

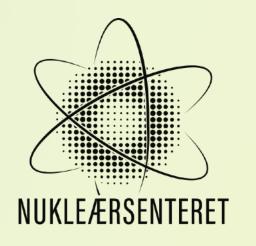
https://doi.org/10.1103/2h2s-sbyx



A saga on the y-decay branching ratio of the Hoyle state at the Oslo Cyclotron Laboratory

HELIUM25 - Dresden, Germany, 22.07.2025

Supervisors: Sunniva Siem and Kevin Ching Wei Li

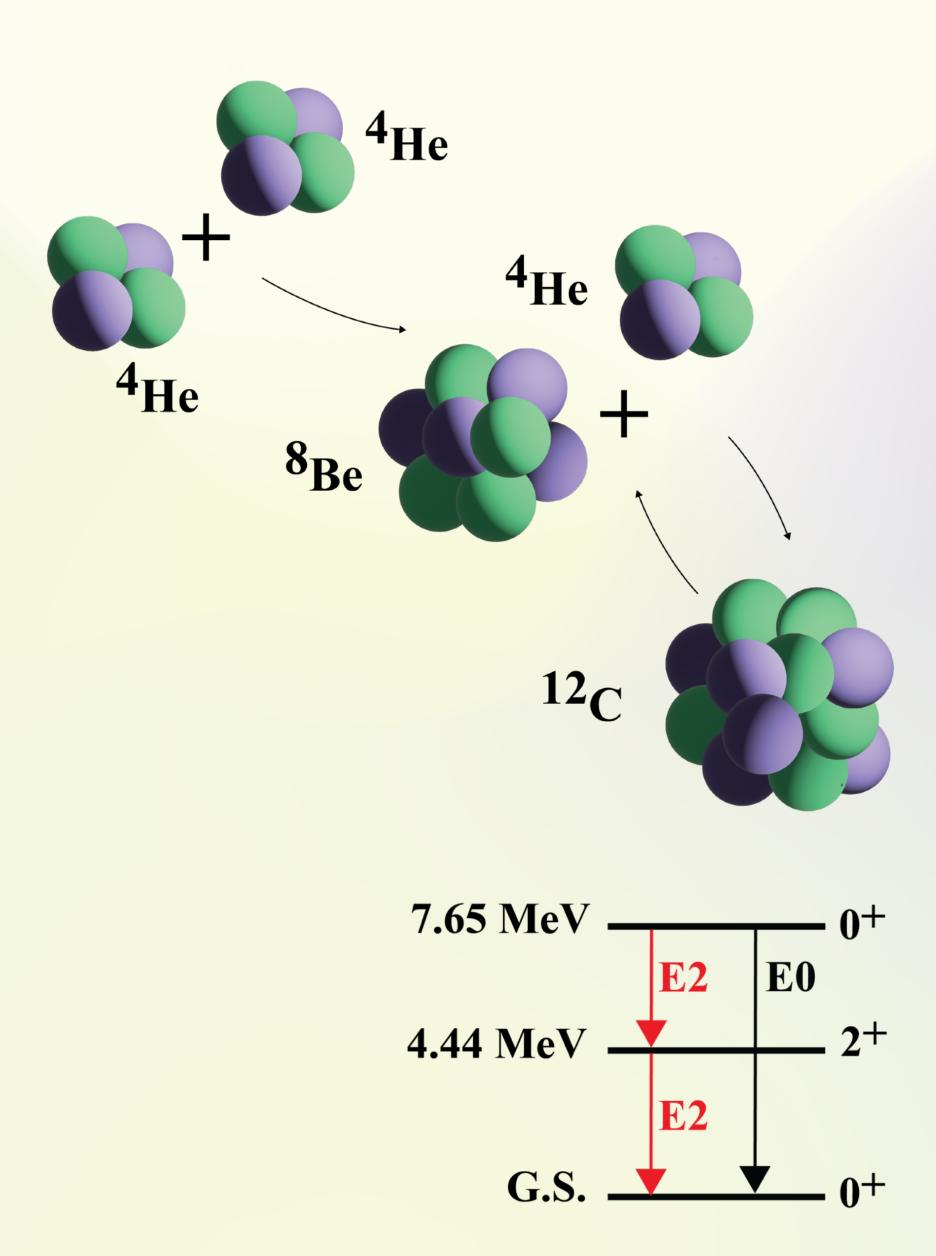


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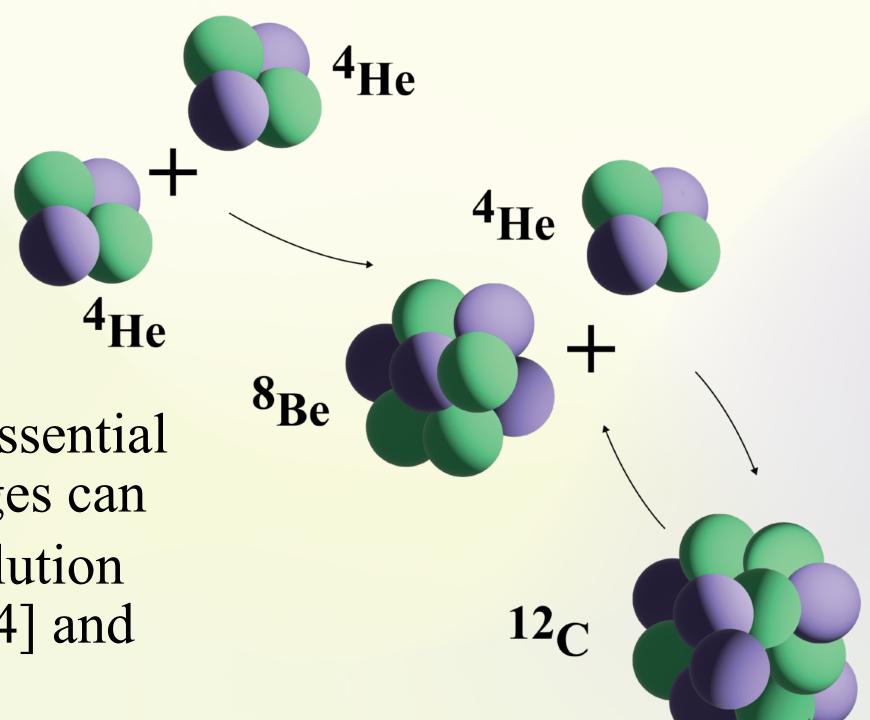
At medium stellar temperatures of T = 0.1-2.0 GK the dominant reaction mechanism of the triple- α process is two-step sequential fusion through the Hoyle state in ¹²C (Freer *et al.* (2014) [1]).

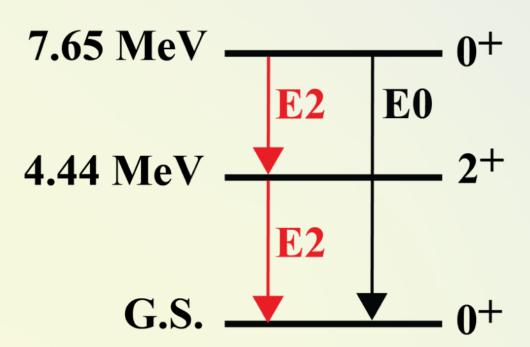




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Accurate measurement of the Hoyle state's radiative width is essential for determining the triple-α process rate, as even minor changes can significantly influence elemental abundances and stellar evolution (Bear *et al.* (2017), Jin *et al.* (2020), Wanajo *et al.* (2011) [2-4] and full talk by Aldara Grichener).





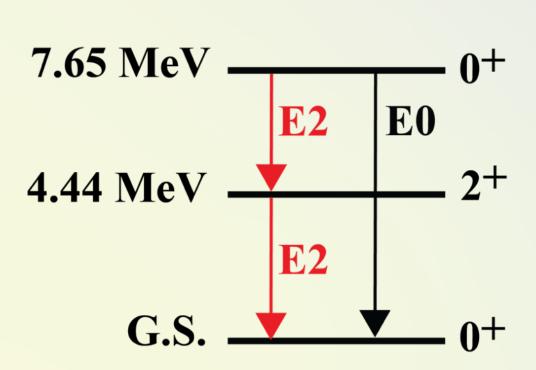


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4] and
12C

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The rate of the triple- α is crucial not only for the production of 12 C, it also influences the subsequent 12 C(α,γ) 16 O reaction rate (deBoer *et al.* (2017), deBoer *et al.* (2025) [5-6]). The balance of the C/O ratio, a key factor in stellar evolution (Woosley *et al.* (2021), Shen *et al.* (2023) [7-8] and full talk by Aldara Grichener) depends on the accuracy of the observables from these reactions.

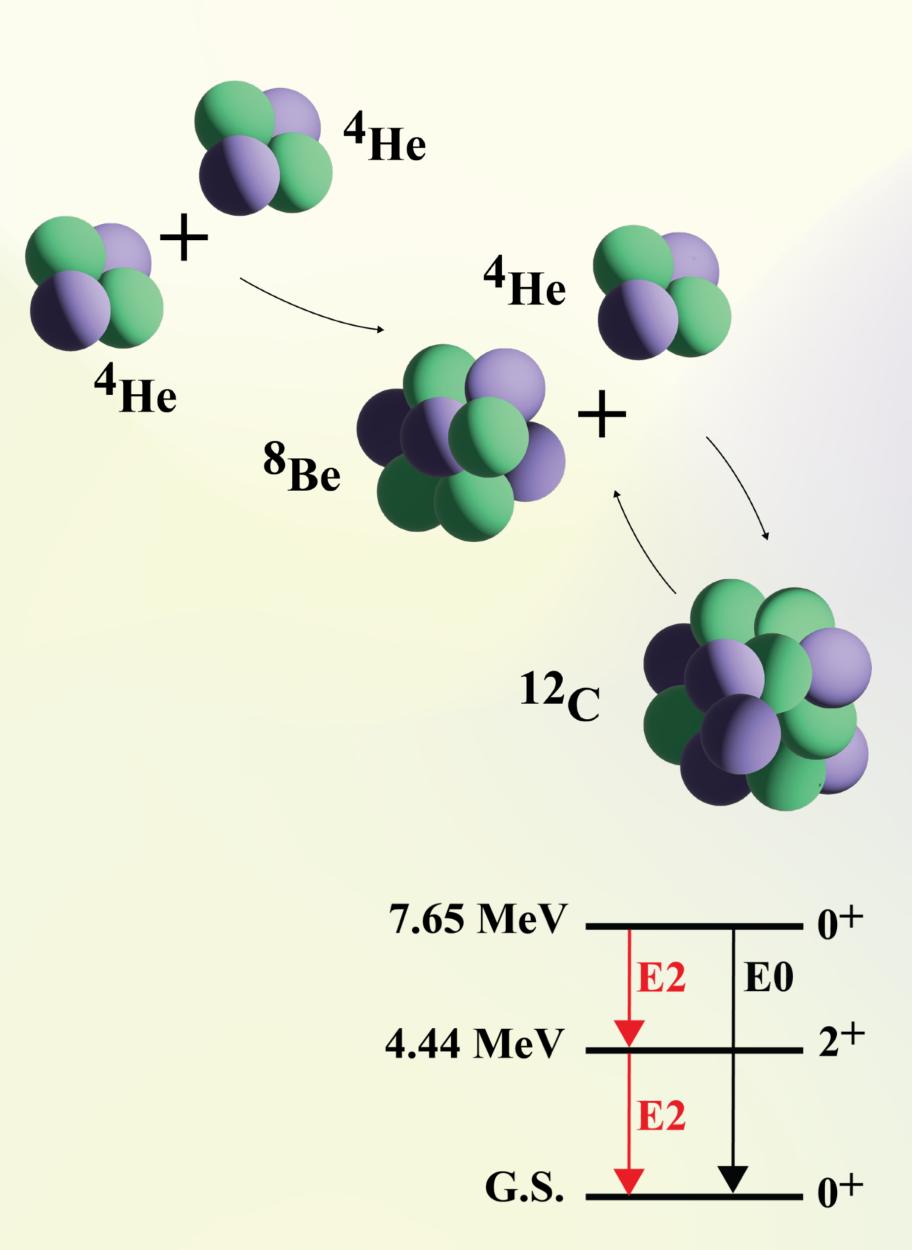




The radiative width of the Hoyle state cannot be measured directly, but it can be deduced indirectly with three independently measured quantities as

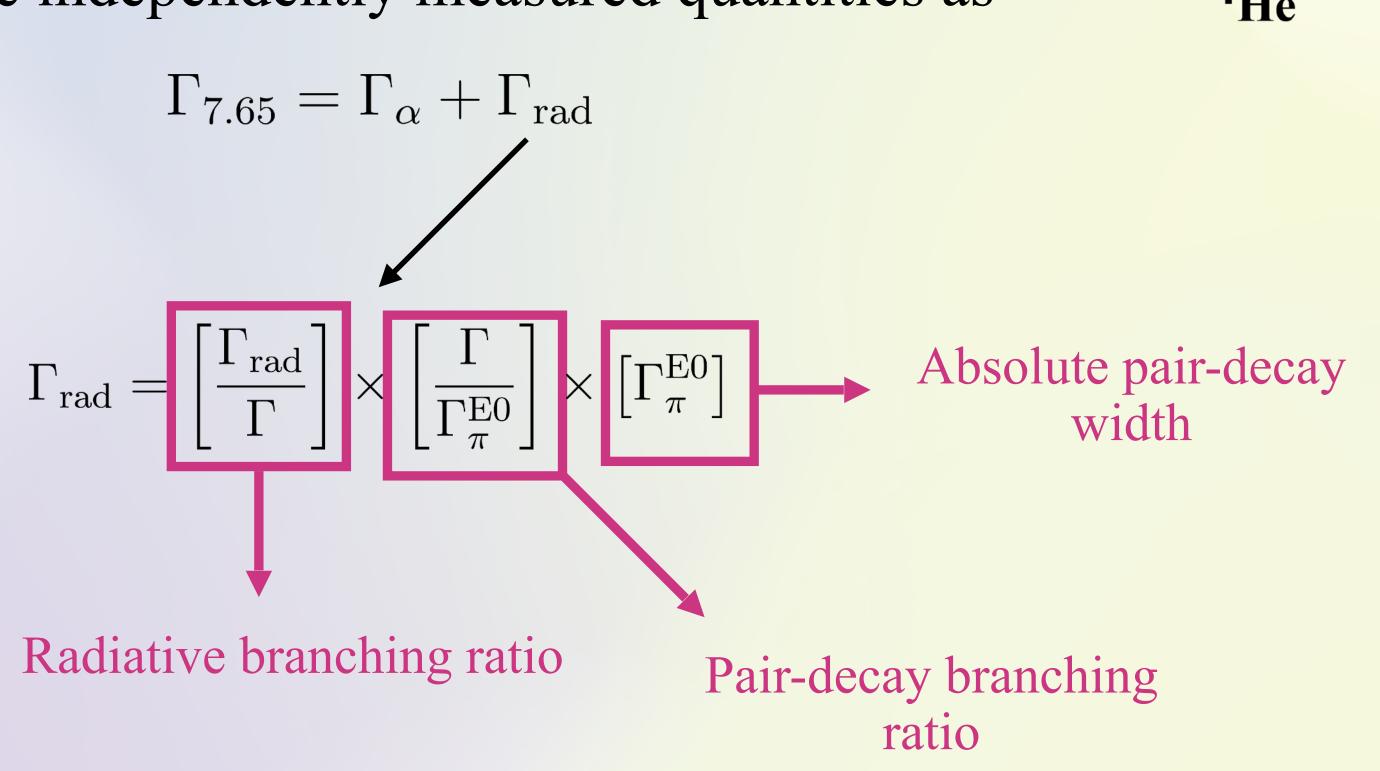
$$\Gamma_{7.65} = \Gamma_{\alpha} + \Gamma_{\mathrm{rad}}$$

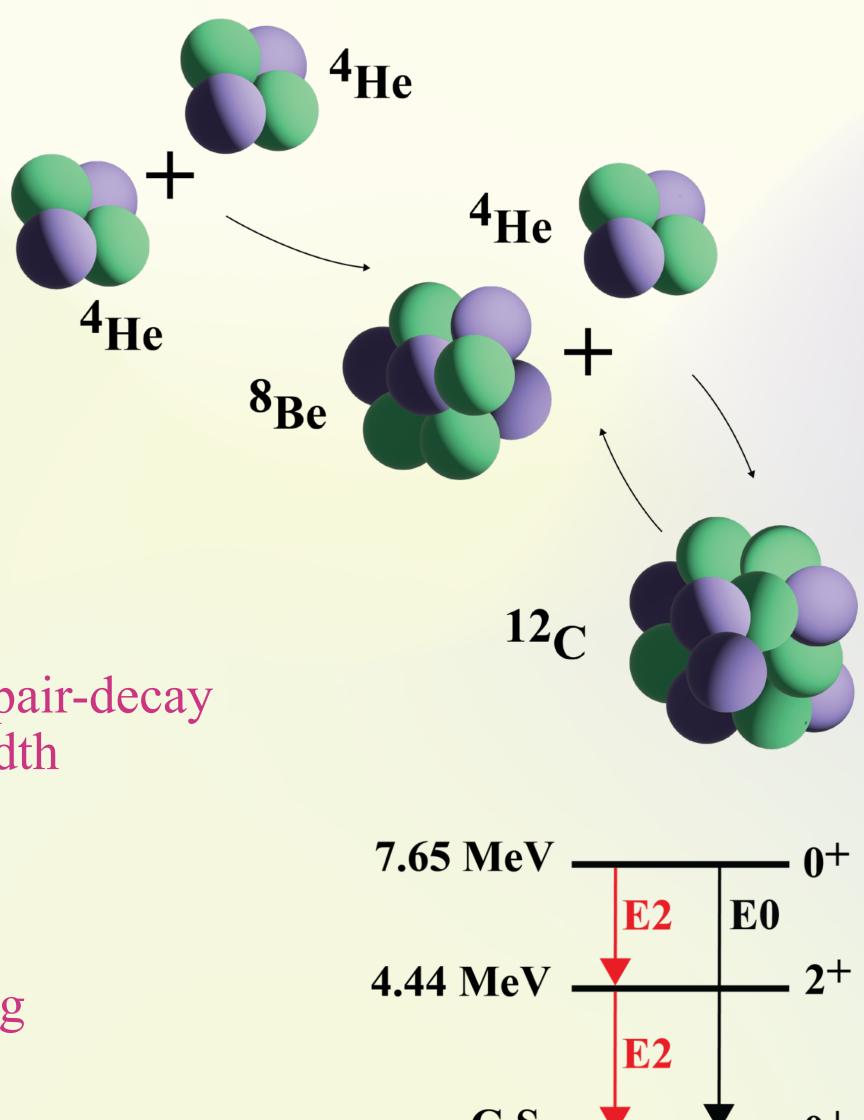
$$\Gamma_{\mathrm{rad}} = \left[\frac{\Gamma_{\mathrm{rad}}}{\Gamma}\right] \times \left[\frac{\Gamma}{\Gamma_{\pi}^{\mathrm{E0}}}\right] \times \left[\Gamma_{\pi}^{\mathrm{E0}}\right]$$





The radiative width of the Hoyle state **cannot** be measured **directly**, but it can be **deduced indirectly** with three independently measured quantities as

