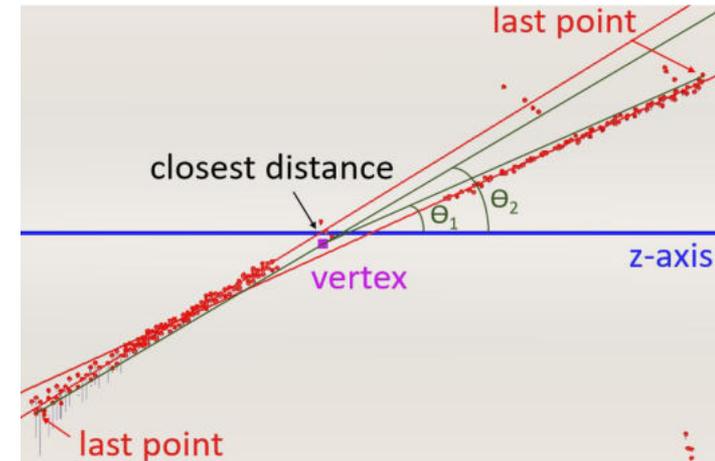
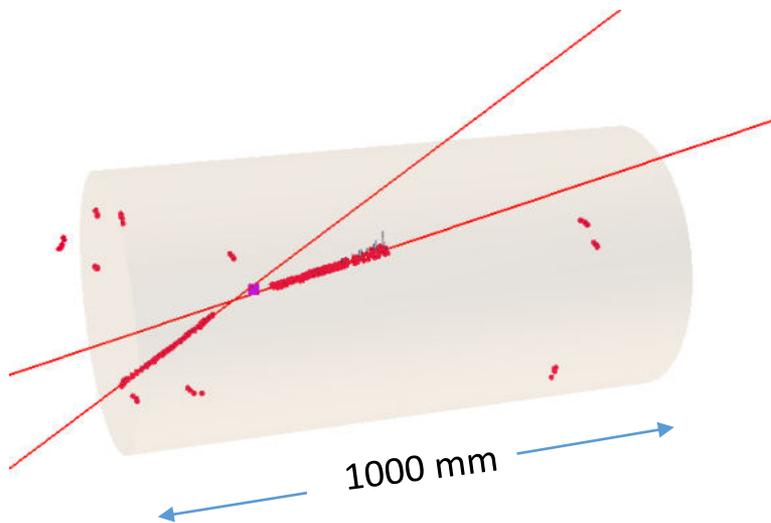
- $^{13}\text{N}(e^-, \nu_e)^{13}\text{C}$  reaction plays an Important Role in the Pre-Explosion Convective Phase of Type Ia Supernova



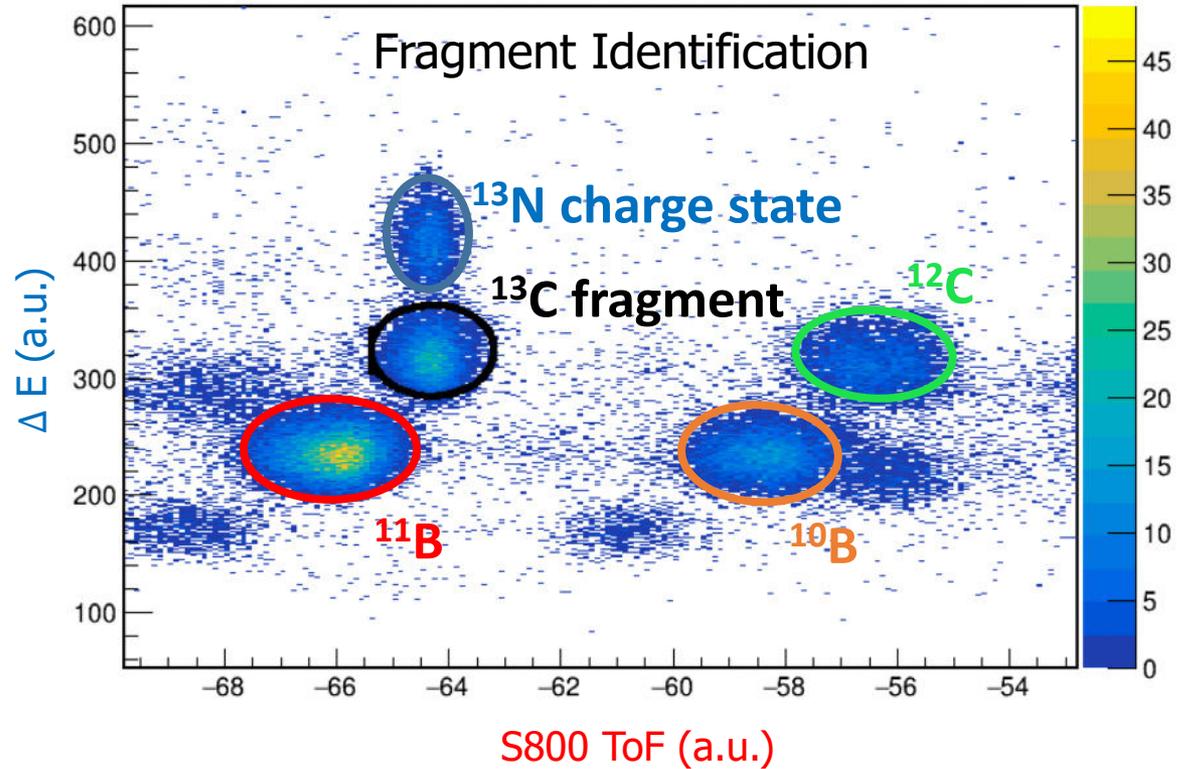
# Visualization of AT-TPC Events Inside the Volume

RANSAC (RANDOM SAMPLE CONSENSUS) algorithm is used to fit the point cloud of the AT-TPC and identify the ( $d, ^2\text{He}$ ) events.

- Vertex is the mean distance weighted by number of hits in each track
- Range is the distance between the position of the vertex and last point on fitted line



# Particle Identification using $\Delta E$ -ToF method



# EXPERIMENT

