

Equations of state of dense matter in the light of present and future nuclear physics and astrophysics constraints

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18th Russbach School on Nuclear Astrophysics



Neutron stars

- NSs are residues of supernovas

▷ NS are born hot $T \approx 10 - 100 \text{ MeV} \approx 10^{11} - 10^{12} \text{ K}$ $T_{M_\odot} \approx 1.57 \cdot 10^7 \text{ K}$

▷ $t(1 \text{ h}) \approx 10^9 \text{ K} \approx 100 \text{ keV}$; cooling by ν and γ emission

- mass range: $1M_\odot \lesssim M \lesssim 2M_\odot$

▷ $M_{\min}$, $M_{\max}$ inform on formation, EoS and composition

- radii $R \approx 10 - 15 \text{ km}$

$$R_{M_\odot} = 6.96 \cdot 10^5 \text{ km}$$

- average density $\approx 2 \cdot 10^{14} \text{ g/cm}^3 \approx \rho_0$

$$\rho_{M_\odot} \approx 1.4 \text{ g/cm}^3$$

- highly non-uniform $0 \lesssim \rho \lesssim 5 - 10\rho_0$

what are NS made of?

- compactness $0.1 \lesssim GM/c^2 R \lesssim 0.35$

$$C_{BH} = 0.5$$

- surface gravity is $7 \cdot 10^{12} \text{ m/s}^2$

$$g_{Earth} = 9.8 \text{ m/s}^2$$

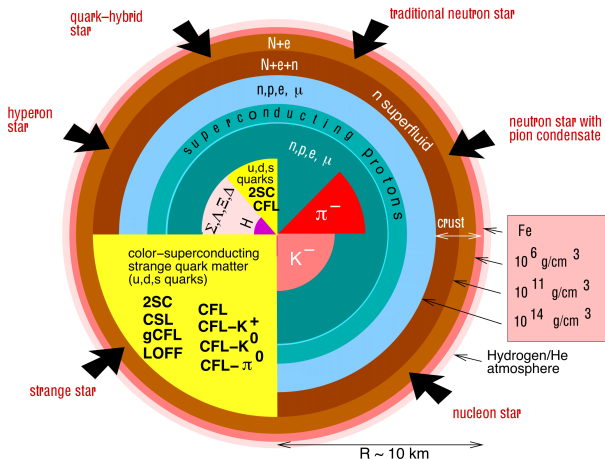
- fast spinning: $\nu = 716 \text{ Hz}$ (PSR J1748-2446)

- huge magnetic fields: $B = 10^{15} \text{ G}$

$$B_{Earth;core} = 25 \text{ G}, B_{RMN} = 10^5 \text{ G}$$

NS are labs for dense matter, General Relativity, physics of magnetic fields ...

Structure and Composition



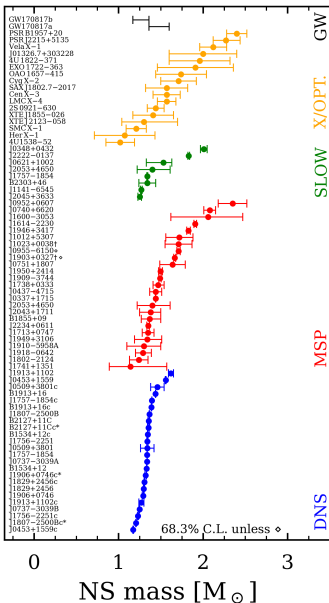
CRUST - A. Fantina's talk
 crystal struct. + pasta
 inhomogeneous
 nuclei, neutrons, electrons
uncertainties: inner crust,
 due to $E_{\text{sym}}(n)$

CORE - This talk
 homogeneous struct.
uncertain composition:
 nucleons, hyperons, pions,
 quarks, electrons, muons,
 due to $E(n, Y_e)$

Equation of State $P(e)$
 key for struct. and compo.