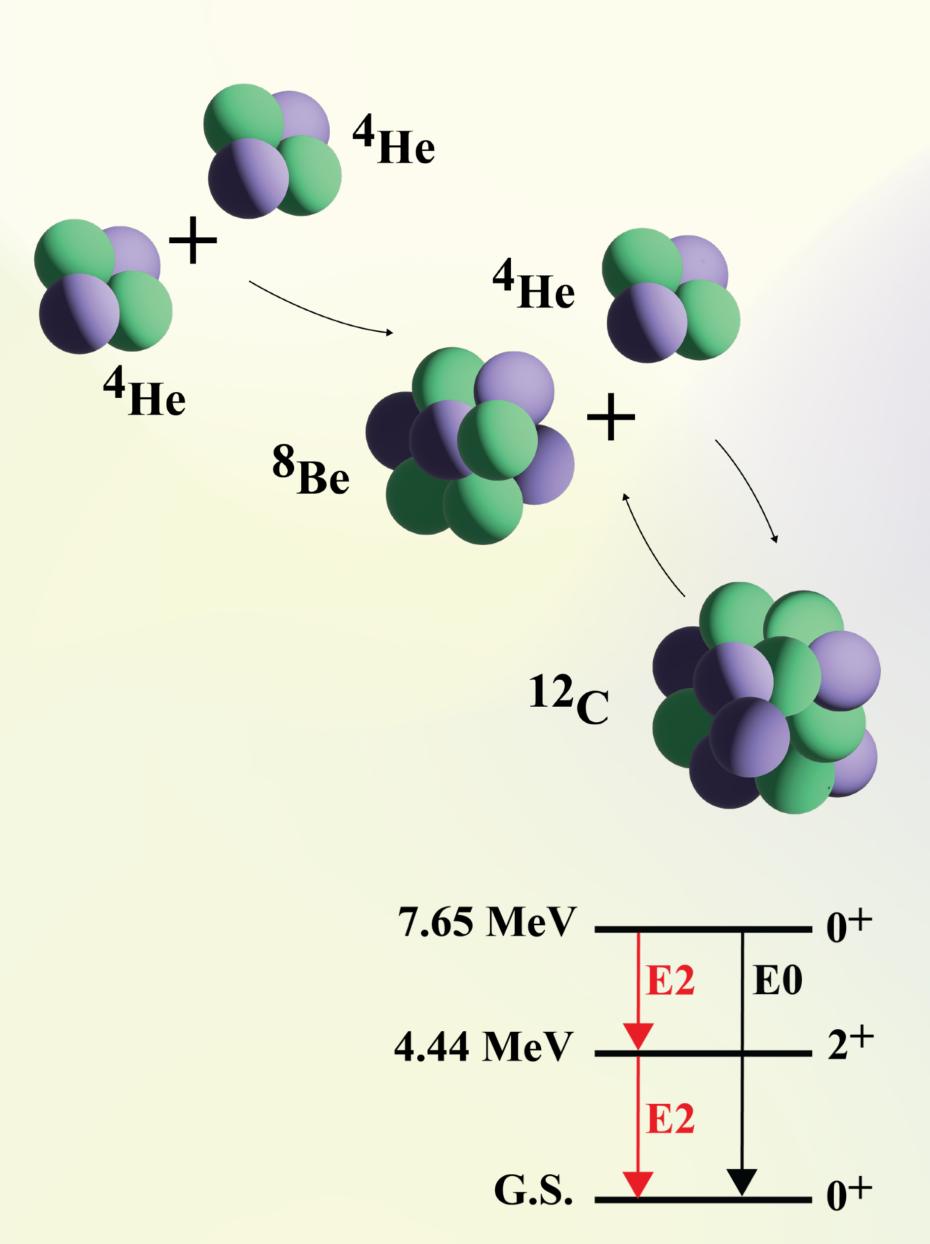






The radiative branching ratio can be measured directly by either measuring surviving ¹²C nuclei in the reaction, or by measuring the γ-decay branching ratio and the pair-decay branching ratio

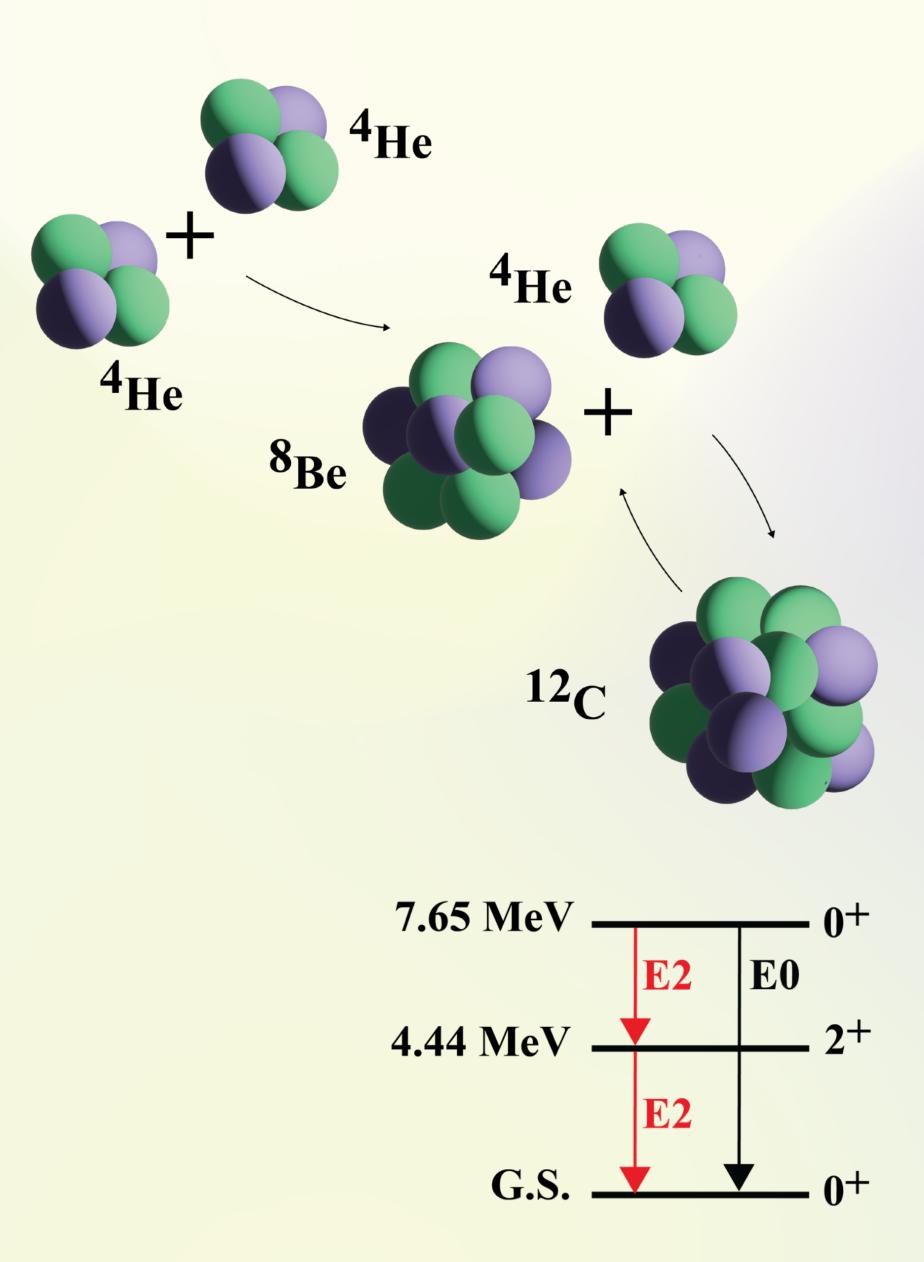
$$\Gamma_{
m rad} = \left[rac{\Gamma_{
m rad}}{\Gamma}
ight] imes \left[rac{\Gamma}{\Gamma_{\pi}^{
m E0}}
ight] imes \left[\Gamma_{\pi}^{
m E0}
ight]$$





The radiative branching ratio can be measured **directly** by either measuring **surviving** ¹²**C nuclei** in the reaction, or by measuring the γ-decay branching ratio

$$\Gamma_{
m rad} = egin{bmatrix} \Gamma_{
m rad} \ \hline \Gamma_{
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m rad} \ \hline \Gamma_{
m gal} \ \hline \Gamma \end{array} = egin{bmatrix} \Gamma_{
m rad} \ \hline \Gamma_{
m gal} \ \hline \Gamma \end{array}$$



Previous measurements of the radiative branching ratio of the Hoyle state

Surviving recoil 12C

Seeger (1963) Markham (1976)

Hall (1964) Tsukuba (2021)

Chamberlin (1974) Luo (2024)

Davids (1975) Dell'Aquila (2024)

Mak (1975) Rana (2024)

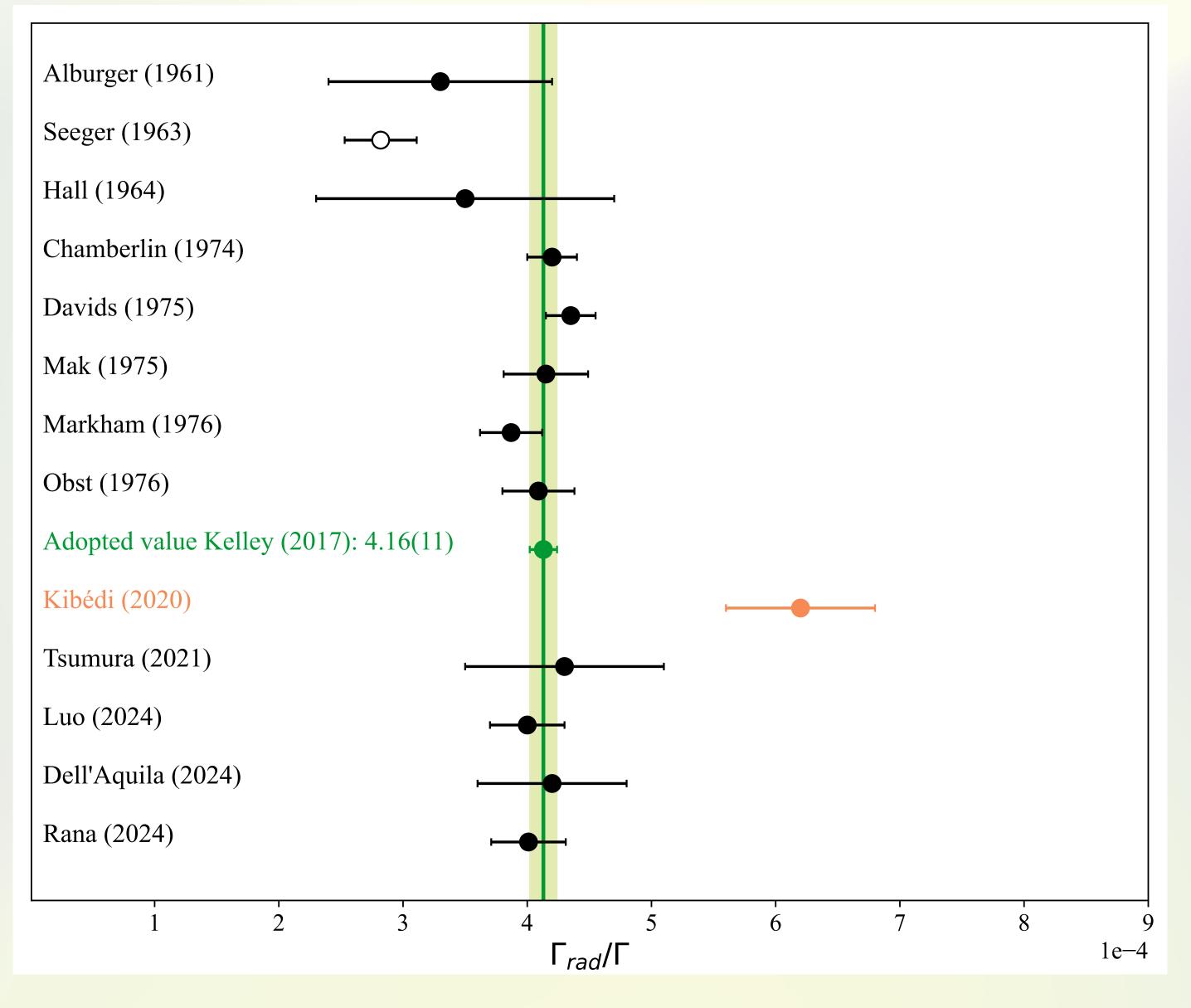
Combination of y-decay and pair-decay branching ratio

Alburger (1961)

Obst (1976) [9]

Kibédi (2020) [10]

Rana (2024)









Purpose: The main purpose was to perform a new measurement of the γ-decay branching ratio of the Hoyle state to deduce the radiative branching ratio of the Hoyle state. An additional objective was to independently verify aspects of the aforementioned measurement conducted by Kibédi *et al*. [Phys. Rev. Lett. 125, 182701 (2020)].

The purpose of this project

PHYSICAL REVIEW C 112, 015803 (2025)

Remeasuring the γ -decay branching ratio of the Hoyle state

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1 Department of Physics, University of Oslo, N-0316 Oslo, Norway

2 Norwegian Nuclear Research Centre, Oslo, Norway

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Background: The radiative branching ratio of the Hoyle state is crucial to estimate the triple- α reaction rate in stellar environments at medium temperatures of T=0.1 to 2 GK. Knowledge of the γ -decay channel is critical as this is the dominant radiative decay channel for the Hoyle state. A recent study by Kibédi *et al.* [Phys. Rev. Lett. 125, 182701 (2020)] has challenged our understanding of this astrophysically significant branching ratio and its constraints.

Purpose: The main purpose was to perform a new measurement of the γ -decay branching ratio of the Hoyle state to deduce the radiative branching ratio of the Hoyle state. An additional objective was to independently verify aspects of the aforementioned measurement conducted by Kibédi *et al.* [Phys. Rev. Lett. **125**, 182701 (2020)].

Method: For the primary experiment of this work the Hoyle state was populated by the 12 C(p, p') reaction at 10.8 MeV at the Oslo Cyclotron Laboratory. The γ -decay branching ratio was deduced through triple-coincidence events, each consisting of a proton-ejectile energy corresponding to population of the 0_2^+ Hoyle state, and the subsequent cascade of 3.21 and 4.44 MeV γ rays. To verify the analysis, a surrogate γ -ray cascade from the 0_2^+ state in 28 Si was also studied. Following the same methodology, an independent analysis of the 2014 data published by Kibédi *et al.* [Phys. Rev. Lett. **125**, 182701 (2020)] was carried out.

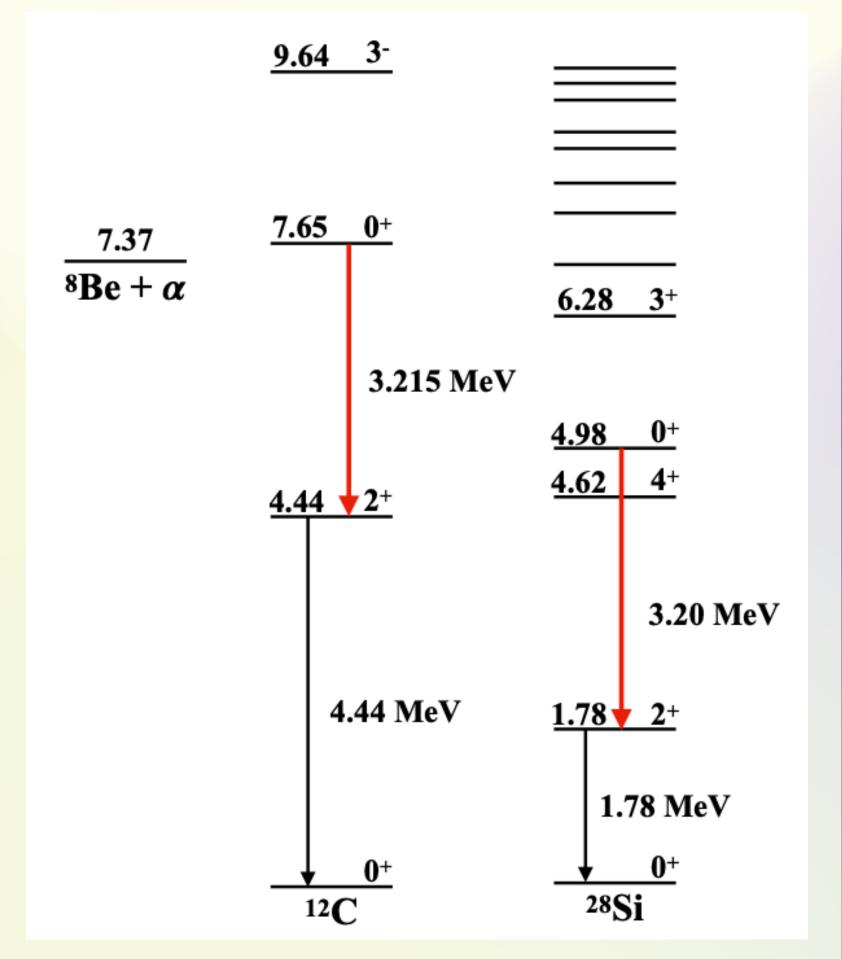
Results: From the main experiment of this work, a γ -decay branching ratio of the Hoyle state was determined as $\Gamma_{\gamma}^{7.65}/\Gamma^{7.65}=4.0(3)\times 10^{-4}$, yielding a radiative branching ratio of $\Gamma_{\rm rad}/\Gamma=4.1(4)\times 10^{-4}$. The independent reanalysis of the 2014 experiment published by Kibédi *et al.* [Phys. Rev. Lett. **125**, 182701 (2020)] in this work yielded $\Gamma_{\gamma}^{7.65}/\Gamma^{7.65}=4.5(6)\times 10^{-4}$, with a corresponding radiative branching ratio of $\Gamma_{\rm rad}/\Gamma=4.6(6)\times 10^{-4}$. **Conclusions:** The radiative branching ratio of the Hoyle state reported in this work is in excellent agreement with several recent studies, as well as the previously adopted ENSDF average of $\Gamma_{\rm rad}/\Gamma=4.16(11)\times 10^{-4}$. In this work, several issues were found in the analysis of Kibédi *et al.* [Phys. Rev. Lett. **125**, 182701 (2020)], with the corrected values no longer being discrepant with the ENSDF average.

How can we measure the γ -decay branching ratio of the Hoyle state?

Amount of particles populating the Hoyle state resulting in the desired gamma cascade 12 C(p, p' $\gamma_1\gamma_2$)

 $X \frac{\text{Correction}}{\text{factors}} = \Gamma \gamma / \Gamma$

Total amount of particles populating the Hoyle state 12 C(p, p' $\gamma_1\gamma_2$ + p' 3α + ...)





How can we measure the γ -decay branching ratio of the Hoyle state?

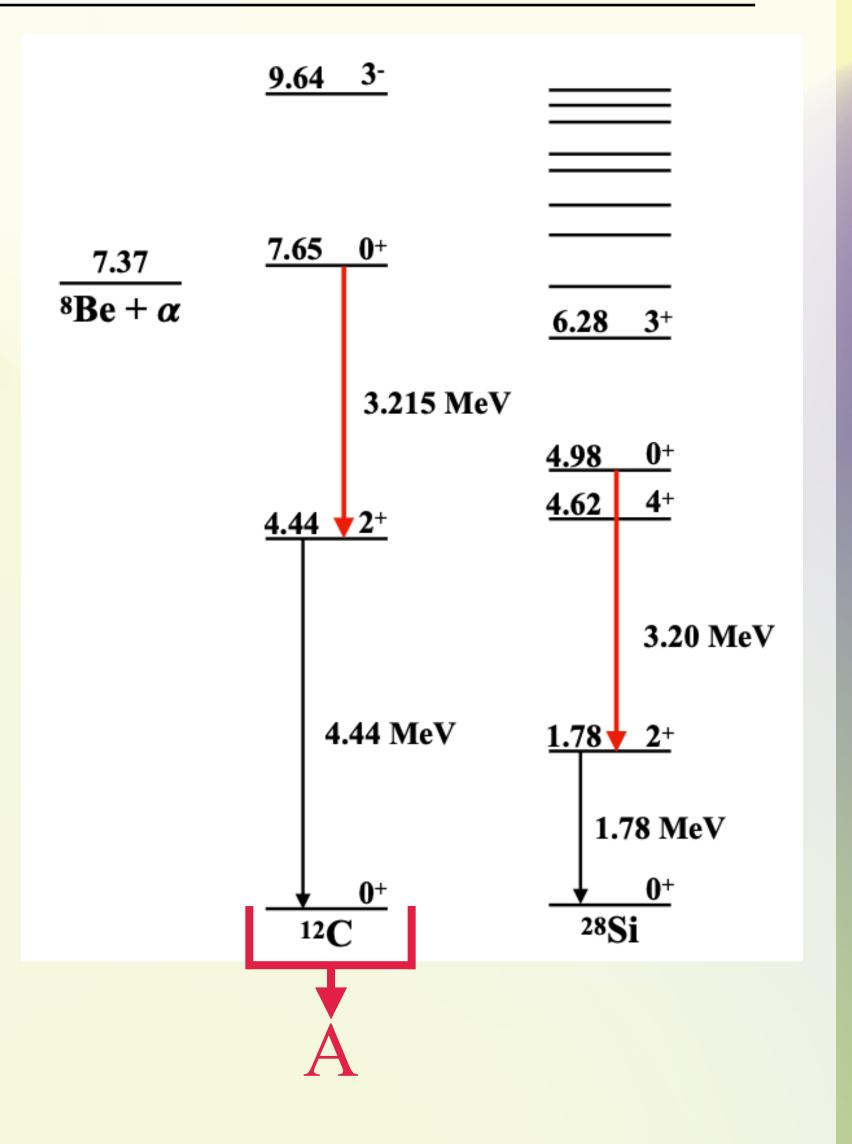
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Same measurement: Two different analysis methods to obtain Γ_{γ}/Γ

$$egin{array}{c} egin{array}{c} egin{array}{c} \Gamma_{\gamma}^{E2} \ \hline \Gamma^{7.65} \ \hline \Gamma^{7.65} \ \hline N_{
m inclusive}^{7.65} imes \epsilon_{3.21} imes \epsilon_{4.44} imes c_{
m det} imes W_{020}^{7.65} \end{array}$$





How can we measure the γ -decay branching ratio of the Hoyle state?

Amount of particles populating the Hoyle state resulting in the desired gamma cascade 12 C(p, p' $\gamma_1\gamma_2$)

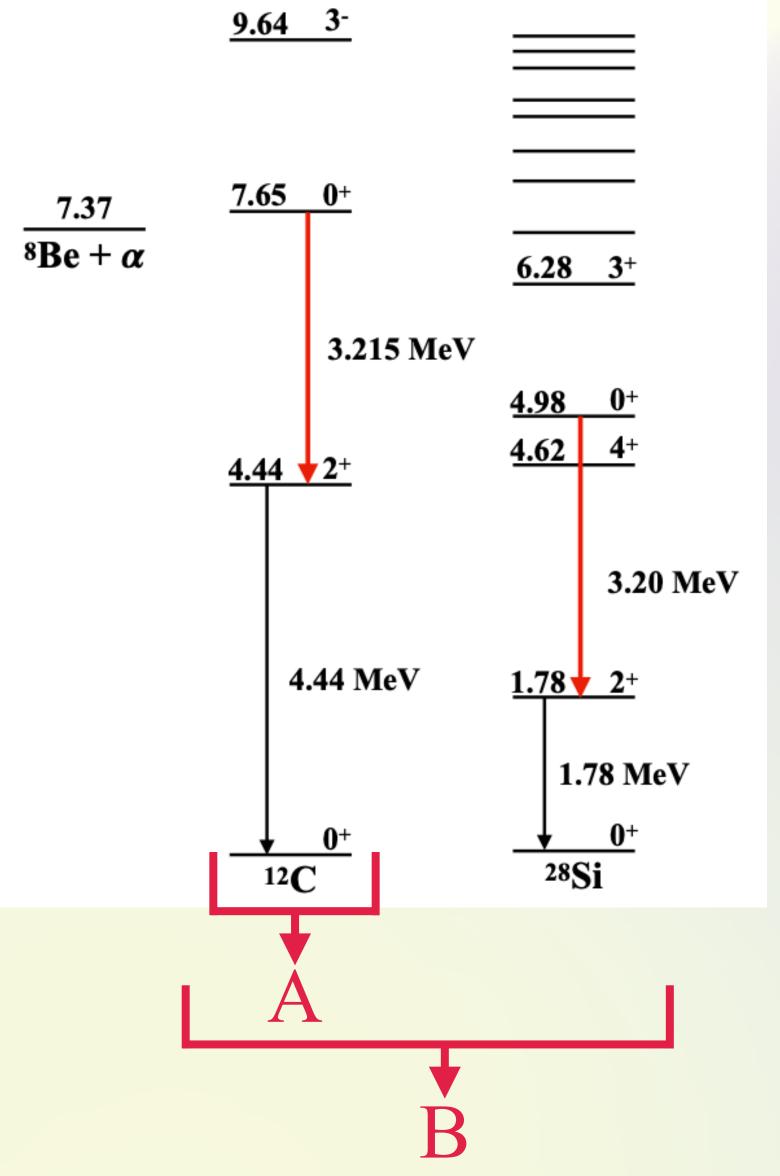
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m inclusive}^{7.65} imes \epsilon_{3.21} imes \epsilon_{4.44} imes c_{
m det} imes W_{020}^{7.65} \end{array}$$

$$\mathbf{B} \frac{\Gamma_{\gamma}^{7.65}}{\Gamma} = \frac{N_{020}^{7.65}}{N_{020}^{4.98}} \times \frac{N_{\text{inclusive}}^{4.98}}{N_{\text{inclusive}}^{7.65}} \times \frac{\epsilon_{1.78}}{\epsilon_{4.44}} \times \frac{\epsilon_{3.20}}{\epsilon_{3.21}} \times \frac{W_{020}^{4.98}}{W_{020}^{7.65}} \times \frac{c_{\text{det}}^{4.98}}{c_{\text{det}}^{7.65}}$$





Measurements in this work and analysis pipeline

2012 2012 $^{12}\text{C}(p, p')^{12}\text{C}$ $2_1^+ \text{ at E}_x = 4.44 \text{ MeV}$

> 28 Si $(p, p')^{28}$ Si 2_1^+ at $E_x = 1.78 \text{ MeV}$ 0_2^+ at $E_x = 4.98 \text{ MeV}$

 $^{12}\text{C}(p, p')^{12}\text{C}$ $2_1^+ \text{ at E}_x = 4.44 \text{ MeV}$ $0_2^+ \text{ at E}_x = 7.65 \text{ MeV}$

2014

 0_{2}^{+} at $E_{x} = 7.65 \text{ MeV}$

2019

 28 Si $(p, p')^{28}$ Si 2_1^+ at $E_x = 1.78 \text{ MeV}$ 0_2^+ at $E_x = 4.98 \text{ MeV}$ 3_1^+ at $E_x = 6.28 \text{ MeV}$

2014

 $^{12}\text{C}(p, p')^{12}\text{C}$ $2_1^+ \text{ at E}_x = 4.44 \text{ MeV}$

 $^{28}\text{Si}(p, p')^{28}\text{Si}$ $2_1^+ \text{ at } E_x = 1.78 \text{ MeV}$ $3_1^+ \text{ at } E_x = 6.28 \text{ MeV}$

2019

 $^{28}\text{Si}(p, p')^{28}\text{Si}$ $2_1^+ \text{ at E}_x = 1.78 \text{ MeV}$ 0_{2}^{+} at $E_{x} = 4.98 \text{ MeV}$

2020

2020

Energy and time calibration of particle detectors and γ -ray detectors. Extracting yields from particle spectra.

Determine measured and simulated absolute photopeak efficiencies. Determine measured gated efficiencies for both gating on individual γ rays and summed- γ rays. Generate γ - γ matrices and summed- γ matrices.

Extract triple-coincidence (p- γ - γ) yields.

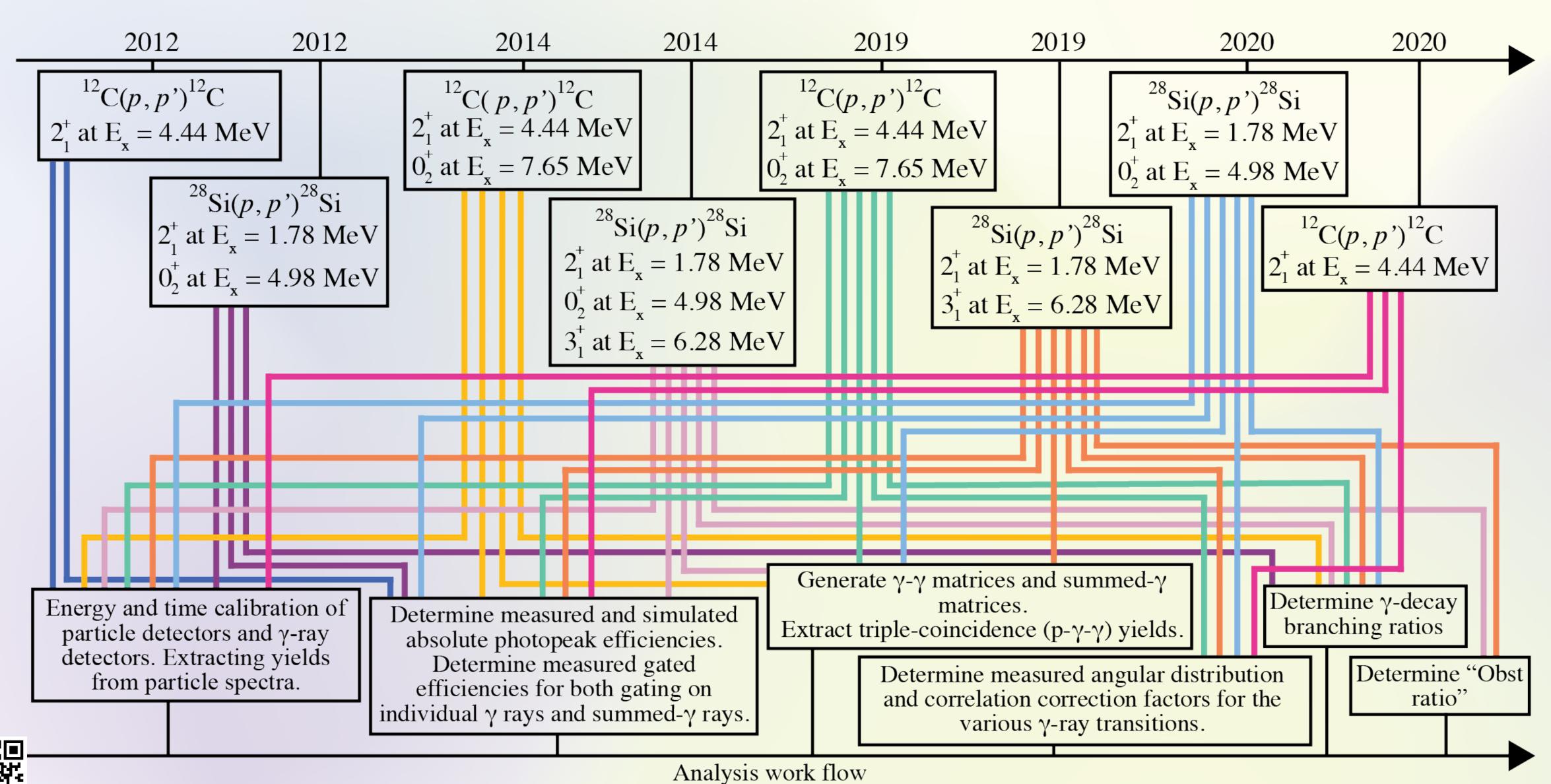
Determine measured angular distribution and correlation correction factors for the various γ -ray transitions.

Determine γ-decay branching ratios

> Determine "Obst ratio"



Measurements in this work and analysis pipeline





Experimental equipment

SiRi

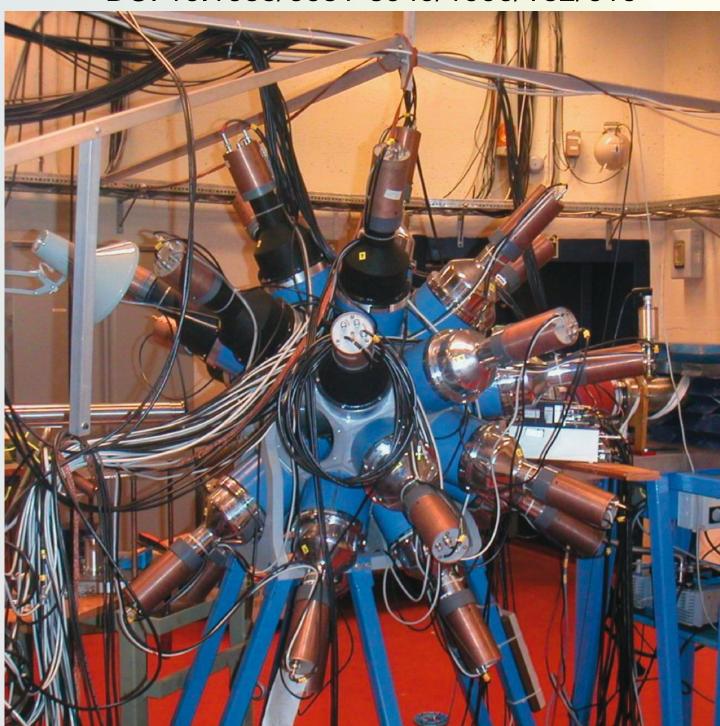
Guttormsen *et al.* (2011) [11] https://doi.org/10.1016/j.nima.2011.05.055



- Silicon Ring (SiRi) particle telescope
- Eight trapezoidal dE-E detectors
- Backwards position: theta = 126°-140°, 2° intervals
- Front position: theta = 40° - 54° , 2° intervals
- dE-detectors 130 μ m, E-detectors 1550 μ m

CACTUS

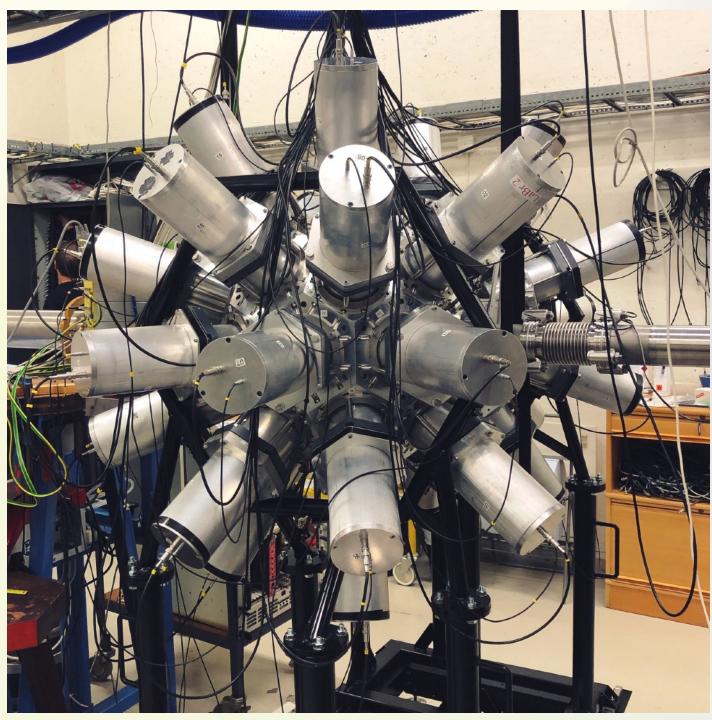
Guttormsen *et al.* (1990) [12] DOI 10.1088/0031-8949/1990/T32/010



- 26 NaI detectors (5" x 5")
- Collimated with 10 cm of lead
- Each detector subtending a solid angle of $\sim 0.63\%$ of 4π
- Total gamma-ray efficiency (1.3 MeV) ~ 14.1%
- Distance from target 22 cm

OSCAR

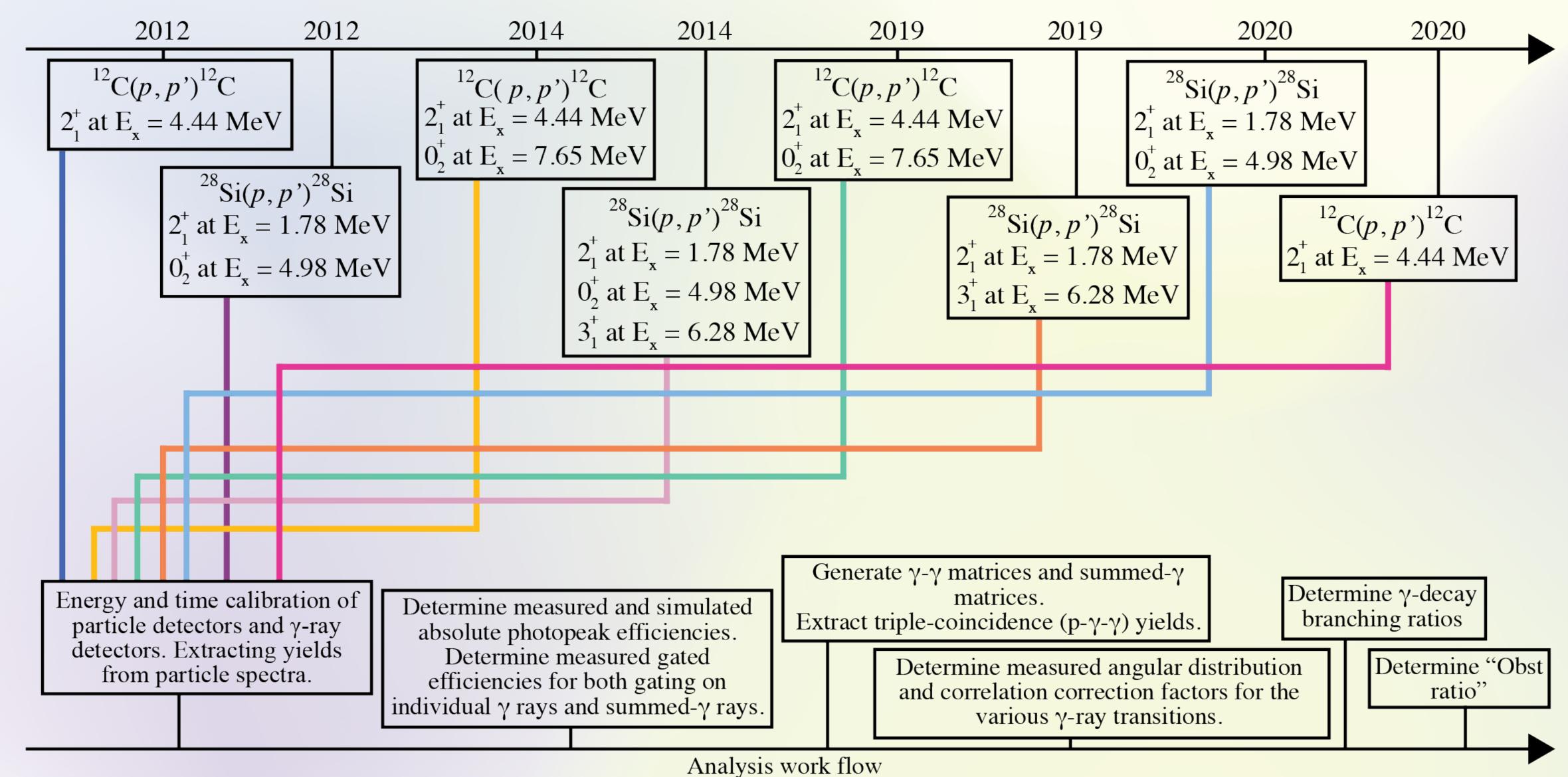
Zeiser *et al.* (2021) [13] https://doi.org/10.1016/j.nima.2020.164678