Image credit: F. Weber

Observables: Masses



[Suleiman et al., PRC104, 015801]

DNS: binaries with two neutron stars,

MSP: millisecond pulsars with $f > 50$ Hz ,

SLOW: slowly rotating pulsars with $f < 50$ Hz ,

X/OPT: measurement via X-ray or optical obs. ,

GW: measurements using detection of GW

Massive NS

PSR J1614-2230 ($M = 1.908 \pm 0.016 M_{\odot}$) [Demorest+, 2010; Arzoumanian+, 2018]; PSR J0348+0432 ($M = 2.01 \pm 0.04 M_{\odot}$) [Antoniadis+, 2013]; MSP J0740+6620 ($M = 2.08^{+0.07}_{-0.07} M_{\odot}$) [Fonseca+, 2021]; PSR J1810+1744 ($M = 2.13 \pm 0.04 M_{\odot}$) [Romani+, 2021]

Relevant for the composition of the core

Observables: Radii

Two measurements:

▷ **PSR J0030+0451** by NICER

$$R(1.44^{+0.15}_{-0.14} M_{\odot}) = 13.02^{+1.24}_{-1.06} \text{ km [Miller+, 2019]}$$

$$R(1.34^{+0.15}_{-0.16} M_{\odot}) = 12.71^{+1.14}_{-1.19} \text{ km [Riley+, 2019]}$$

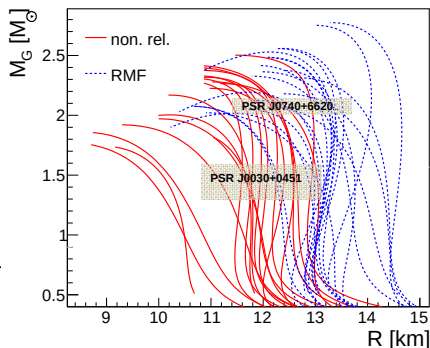
▷ **J0740+6620** by NICER+XMM Newton

$$R(2.08 \pm 0.07 M_{\odot}) = 13.7^{+2.6}_{-1.5} \text{ km [Miller+, 2021]}$$

$$R(2.072^{+0.067}_{-0.066} M_{\odot}) = 12.39^{+1.30}_{-0.98} \text{ km [Riley+, 2021]}$$

- uncertainties still large but enough to rule out a number of EOS

- more measurements from NICER and future LOFT, Athena missions



Data from CompOSE,
<https://compose.obspm.fr/>

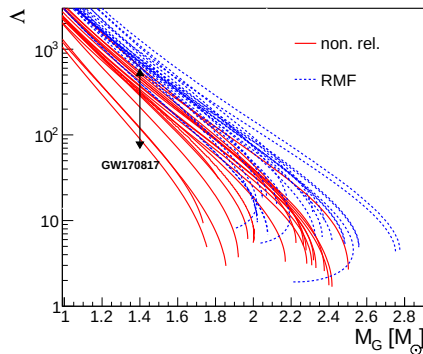
Observables: Tidal deformabilities

▷ the tidal deformability, Λ , describes how much body is deformed by tidal forces, which arise when two massive bodies orbit each other;

▷ GW170817 - detection of GW emitted by the merging of two NS with $M_T = 2.73^{+0.04}_{-0.01} M_\odot$ and $0.72 \leq q = M_2/M_1 \leq 1$

▷ tidal deformability $70 < \Lambda_{1.4} \leq 580$ [Abbott+, P 2018], constraint on the NS EOS over $2n_{\text{sat}} \lesssim n \lesssim 3n_{\text{sat}}$

- enough to rule out a number of realistic EOS



Data from CompOSE,
<https://compose.obspm.fr/>

Equations of state: Cold nuclear matter

$E/A(n, \delta)$ is Taylor expanded in terms of deviation from **isospin asymmetry**, $\delta = (n_n - n_p)/n$, and **saturation density**, $\chi = (n - n_{\text{sat}})/3n_{\text{sat}}$, with $n = n_n + n_p$.

$$\begin{aligned} E/A(n, \delta) &= E/A(n, 0) + S(n) \delta^2 + \dots \\ &= \underbrace{\sum_{i \geq 0} \frac{1}{i!} \chi_{\text{sat}}^{(i)} \chi^i}_{\text{energy SNM}} + \underbrace{\sum_{j \geq 0} \frac{1}{j!} \chi_{\text{sym}}^{(j)} \chi^j \delta^2}_{\text{symmetry energy}} + \dots \end{aligned}$$

$$\chi_{\text{sat}}^{(i)} = 3^i n_{\text{sat}}^i \left(\frac{\partial^i (E/A)}{\partial n^i} \right)_{n=n_{\text{sat}}, \delta=0}; \quad \chi_{\text{sym}}^{(j)} = 3^j n_{\text{sat}}^j \left(\frac{\partial^j S(n)}{\partial n^j} \right)_{n=n_{\text{sat}}, \delta=0}$$

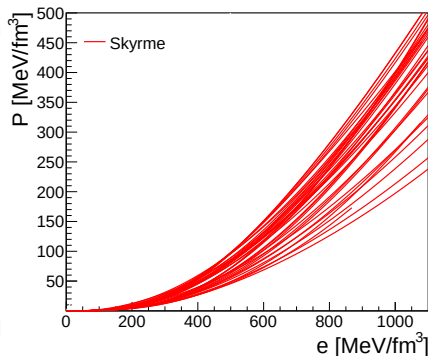
$i=0, 2, \dots$ binding energy per nucleon E_{sat} , incompressibility K_{sat} , etc. at n_{sat}
 $j=0, 1, 2, \dots$ **symmetry energy** J_{sym} and its slope L_{sym} , curvature K_{sym} , etc. at n_{sat}

▷ EOS exist for phenomenological and microscopic models

▷ **large uncertainties away from** $(n_{\text{sat}}, \delta \approx 0)$

Equations of state: Neutron Stars

- may be built from any model of eff. interactions
- NS EOS are 1D, $P(e)$
- composition determined by β -equilibrium, $\mu_n = \mu_p + \mu_e$
- correlations among properties of NS, NM and nuclei
- correlations are best investigated by Bayesian-like analysis, talks by A. Fantina and M. Beznogov
- how to build a NS? talk by A. Fantina
- at $n \gtrsim 2n_{\text{sat}}$, extra particles, hyperons, Δ s, π , quarks, can appear; onset densities depend of the effective interactions



- uncertainties away ($n_{\text{sat}}, \delta \approx 0$)
- dominated by $E_{\text{sym}}(n)$, which is poorly known
- largely different NS properties

Exotica in the core

- at $n \approx 2 - 3n_{\text{sat}}$ extra particle degrees of freedom may be populated: hyperons, $\Delta(1232)$, quarks, condensates [Glendenning, PLB, 1982]

Baryon	B	Q	S	I_3	J^Π	rest mass (MeV)		mean life (s)
Λ	1	0	-1	0	$1/2^+$	1115.683	uds	$2.60 \cdot 10^{-10}$
Σ^+	1	1	-1	-1	$1/2^+$	1189.37	uus	$8.02 \cdot 10^{-11}$
Σ^0	1	0	-1	0	$1/2^+$	1192.642	uds	$7.4 \cdot 10^{-20}$
Σ^-	1	-1	-1	1	$1/2^+$	1197.449	dds	$1.48 \cdot 10^{-10}$
Ξ^0	1	0	-2	-1/2	$1/2^+$	1314.83	uss	$2.90 \cdot 10^{-10}$
Ξ^-	1	-1	-2	1/2	$1/2^+$	1321.31	dss	$1.64 \cdot 10^{-10}$
Δ^{++}	1	2	0	-3/2	$3/2^+$	1232	uuu	$5.63 \cdot 10^{-24}$
Δ^+	1	1	0	-1/2	$3/2^+$	1232	uud	$5.63 \cdot 10^{-24}$
Δ^0	1	0	0	1/2	$3/2^+$	1232	udd	$5.63 \cdot 10^{-24}$
Δ^-	1	-1	0	3/2	$3/2^+$	1232	ddd	$5.63 \cdot 10^{-24}$