- 30 LaBr₃ detectors (3.5" x 8")
- No collimation
- Each detector subtending a solid angle of $\sim 1.9\%$ of 4π
- Total gamma-ray efficiency $(1.3 \text{ MeV}) \sim 56\%$
- Distance from target 16.3 cm

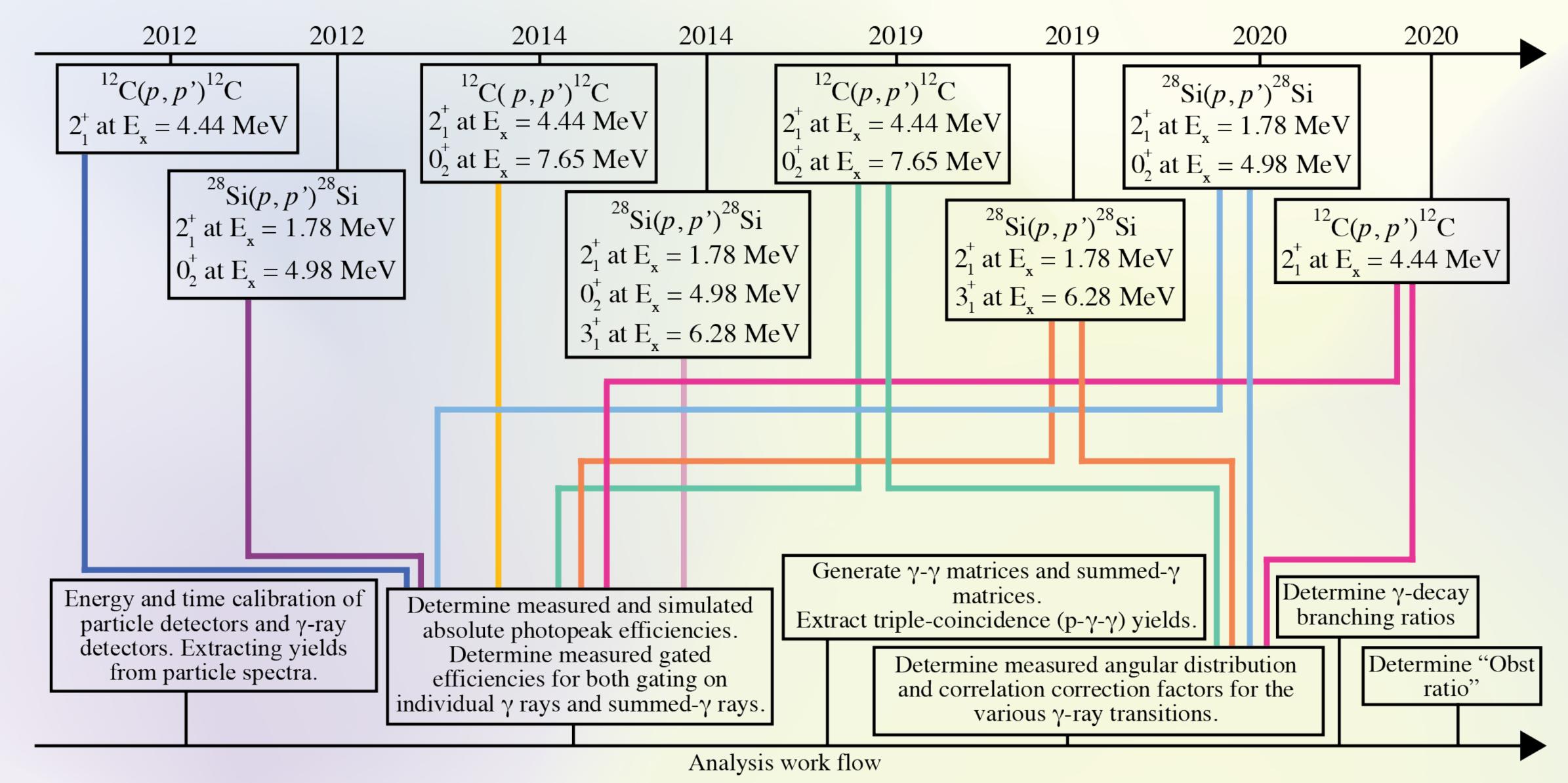


Measurements in this work and analysis pipeline



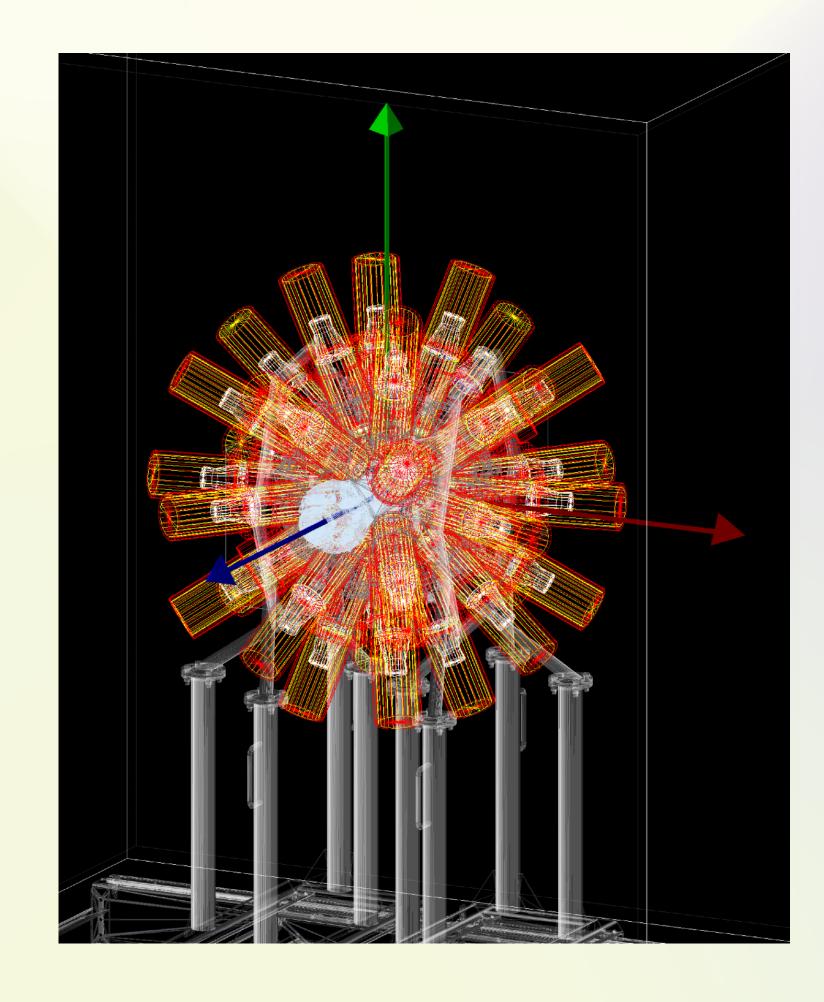


Measurements in this work and analysis pipeline





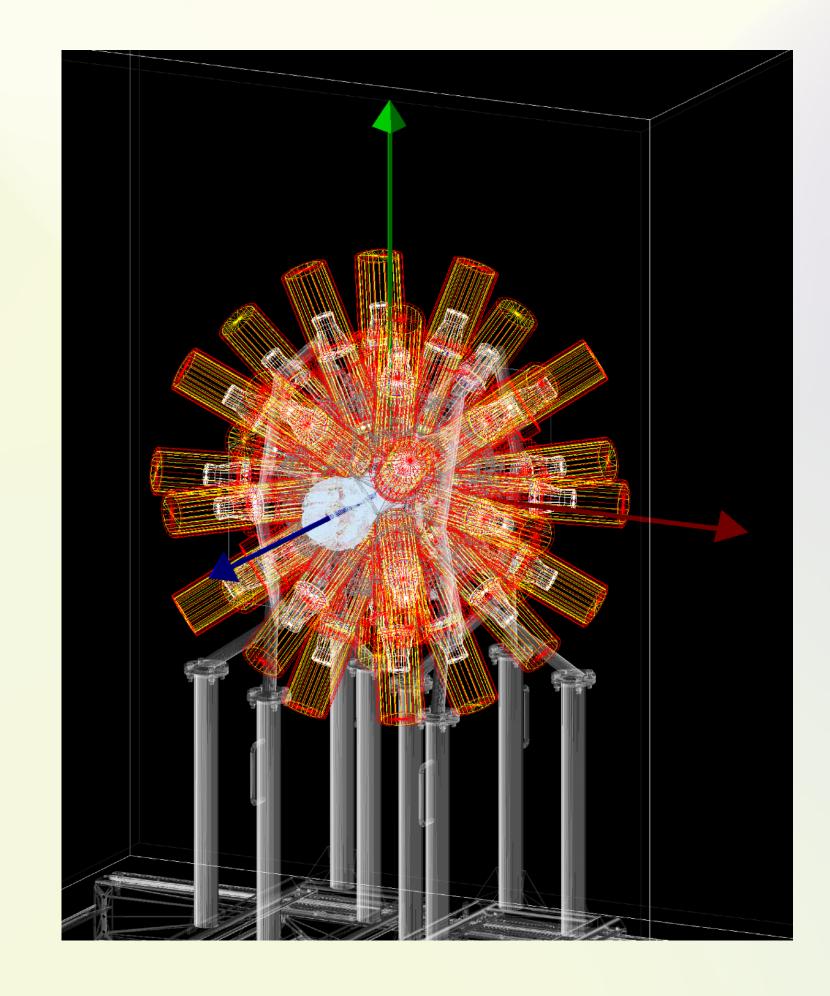
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• We also measured in-beam efficiencies for several transitions to confirm our simulation results, however all results are extracted using experimental efficiencies.

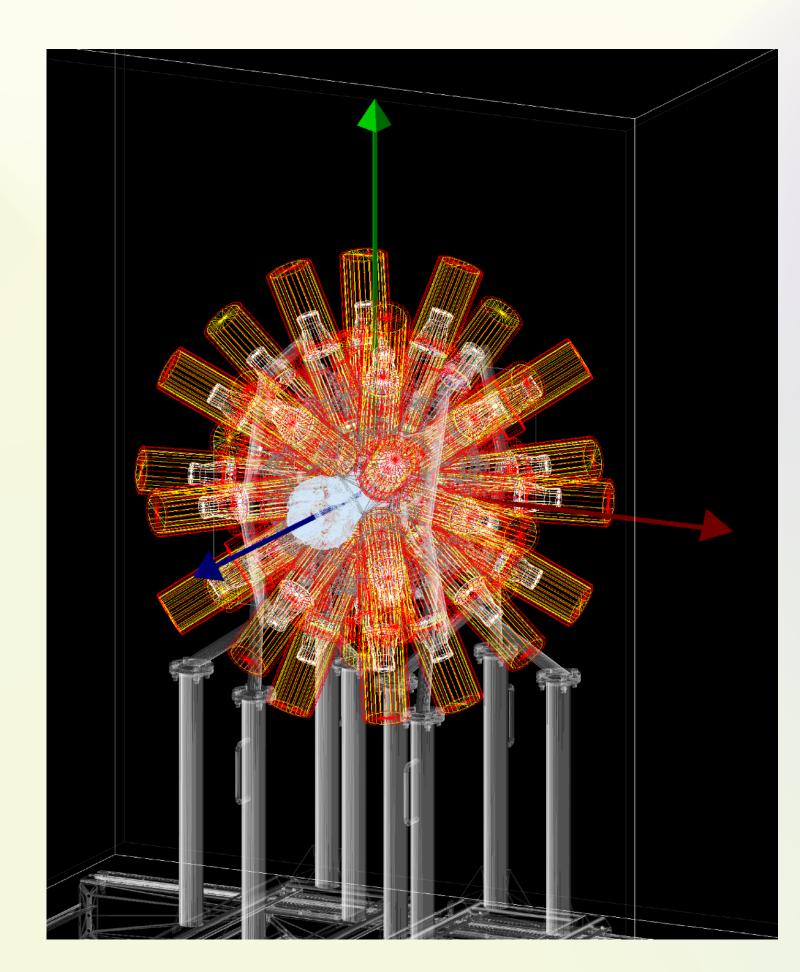




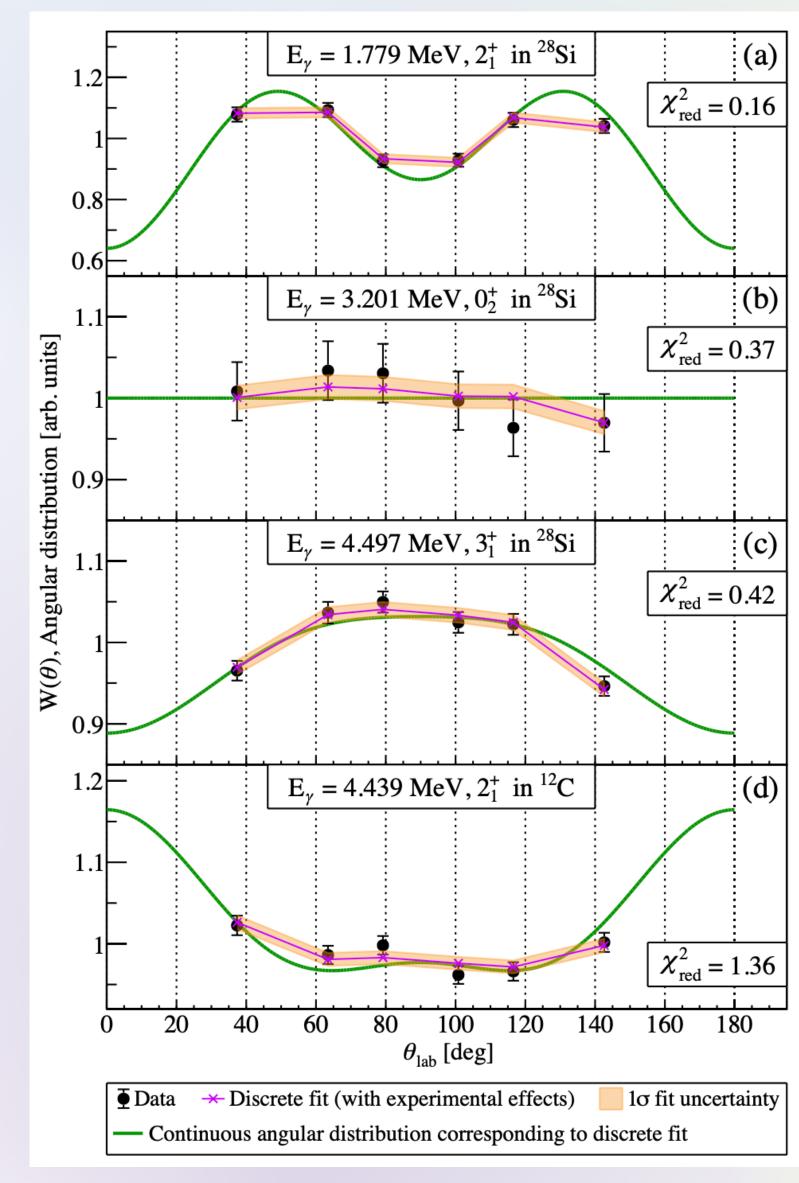
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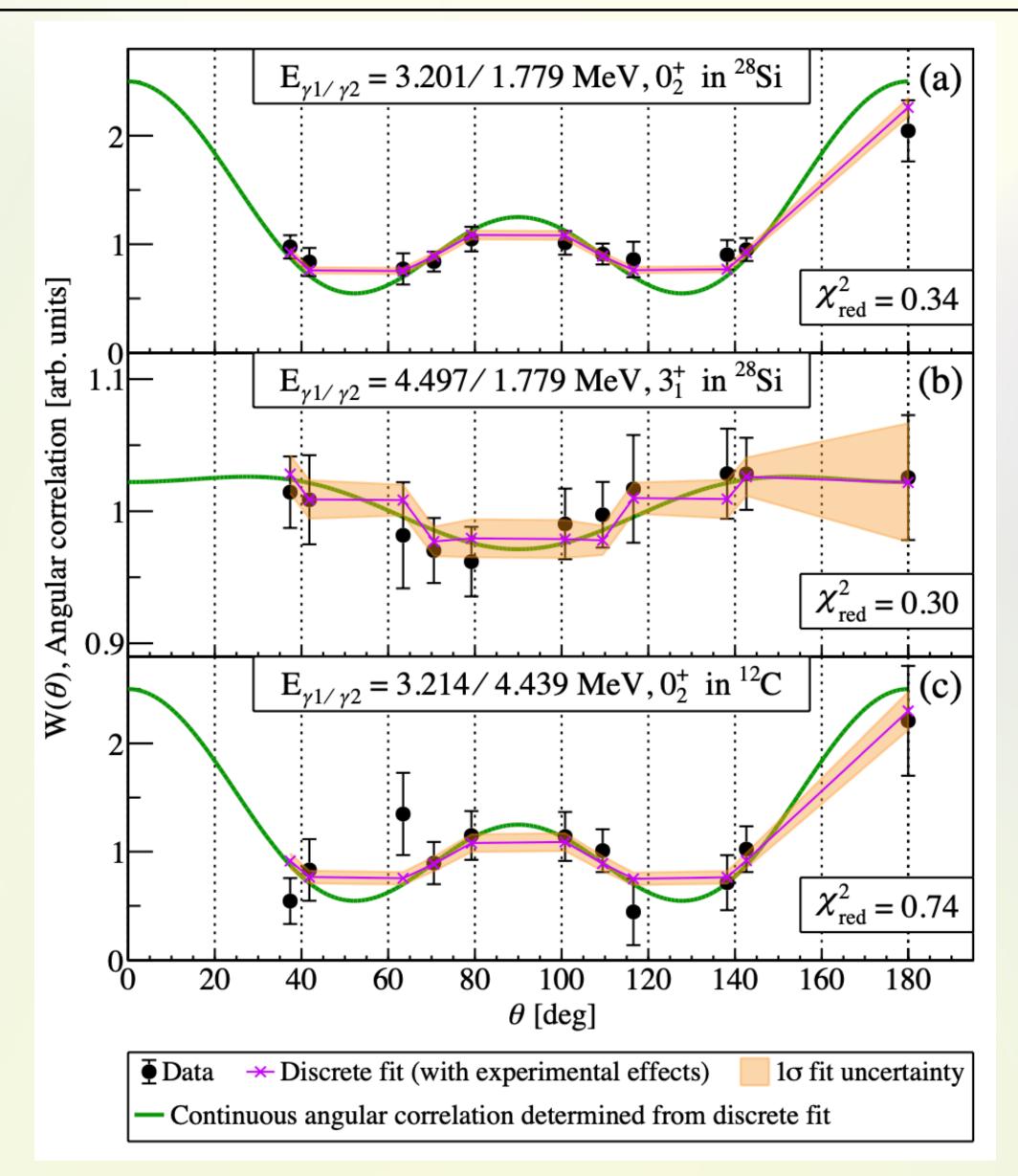
• We also measured in-beam efficiencies for several transitions to confirm our simulation results, however all results are extracted using experimental efficiencies.