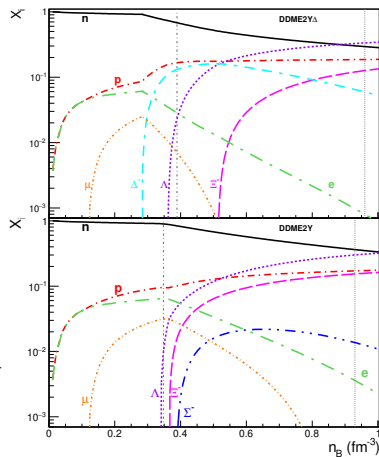
- few hundreds scattering events for $N\Lambda$ and $N\Sigma$
- spectroscopic data of single- and double-hypernuclei [$U_\Lambda^{(N)} \approx -28\text{MeV}$, $U_\Xi^{(N)} \approx -18\text{MeV}$, $U_\Sigma^{(N)} \approx 30\text{MeV}$], [Millener et al., 1998];
- pion-nucleus scattering and pion photo-production, electron scattering on nuclei and electromagnetic excitations of the Δ s provided $-30\text{ MeV} + U_N^{(N)} \leq U_\Delta^{(N)} \leq U_N^{(N)}$ [Drago+, 2014; Kolomeitsev+, 2017]

How to "build" a NS?

- "choose" the particles: baryons (n , p , Λ , $\Xi^{-,0}$, $\Sigma^{-,0,+}$, $\Delta^{-,0,+,++}$), mesons ($\pi^{-,0,+}$, $K^{-,0,+}$), and leptons (e^{-} , μ^{-})
- choose the approach and the nucleonic effective EOS
- tune the coupling constants of all exotic species
- for each n_B solve the equil. eqs.
 - ▶ $n_B = \sum_{i \in B} n_i$,
 - ▶ local net charge neutrality: $\sum_{i \in B} n_i + \sum_{\alpha \in L} n_\alpha = 0$,
 - ▶ chemical equilibrium for baryons: $\mu_i = Q_B \mu_B + Q_Q \mu_Q + Q_S \mu_S$,
 - ▶ chemical equilibrium for leptons $\mu_\alpha = Q_Q \mu_Q + Q_L \mu_L$
[strangeness not conserved $\mu_S = 0$; ν are not trapped $\mu_L = 0$]
 - ▶ "switch-on" particles with $\mu_i > m_i c^2$, $\mu_\alpha > m_\alpha c^2$
 - ▶ repeat until converged
- loop over n_B ; result: $n_i(n_B)$, $n_L(n_B)$, $P(n_B)$, $e(n_B)$, etc.
- with $P(e)$ solve Tolman-Oppenheimer-Volkoff (TOV) eqs.
- check causality, compliance with astrophys. data ($M_{max} \gtrsim 2M_\odot$, $R_{1.4}$, $R_{2.08}$, $\Lambda_{1.4}$)

NS with exotic cores: composition

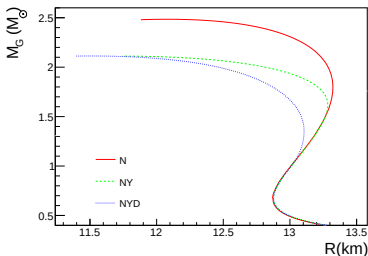
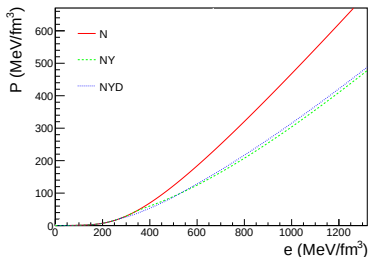
- particles' onset and abundances are decided upon rest mass, interaction potential, charge
- uncertainties in NN , NY , $N\Delta$ entail uncertainties in composition, especially at high n_B
- not all “allowed” species are present
 - ▶ hyperonic NS: only Λ , Ξ^- and Σ^-
 $n_\Lambda \approx 2n_{\text{sat}}$, $M_\Lambda \approx 1.5M_\odot$
 $n_{\Xi^-} \approx 2.5n_{\text{sat}}$, $M_{\Xi^-} \approx 1.6 - 1.8M_\odot$
 - ▶ Δ -admixed hyperonic NS: only Δ^- , Λ , Ξ^-
- change in abundances will impact $P(e)$, NS properties