• Simulation accounts for ± 1 mm distance uncertainty for the OSCAR detectors, beam energy differences, corrections from measuring cascading gammas and finite-solid effects of the LaBr3-detectors of OSCAR.











- For the CACTUS array we do not have a full GEANT4 simulation available.
- For results of 2012 and 2014 measurements, no correction to the distance uncertainty for the detectors, beam energy differences, corrections from measuring cascading gammas and finite-solid effects of the NaI(Ti)-detectors of CACTUS.
- A 3% systematic uncertainty was added to all efficiencies to account for the missing corrections.
- Angular correlation correction factor W_{020} from Kibédi et al. (2020) was used for all measurements using CACTUS.

	$^{12}\mathrm{C}(p,p')$ / $^{28}\mathrm{Si}(p,p')$ with $E_p=16.0~\mathrm{MeV}$ performed in 2012	$^{12}{\rm C}(p,p') \ / \ ^{28}{\rm Si}(p,p') \ { m with} \ E_p = 10.7 \ { m MeV}$ performed in 2014 [16]
$\epsilon_{1.78}$ (data, fitted) $\epsilon_{1.78}$ (data, gated)	$0.0024(2) \\ 0.0024(1)$	$0.0028(1)^{a} \ 0.0031(1)^{a}$
$\epsilon_{3.20}$ (data, fitted)	0.00168(8)	0.00169(6)
$\epsilon_{4.44}$ (data, fitted) $\epsilon_{4.44}$ (data, gated)	$0.00136(4) \\ 0.00173(5)$	$0.00143(4) \\ 0.00172(5)$
$\epsilon_{4.49}$ (data, fitted)		0.00152(9)
$\epsilon_{1.78}\epsilon_{3.20}c_{ m det} \; ({ m data, gated}) \ \epsilon_{1.78}\epsilon_{3.20}c_{ m det} \; ({ m generated, gated})$	$0.0022(1) \\ 0.0023(1)$	$0.0035(2) \\ 0.0032(2)$
$\epsilon_{1.78}\epsilon_{4.49}c_{ m det} \; ({ m data, gated}) \ \epsilon_{1.78}\epsilon_{4.49}c_{ m det} \; ({ m generated, gated})$		$0.0030(2) \\ 0.0034(2)$
$\epsilon_{3.20}\epsilon_{4.44}c_{\mathrm{det}}$ (generated, gated)		0.0025(2)

<sup>7.65 0+

6.28 3+

3.215</sup> MeV

4.44 V2+

4.44 MeV

1.78 V 2+

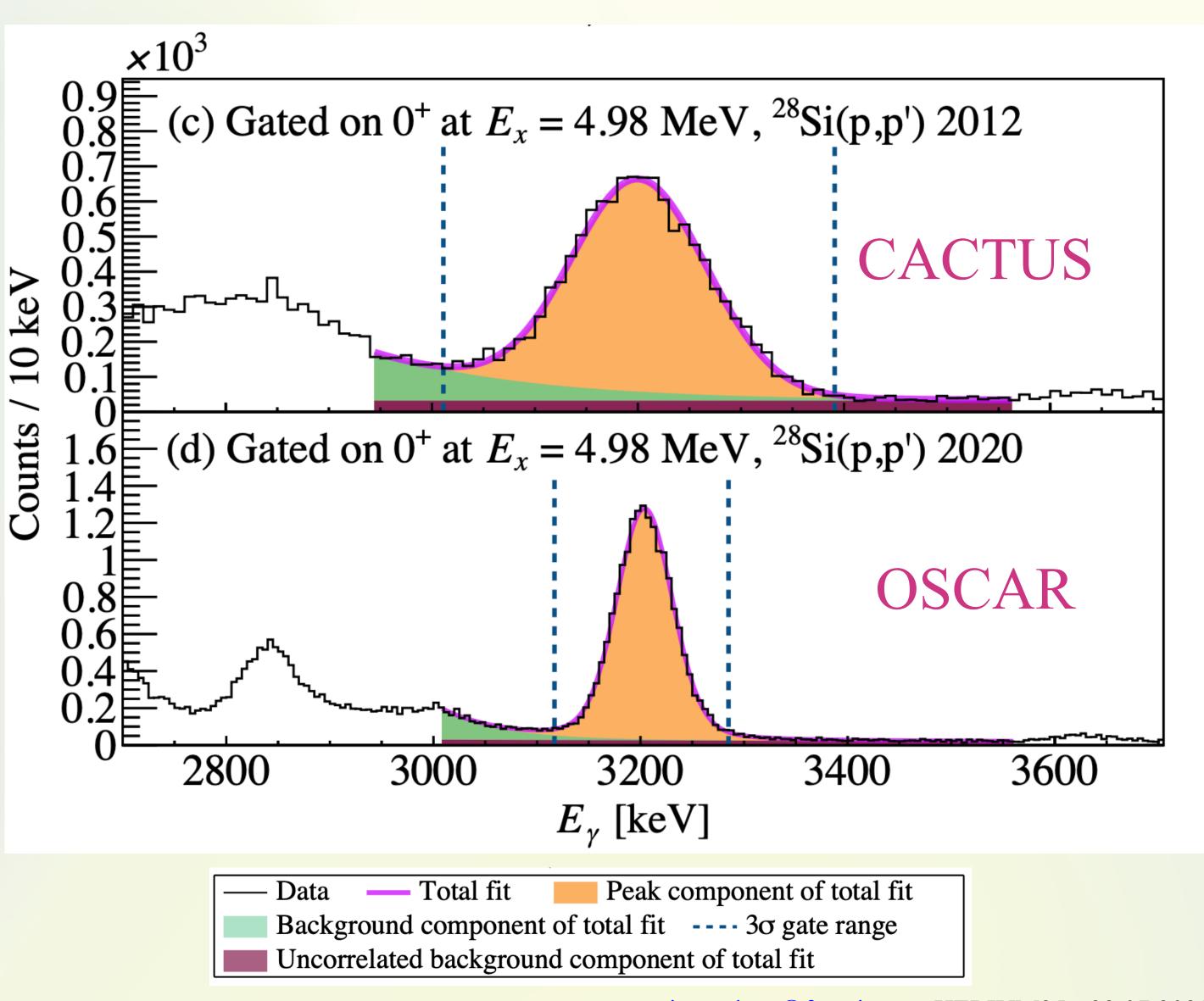
1.78 MeV

1.78 MeV

28Si



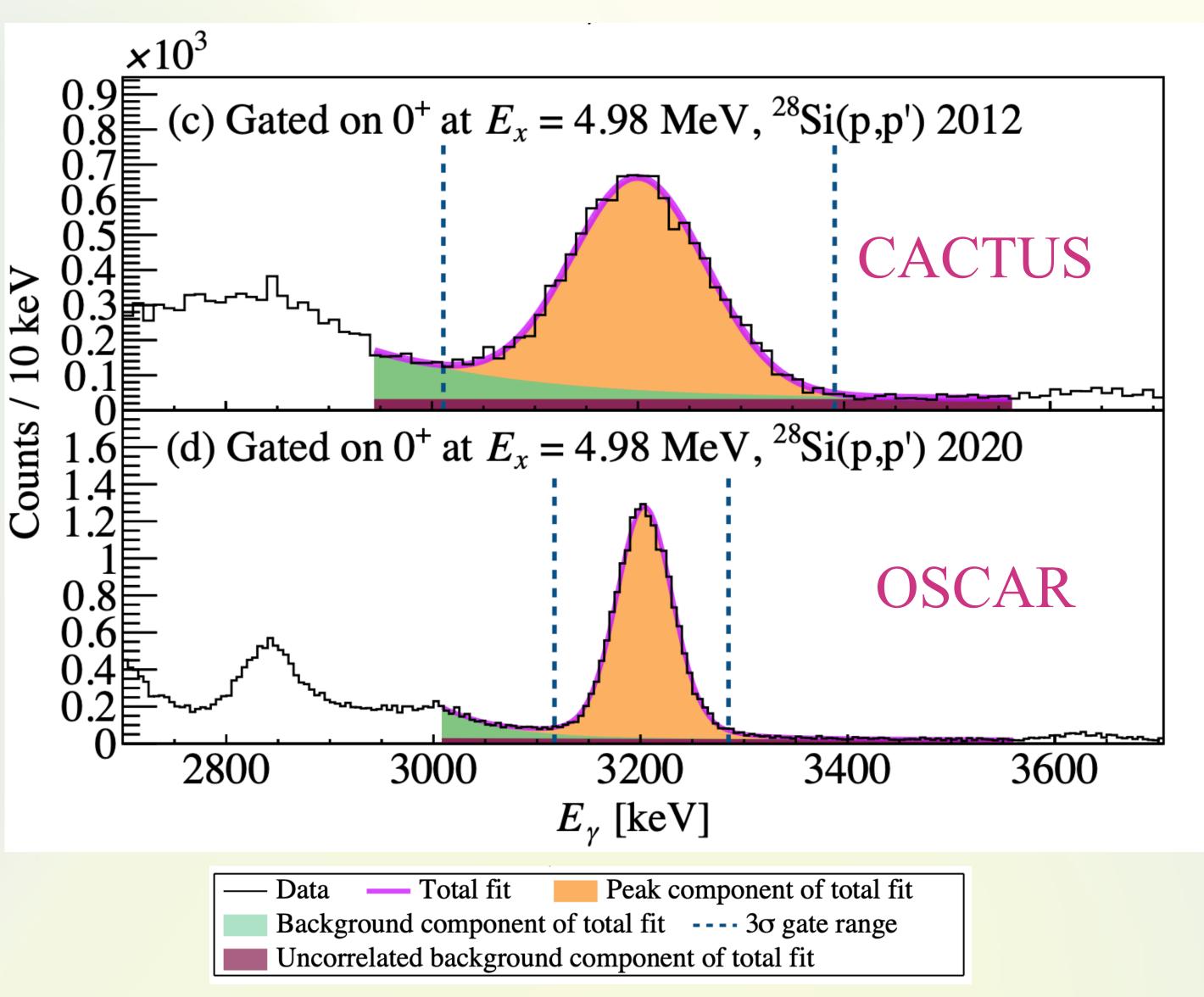
When extracting the γ -decay branching ratio using **triple coincidences**, the γ ray being gated on **must** be defined as a **gated efficiency**, and not as **absolute photopeak efficiency**.





When extracting the γ -decay branching ratio using **triple coincidences**, the γ ray being gated on **must** be defined as a **gated efficiency**, and not as **absolute photopeak efficiency**.

$$rac{\Gamma_{\gamma}^{E2}}{\Gamma^{7.65}} = rac{N_{020}^{7.65}}{N_{
m inclusive}^{7.65} imes \epsilon_{3.21}} imes \epsilon_{4.44} imes c_{
m det} imes W_{020}^{7.65}$$

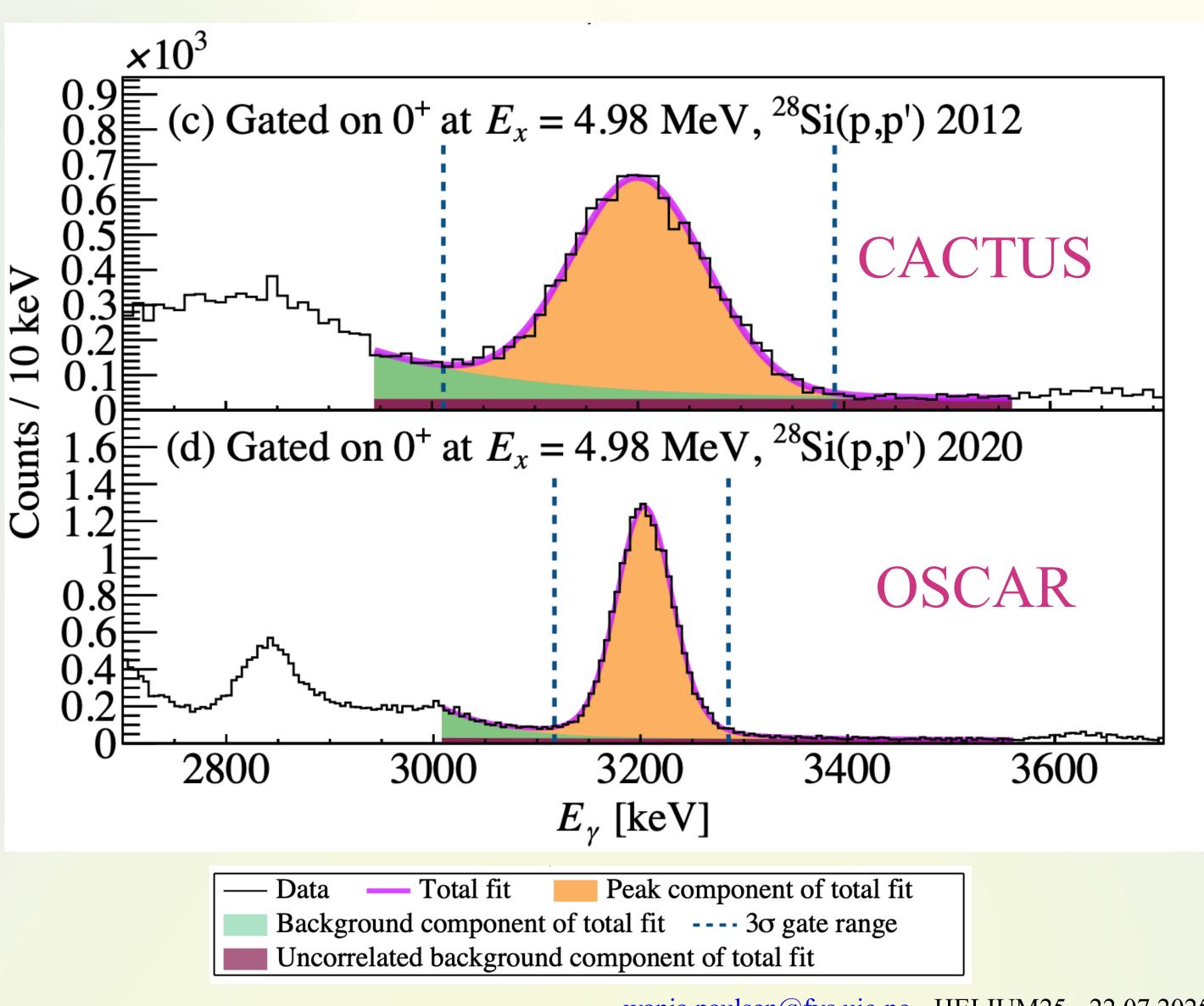




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m inclusive}^{7.65} imes \epsilon_{3.21} imes \epsilon_{4.44} imes c_{
m det} imes W_{020}^{7.65}}$$

Depending on the **resolution** of the detectors, events within the gate might fall **outside** the **absolute photopeak**, but will still yield valid **triple coincidences**: These events **must** be accounted for.