[Raduta+, MNRAS (2020)]

NS with exotic cores: EOS softening, reduction of M_{max}

- exotic species soften the EOS
- exotic NS have lower M_{max}
compliance with $\approx 2M_{\odot}$ constraints
composition and interaction potentials
- exotic NS have smaller R , Λ
compliance with GW170817 constraints
interaction potentials



CompOSE

online repository for EOS (<https://compose.obspm.fr/>)

- stores thermodyn., composition, microscopic, transport properties in standardized format
- tabulation with respect to temperature (T), charge fraction (Y_Q), part. number density (n_B)
- wide ranges: $0.1 \leq T \text{ [MeV]} \leq 100$; $0.01 \leq Y_Q \leq 0.6$; $10^{-10} \leq n_B \text{ [fm}^{-3}] \leq 1 - 2$
- fine mesh; allows interpolation
- various types of EOS: cold neutron stars; neutron matter; “general purpose”, ready for input in simulations; from microscopic, phenomenological, schematic models; various particle d.o.f.

provides tools

- to sort by type; approach; particle composition; prop. of NM; group of authors
- to compute thermodyn. quantities, thermal coefficients,
- to extract information for arbitrary thermodyn. conditions,

modular; constantly upgrading

[Typel, Oertel, Klaehn, Phys.Part.Nucl. (2015); Typel et al., Eur.Phys.J.A (2022)]

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Eos Table +

<https://compose.obspm.fr/table/fam=3/part=3/home=3>



CompStar Online Supernovae Equations of State

EoS

Family : Cold Neutron Star EoS
 Particles : models with hyperons
 C.M. Homogeneous Matter : Relativistic density functional models

Show entries

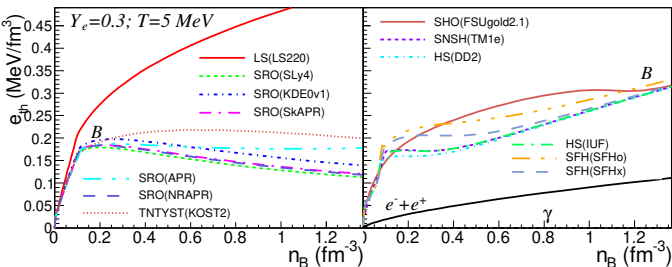
Npartes	Name	Family	Particles Content	C.M. Homogeneous	C.M. Inhomogeneous	Particles	T min [MeV]	T max [MeV]	T pts	nB min [fm ⁻³]	nB max [fm ⁻³]	nB pts
3	[DSGCM] 5	Cold Neutron Star EoS	models with hyperons	Relativistic density functional models	—	np&B	0	0	1	0.03	1.9	187
3	[DSGCM] 1 with crust	Cold Neutron Star EoS	models with hyperons	Relativistic density functional models	Non unified models (crust model matched)	np&B&L	0	0	1	3e-07	3	1191
3	[DSGCM] 4 with crust	Cold Neutron Star EoS	models with hyperons	Relativistic density functional models	Non unified models (crust model matched)	np&B	0	0	1	3e-07	3	1129
3	[DSGCM] 6 with crust	Cold Neutron Star EoS	models with hyperons	Relativistic density functional models	Non unified models (crust model matched)	np&B&L	0	0	1	3e-07	3.9	1223
3	[DSGCM]-1	Cold Neutron Star EoS	models with hyperons	Relativistic density functional models	—	np&B	0	0	1	0.03	2	303
3	OPUS(DSGM1) (with hyperons)	Cold Neutron Star EoS	models with hyperons	Relativistic density functional models	Non unified models (crust model matched)	np&B	0	0	1	7.9e-15	1.1	303
3	[DSGCM]-2	Cold Neutron Star EoS	models with hyperons	Relativistic density functional models	—	np&E	0	0	1	0.03	2	303
3	[DSGCM]-4	Cold Neutron Star EoS	models with hyperons	Relativistic density functional models	—	np&E	0	0	1	0.03	3	303
3	[DSGCM] 4 with crust	Cold Neutron Star EoS	models with hyperons	Relativistic density functional models	Non unified models (crust model matched)	np&B	0	0	1	3e-07	1.9	1823
3	OPUS(DSGM14) (with hyperons)	Cold Neutron Star EoS	models with hyperons	Relativistic density functional models	Non unified models (crust model matched)	np&B	0	0	1	7.9e-15	1.1	303
3	[DSGCM] hadronic (cold neutron stars) with crust	Cold Neutron Star EoS	models with hyperons	Relativistic density functional models	Non unified models (crust model matched)	np&B&L	0	0	1	3e-07	3	1191
3	[DSGCM] 3 with crust	Cold Neutron Star EoS	models with hyperons	Relativistic density functional models	Non unified models (crust model matched)	np&B&L	0	0	1	3e-07	3	1129
3	[DSGCM]-6	Cold Neutron Star EoS	models with hyperons	Relativistic density functional models	—	np&E	0	0	1	0.03	1.9	187
3	[DSGCM]-5	Cold Neutron Star EoS	models with hyperons	Relativistic density functional models	—	np&B&L	0	0	1	0.03	3	303
3	[DSGCM] 2 with crust	Cold Neutron Star EoS	models with hyperons	Relativistic density functional models	Non unified models (crust model matched)	np&B	0	0	1	3e-07	3	1191
3	OPUS(DSGM7) (with hyperons)	Cold Neutron Star EoS	models with hyperons	Relativistic density functional models	Non unified models (crust model matched)	np&B	0	0	1	7.9e-15	1.1	308
3	[DSGCM] Hadronic (cold neutron stars)	Cold Neutron Star EoS	models with hyperons	Relativistic density functional models	—	np&B & L	0	0	1	0.03	3	303
3	OPUS(DSGM10) (with hyperons)	Cold Neutron Star EoS	models with hyperons	Relativistic density functional models	Non unified models (crust model matched)	np&B	0	0	1	7.9e-15	0.99	307