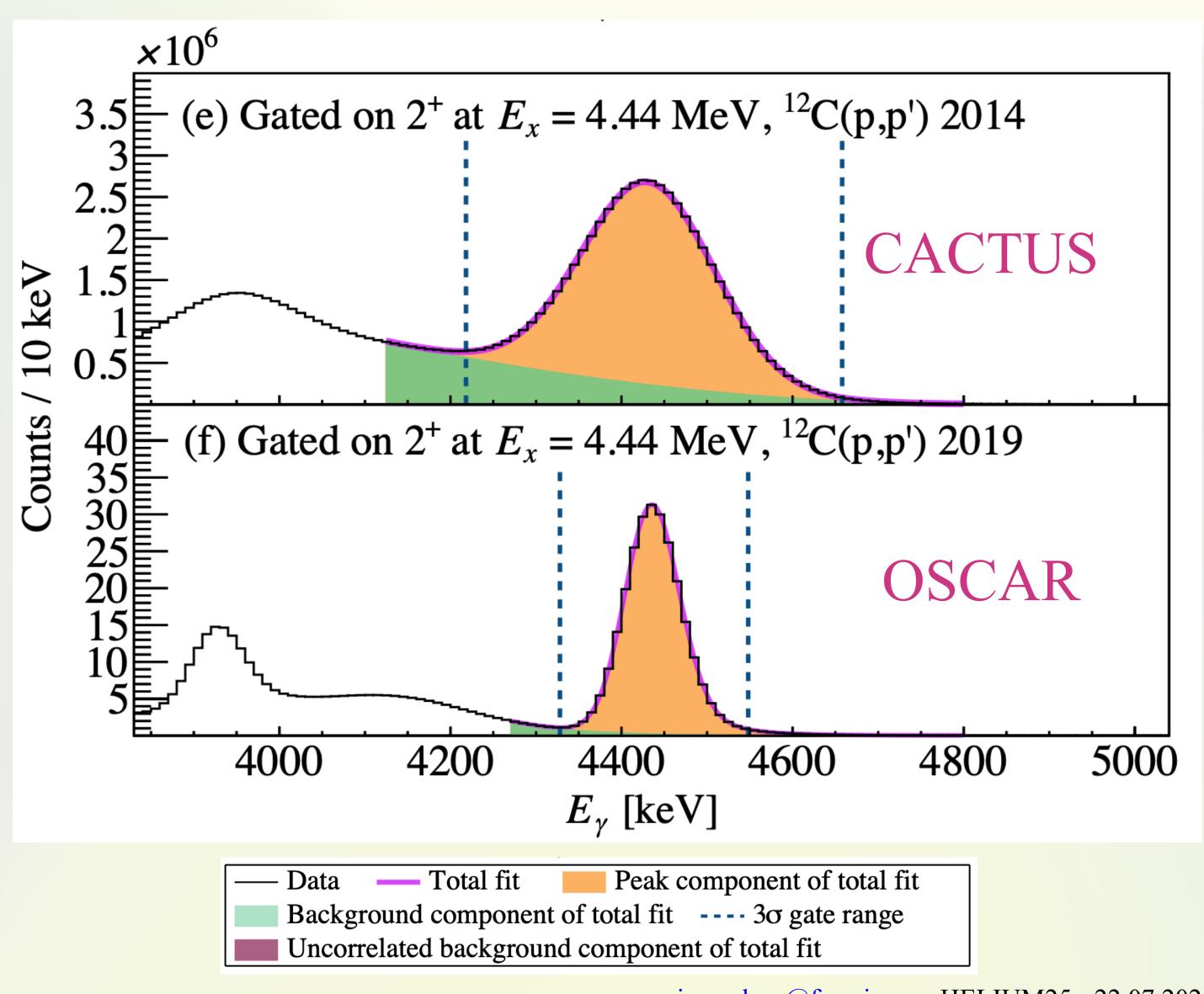




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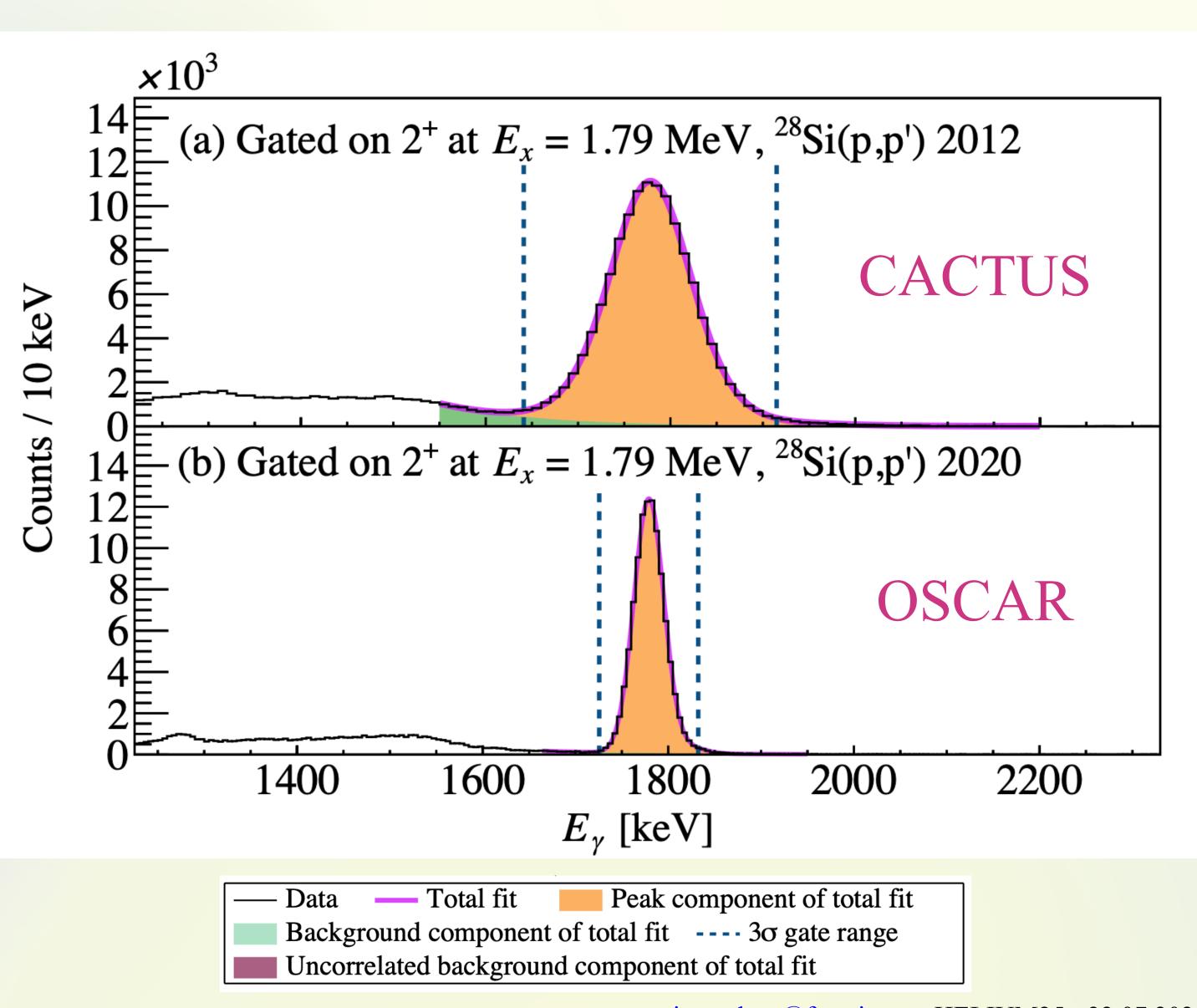
Depending on the **resolution** of the detectors, events within the gate might fall **outside** the **absolute photopeak**, but will still yield valid **triple coincidences**: These events **must** be accounted for.





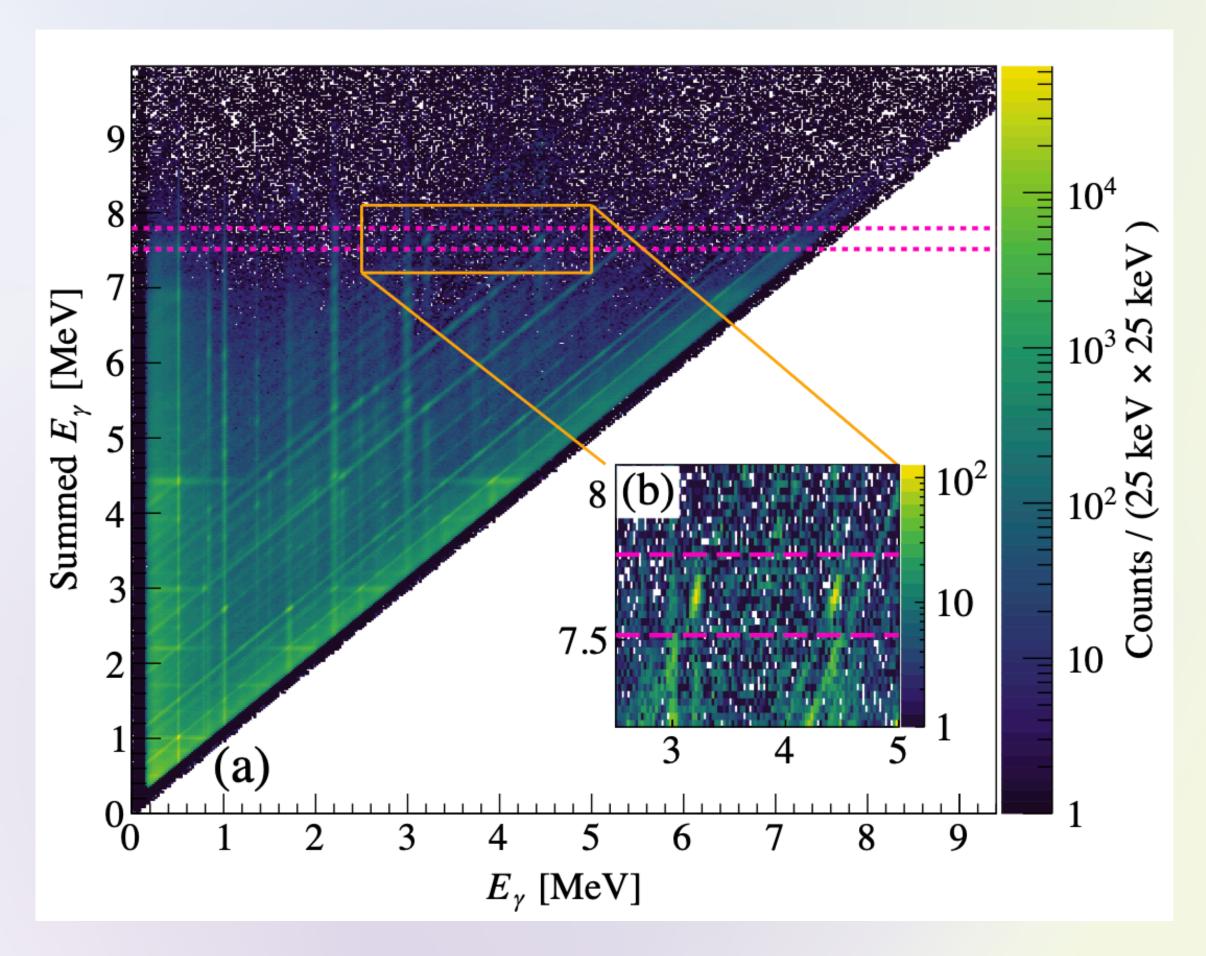
Since this effect is **energy dependent**, validating with the 0+→2+→0+ cascade in ²⁸Si will yield results consistent with **literature value** even **without** taking this effect into account.

$$rac{\Gamma_{\gamma}^{E2}}{\Gamma^{4.98}} = rac{N_{020}^{4.98}}{N_{
m inclusive}^{4.98} imes \epsilon_{1.78}} imes \epsilon_{3.20} imes c_{
m det} imes W_{020}^{4.98} = 1.0$$





Summed- γ matrix for 12 C(p, p') 2019

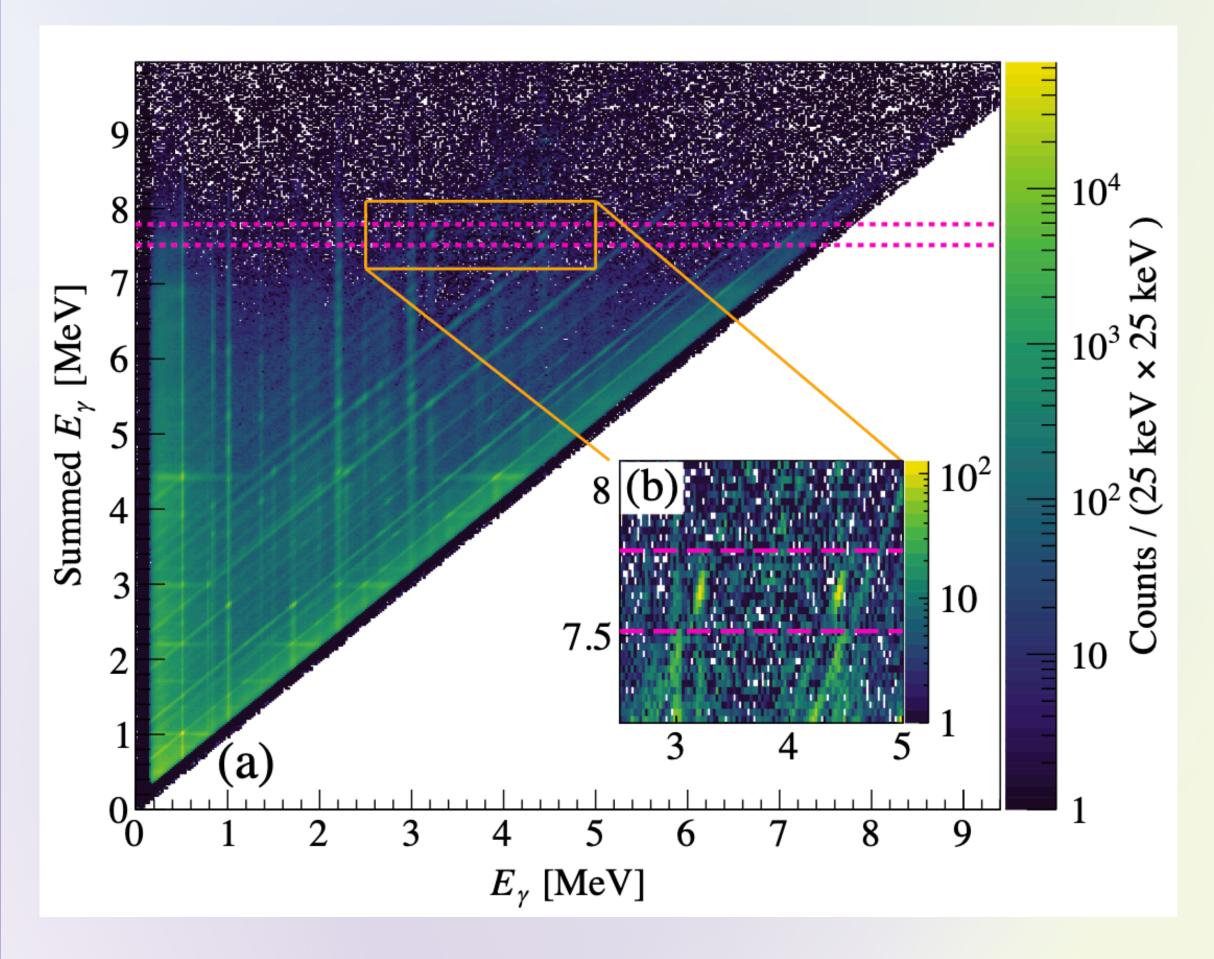


This is not the efficiency of a single γ ray, it is the efficiency of the convolution of two γ rays of different energies.

$$rac{\Gamma_{\gamma}^{E2}}{\Gamma^{7.65}} = rac{N_{020}^{7.65}}{N_{
m inclusive}^{7.65} imes \epsilon_{3.21} imes \epsilon_{4.44} imes c_{
m det}} imes W_{020}^{7.65}$$



Summed- γ matrix for 12 C(p, p') 2019

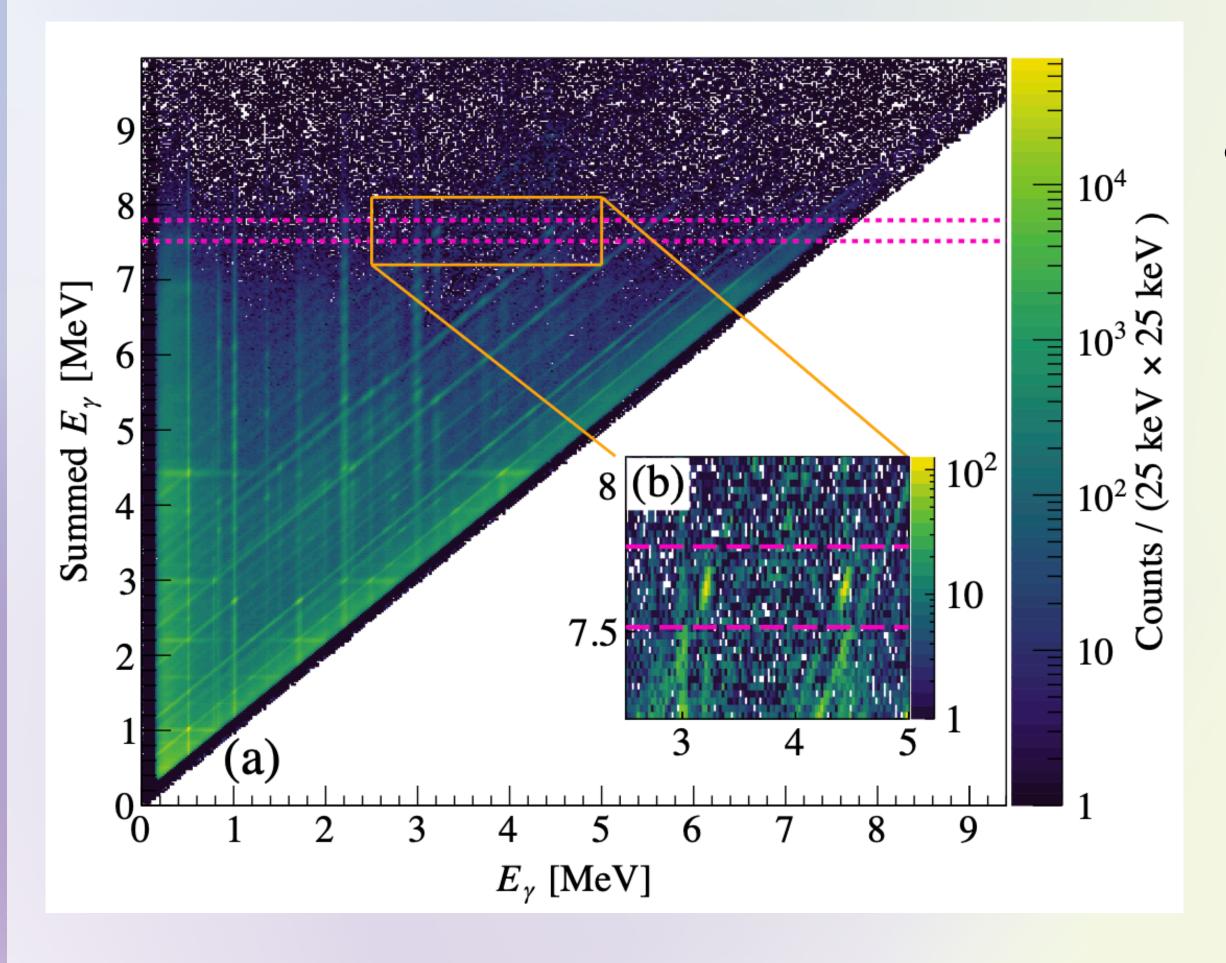


- This is not the efficiency of a single γ ray, it is the efficiency of the convolution of two γ rays of different energies.
- Not only do you need to have the response of this convolution of γ rays, you also need to extract the triple-coincidence yield from a non-trivial peak shape, originating from performing a gate on the sum.

$$rac{\Gamma_{\gamma}^{E2}}{\Gamma^{7.65}} = rac{N_{020}^{7.65}}{N_{
m inclusive}^{7.65} imes \epsilon_{3.21} imes \epsilon_{4.44} imes c_{
m det}} imes W_{020}^{7.65}$$



Summed- γ matrix for 12 C(p, p') 2019

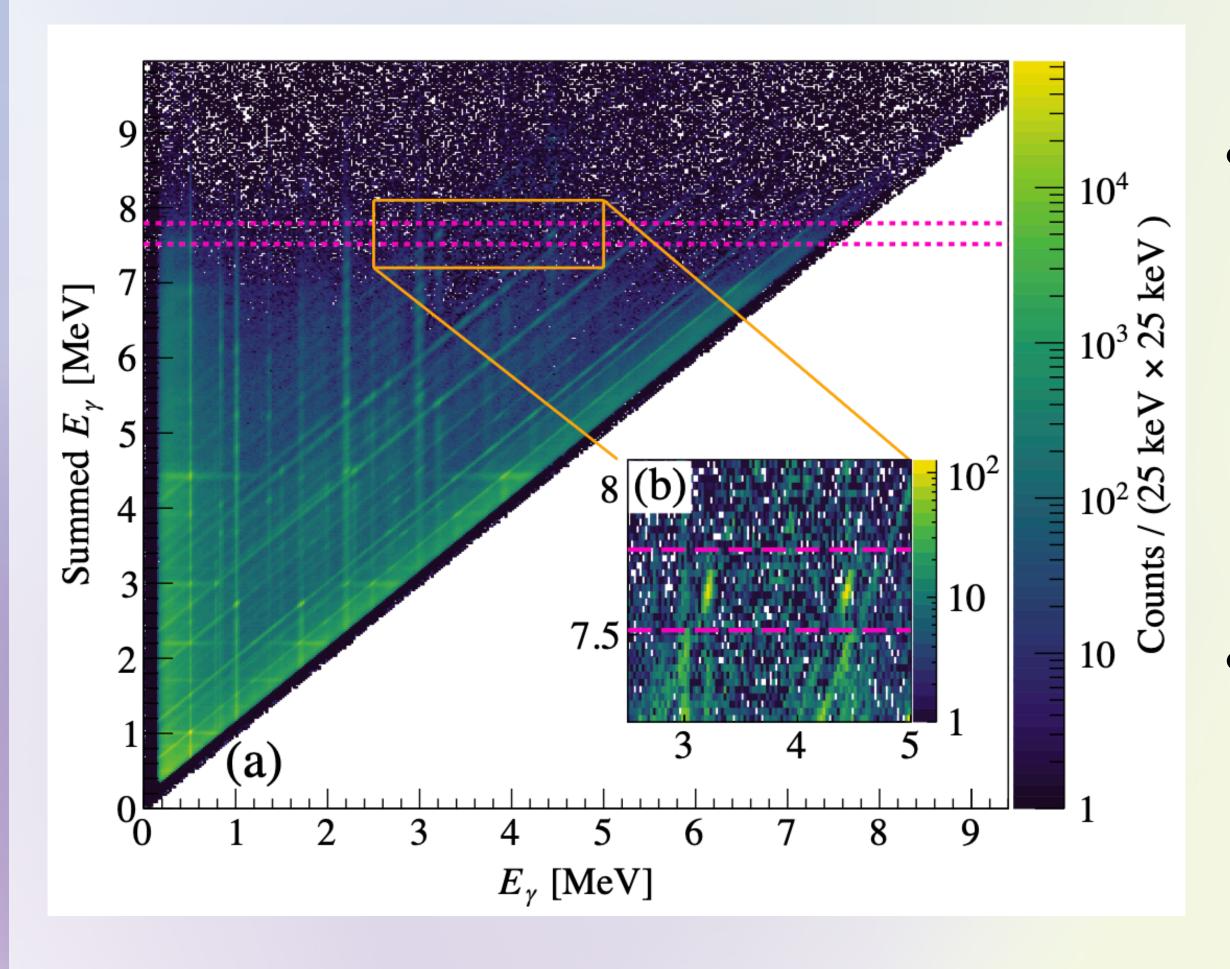


- This is not the efficiency of a single γ ray, it is the efficiency of the convolution of two γ rays of different energies.
- Not only do you need to have the response of this convolution of γ rays, you also need to extract the triple-coincidence yield from a non-trivial peak shape, originating from performing a gate on the sum.
- How do you get the experimental response when your cascade is very weakly populated?