EOS for CCSN and BNS

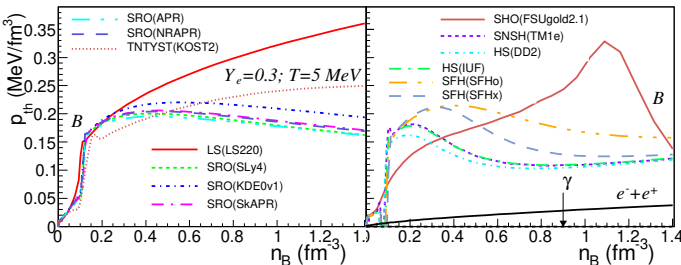
- from 1991 to 2010 only two EoS:
 - (1) Lattimer & Swesty (LS) [NPA 535, 331 (1991)];
 - (2) Shen, Toki, Oyamatsu & Sumiyoshi (STOS) [NPA 637, 435 (1998)]
- in June, 2021
 - about 100 EOS models are now available,
 - 36 EOS with exotic d.o.f. (Λ , hyperons, hyperons and Δ , π , K , quarks)
 - different features:
 - effective interactions: Skyrme, Covariant Density Functionals, ab-initio;
 - various NM properties, i.e. n_{sat} , E_{sat} , K_{sat} , J_{sym} , L_{sym} , K_{sym} , m_{eff} [not always in accord with constraints];
 - still far from exhausting the parameter space

Finite temperature - nucleonic models

Thermal contrib.: $X_{th} = X(n_B, Y_e, T) - X(n_B, Y_e, 0)$



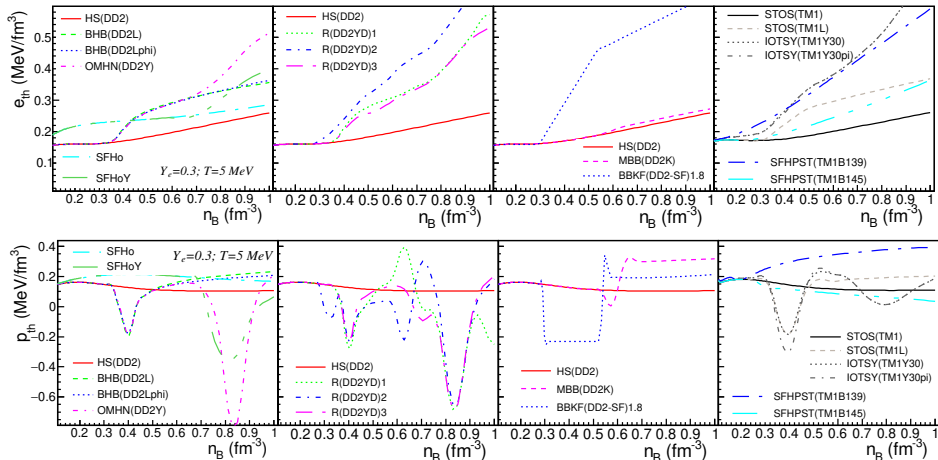
- non-rel. and RMF models behave differently; strong model dependence; so far unexplored



- in Skyrme-like models thermal effects are determined by m^*

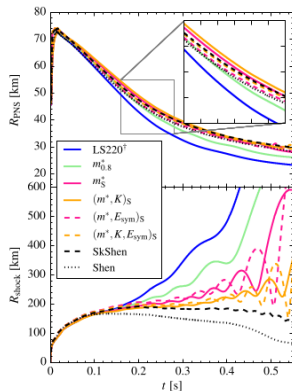
Thermal energy and pressure: models with exotica

Thermal contrib.: $X_{th} = X(n_B, Y_e, T) - X(n_B, Y_e, 0)$

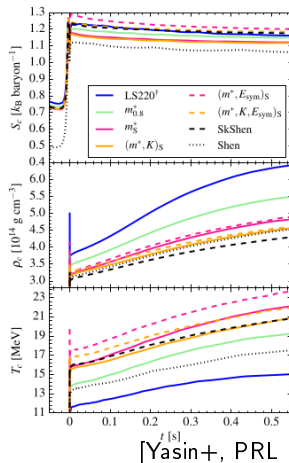


- the larger the number of particle d.o.f. the larger e_{th} ; [Raduta, EPJA (2022)]
- nucleation of exotic d.o.f. diminishes p_{th} ; under specific conditions $p_{th} < 0$

Early post-bounce evolution



$m^*/m = 1$ (LS220), 0.634 (Shen)

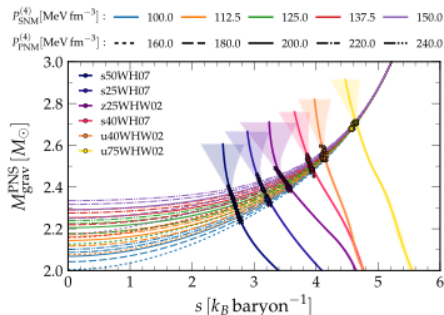
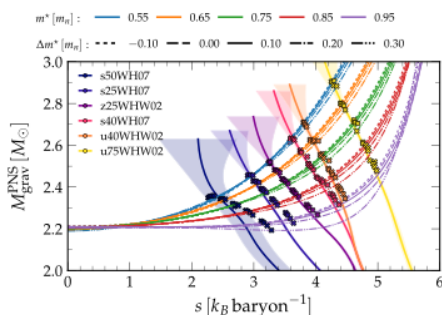


[Yasin+, PRL (2020)]

large $m^* \rightarrow$ fast explosion; fast contraction of PNS; high (low) ρ_c (T)

large $m^* \rightarrow$ high (low) T (n_B and R) in the ν -sphere; large E_ν , L_ν [Schneider+, ApJ(2020)]

BH formation in failed CCSN



[Schneider et al., ApJ (2020)]

simulation results: collapse begins when hot core's gravitational mass exceeds the maximum gravitational mass predicted by the EoS under the specific thermo conditions;

most important ingredients: progenitor and m^*

Conclusions

- Neutron Stars: definition, structure, composition, observables
- Equation of State: constraints, exotic particle d.o.f.
- CompOSE: an online repository of EOS
- Finite-temperature EOS

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- * Nuclear physics for astrophysics
- * Stellar evolution: Compact stars and supernovae
- * Astroparticle physics
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