$$rac{\Gamma_{\gamma}^{E2}}{\Gamma^{7.65}} = rac{N_{020}^{7.65}}{N_{
m inclusive}^{7.65} imes \epsilon_{3.21} imes \epsilon_{4.44} imes c_{
m det}} imes W_{020}^{7.65}$$



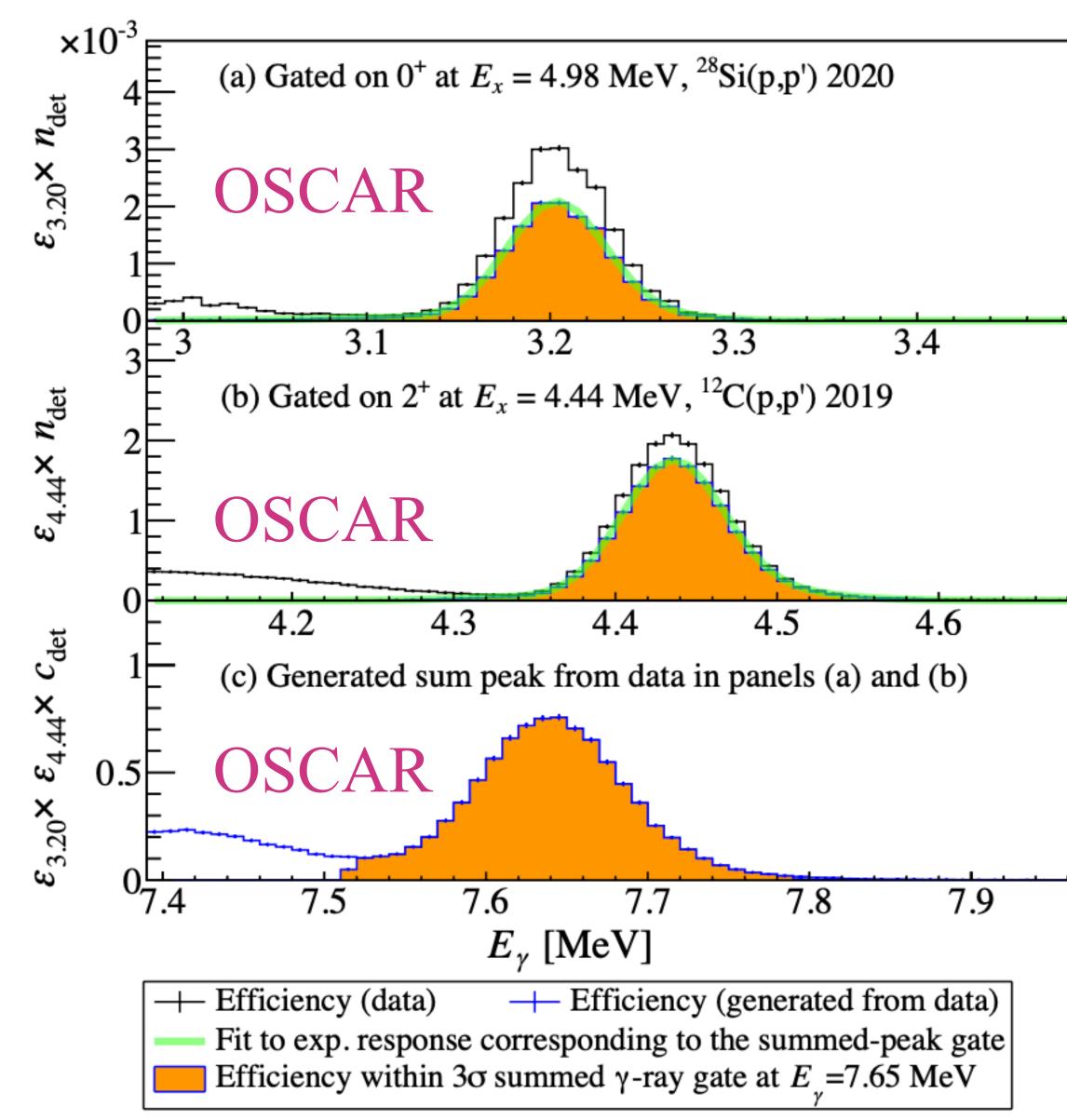
Summed- γ matrix for 12 C(p, p') 2019

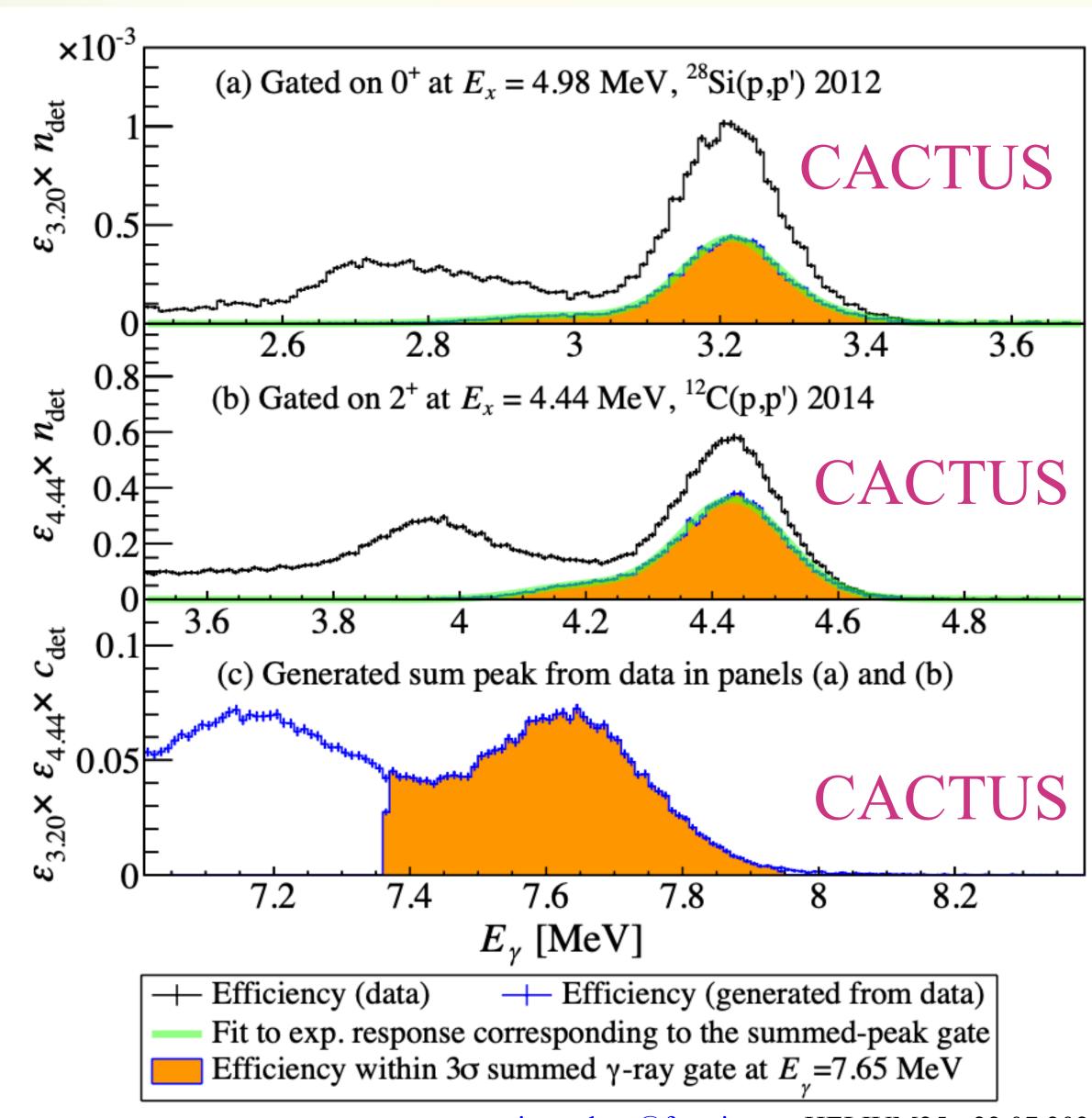


- This is not the efficiency of a single γ ray, it is the efficiency of the convolution of two γ rays of different energies.
- Not only do you need to have the response of this convolution of γ rays, you also need to extract the triple-coincidence yield from a non-trivial peak shape, originating from performing a gate on the sum.
- How do you get the experimental response when your cascade is very weakly populated?
- We used the individual transitions as **probability distributions** and **generated/sampled** our convolved summed-γ efficiency

$$rac{\Gamma_{\gamma}^{E2}}{\Gamma^{7.65}} = rac{N_{020}^{7.65}}{N_{
m inclusive}^{7.65} imes \epsilon_{3.21} imes \epsilon_{4.44} imes c_{
m det}} imes W_{020}^{7.65}$$

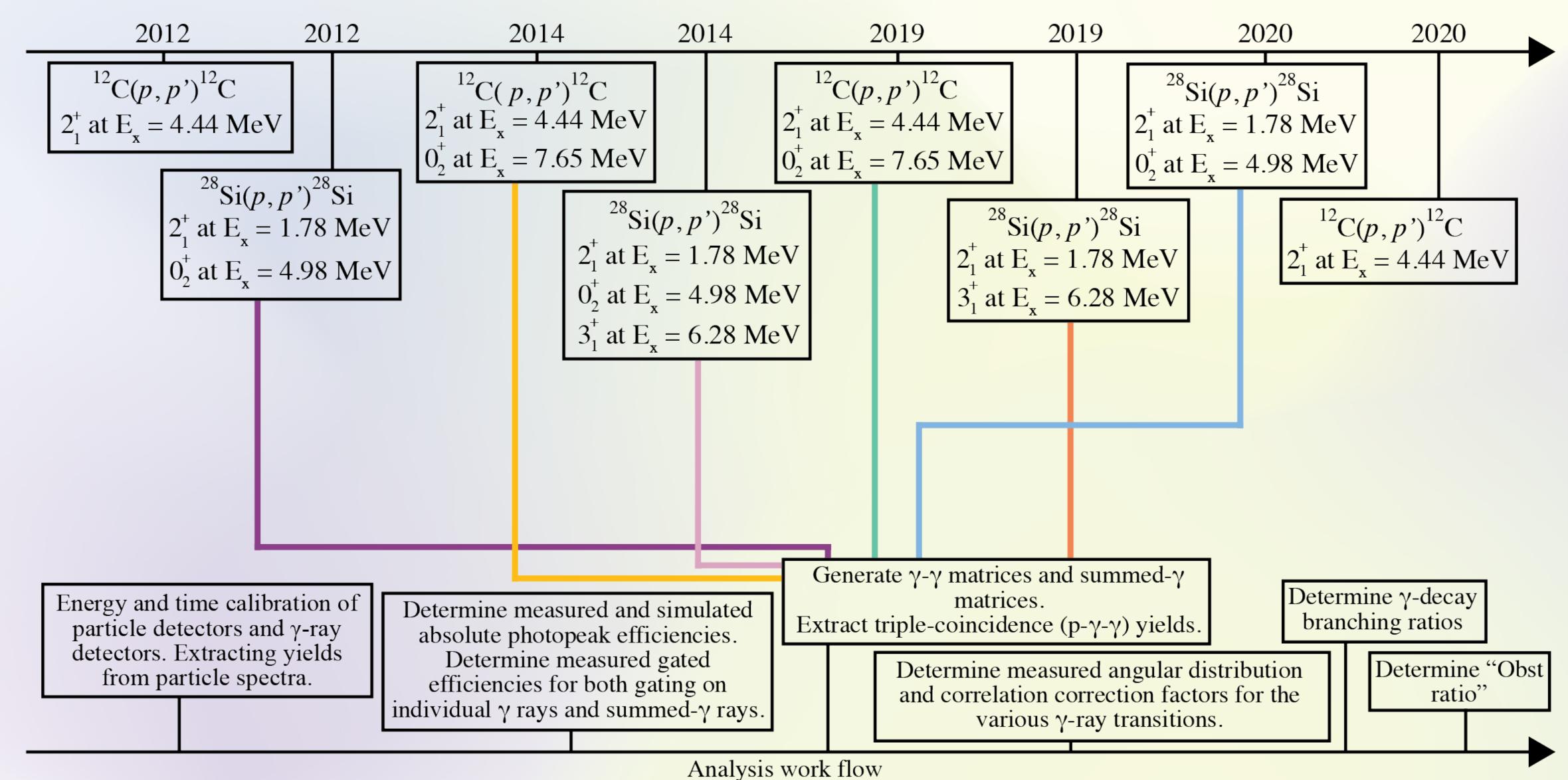








Measurements in this work and analysis pipeline



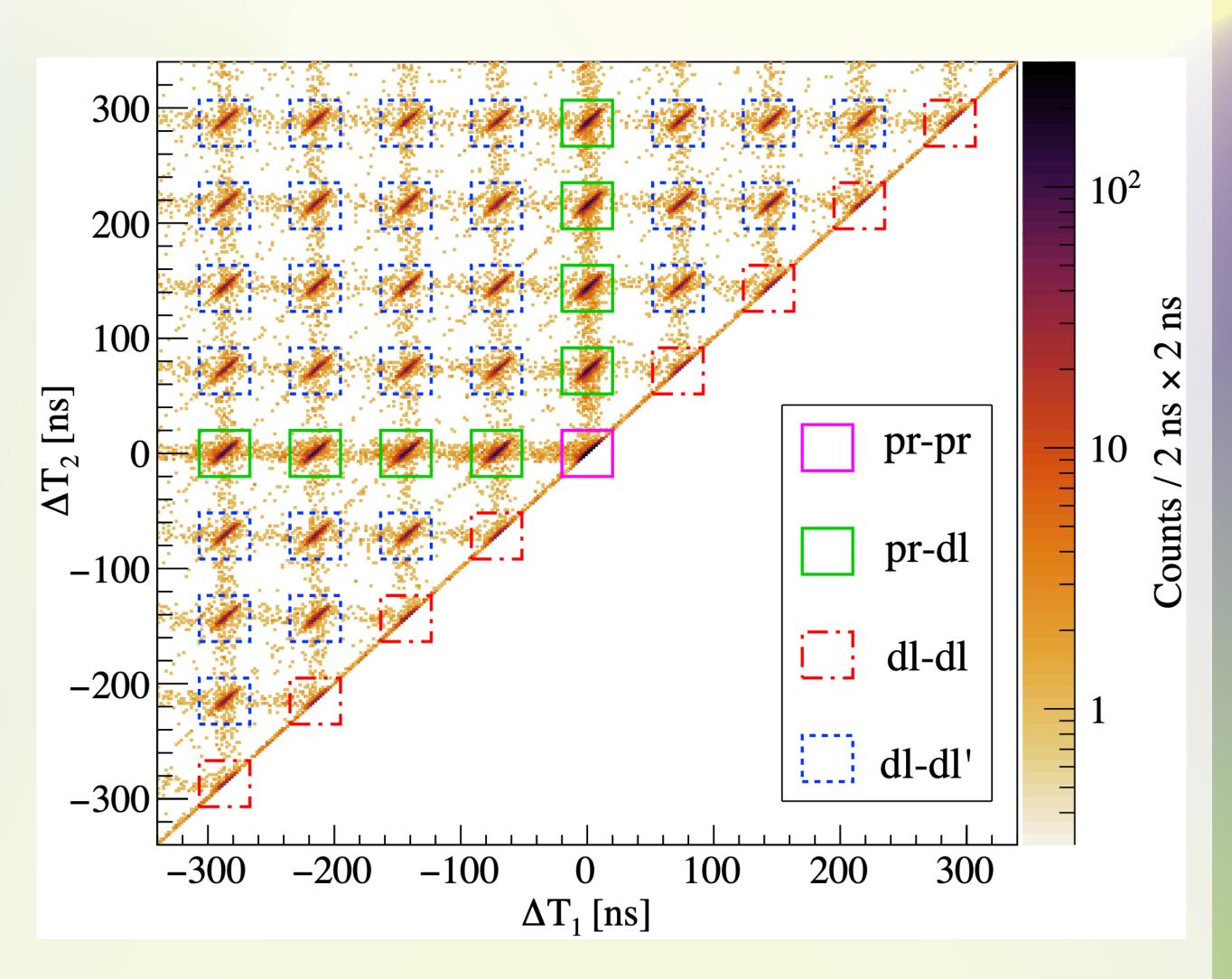


Time-correlated background subtraction

Different combinations of particles:

- Proton and both gammas are in coincidence with each other
- Proton and one gamma are in coincidence
- Both gammas are in coincidence with each other, but not with the proton
- Random background

Final yield of triple coincidences:

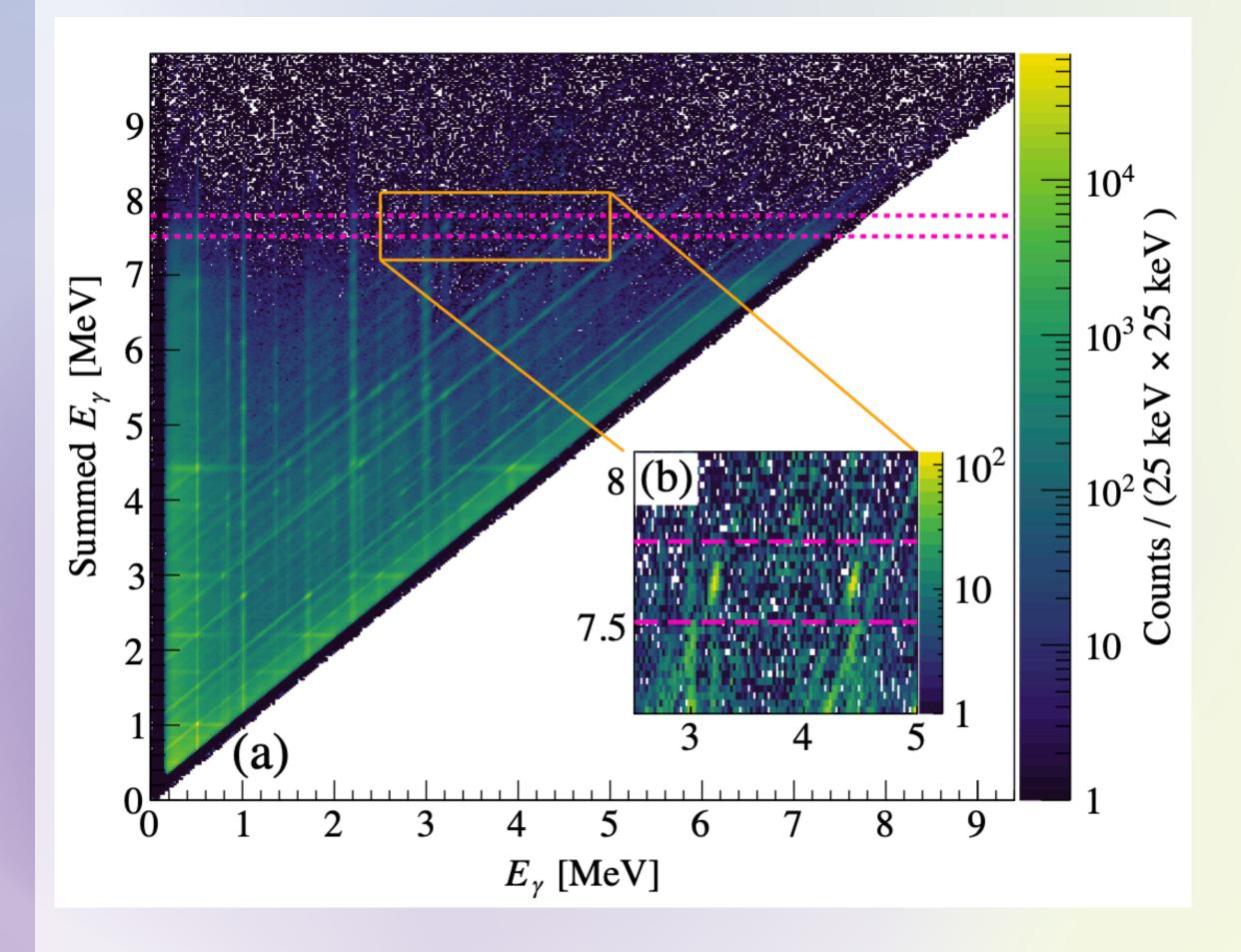




¹²C(p,p') 2019: Extracting triple-coincidence yields

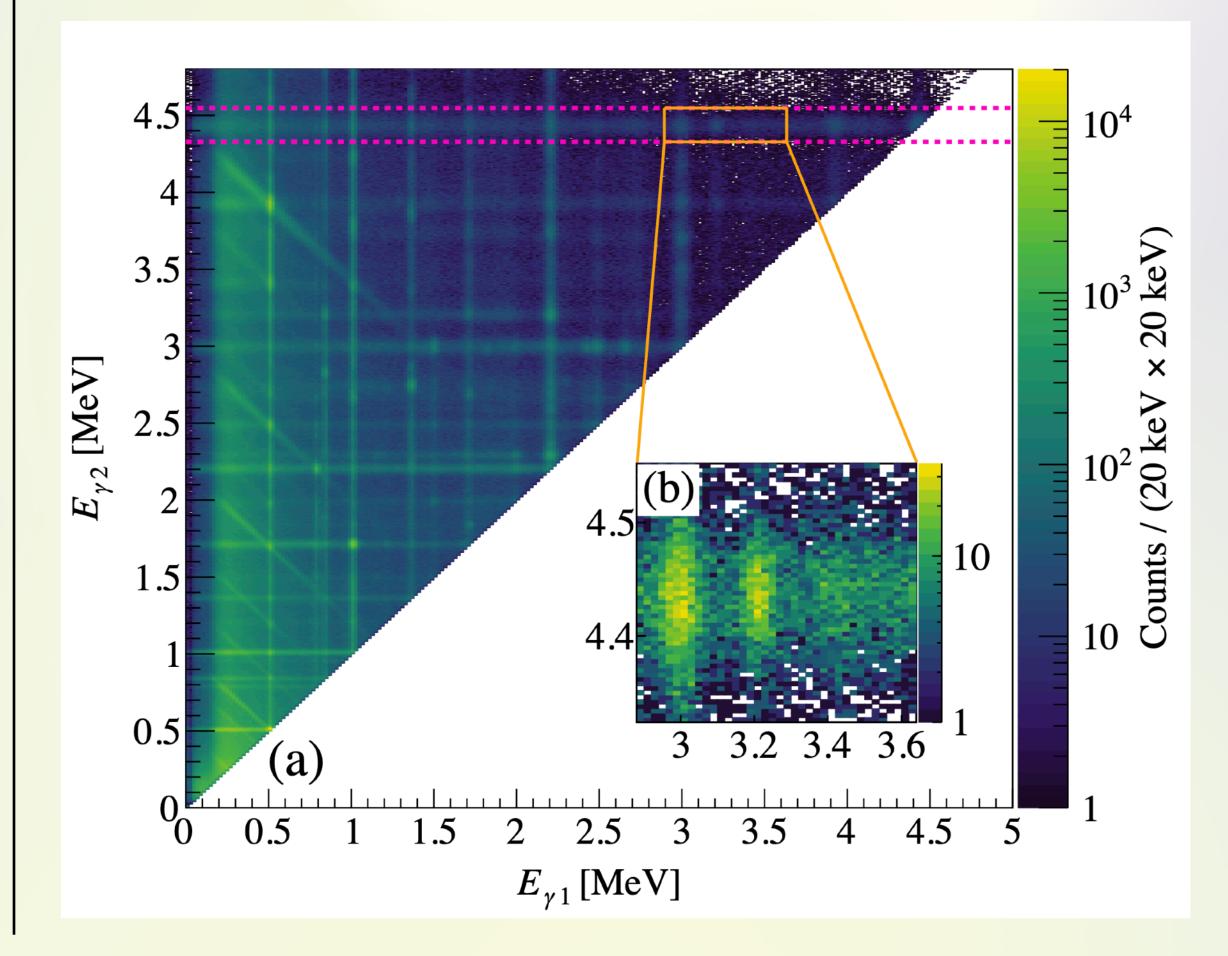
Summed E_{\gamma}

 3σ gate around $E_{\gamma}=7.65$ MeV and diagonal following the Compton scattered $E_{\gamma}=4.44$ MeV γ ray from the $E_{x}=4.44$ MeV 2_{1} in 12 C.



Gamma-gamma

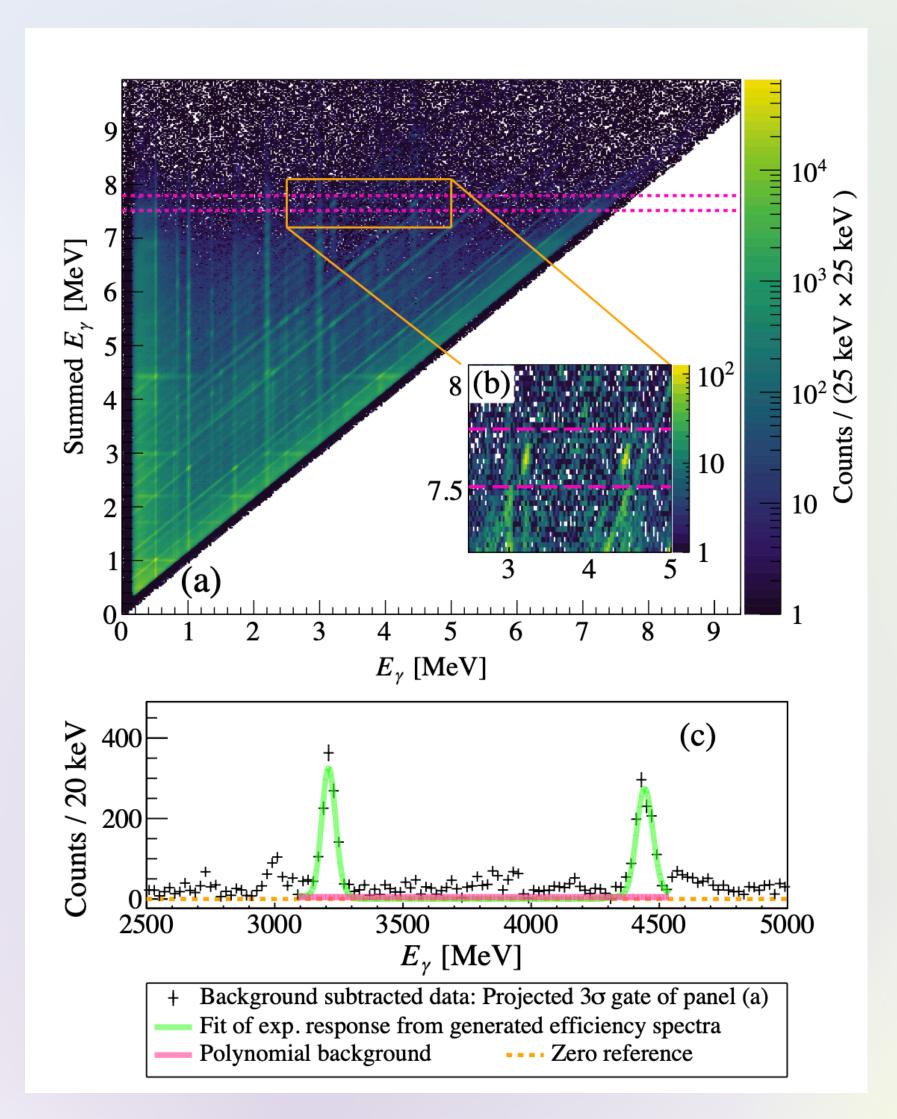
 3σ gate around $E_{\gamma}=4.44$ MeV from Hoyle state cascade of the $E_x=7.65$ MeV 0_2^+ in ^{12}C .



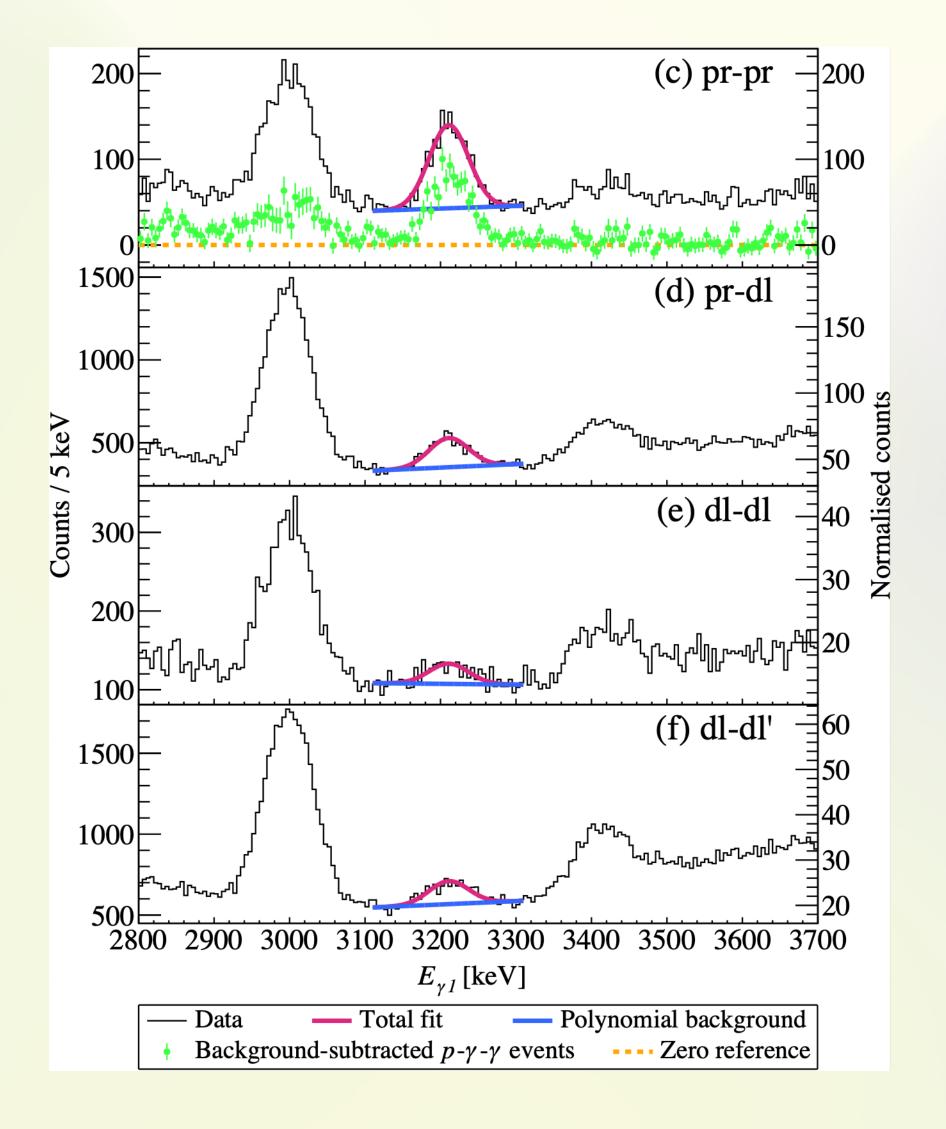


¹²C(p,p') 2019: Extracting triple-coincidence yields

Summed E_{\gamma}



Gamma-gamma

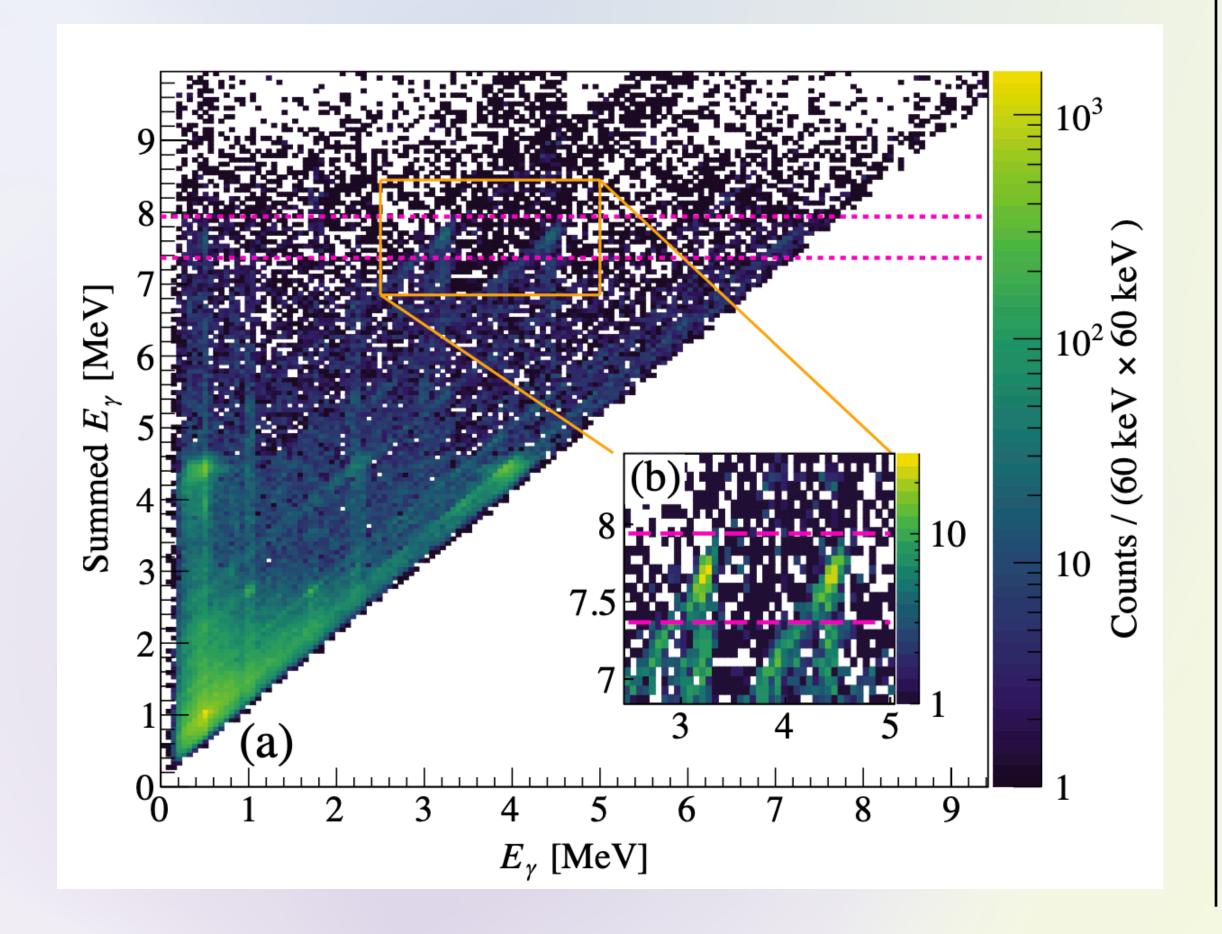




¹²C(p,p') 2014: Extracting triple-coincidence yields

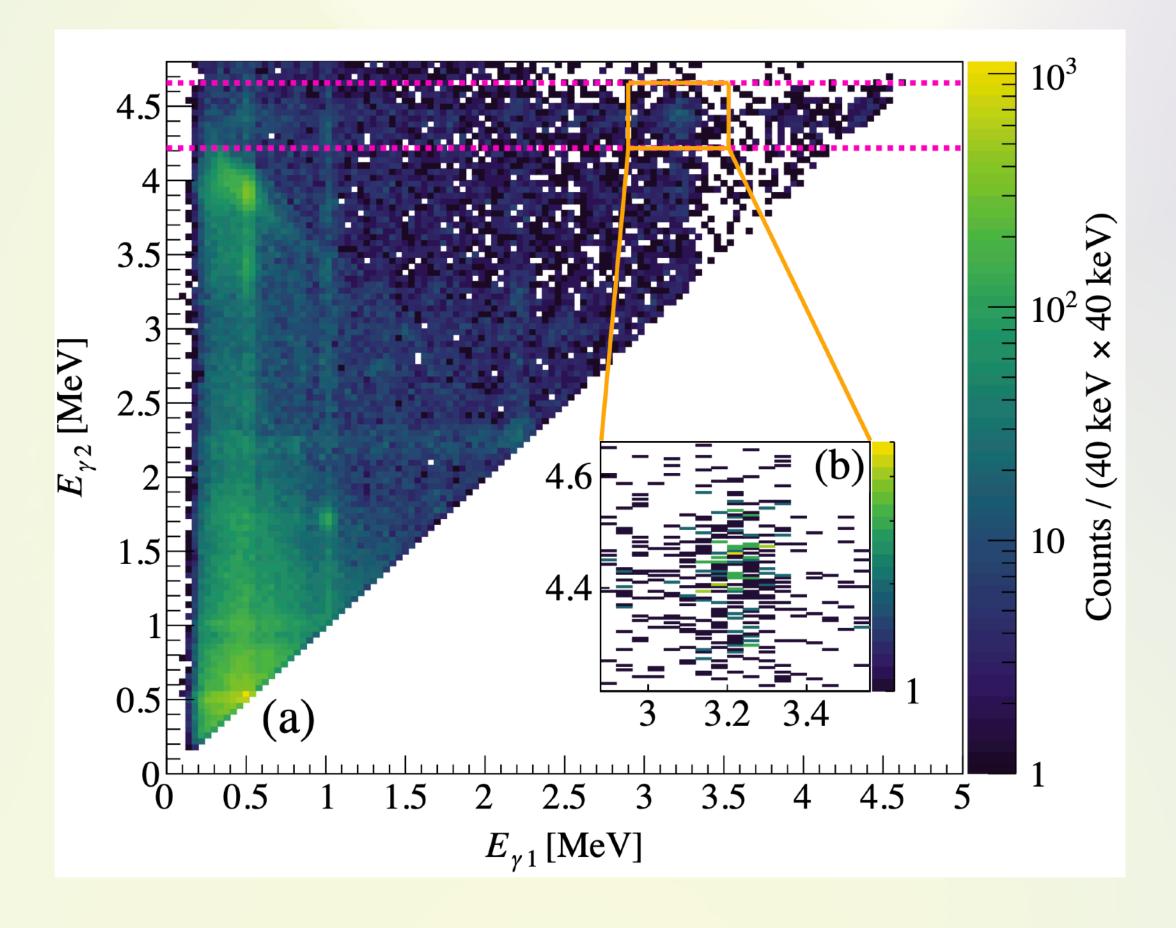
Summed E_{\gamma}

 3σ gate around $E_{\gamma}=7.65$ MeV and diagonal following the Compton scattered $E_{\gamma}=4.44$ MeV γ ray from the $E_{x}=4.44$ MeV 2_{1} in 12 C.



Gamma-gamma

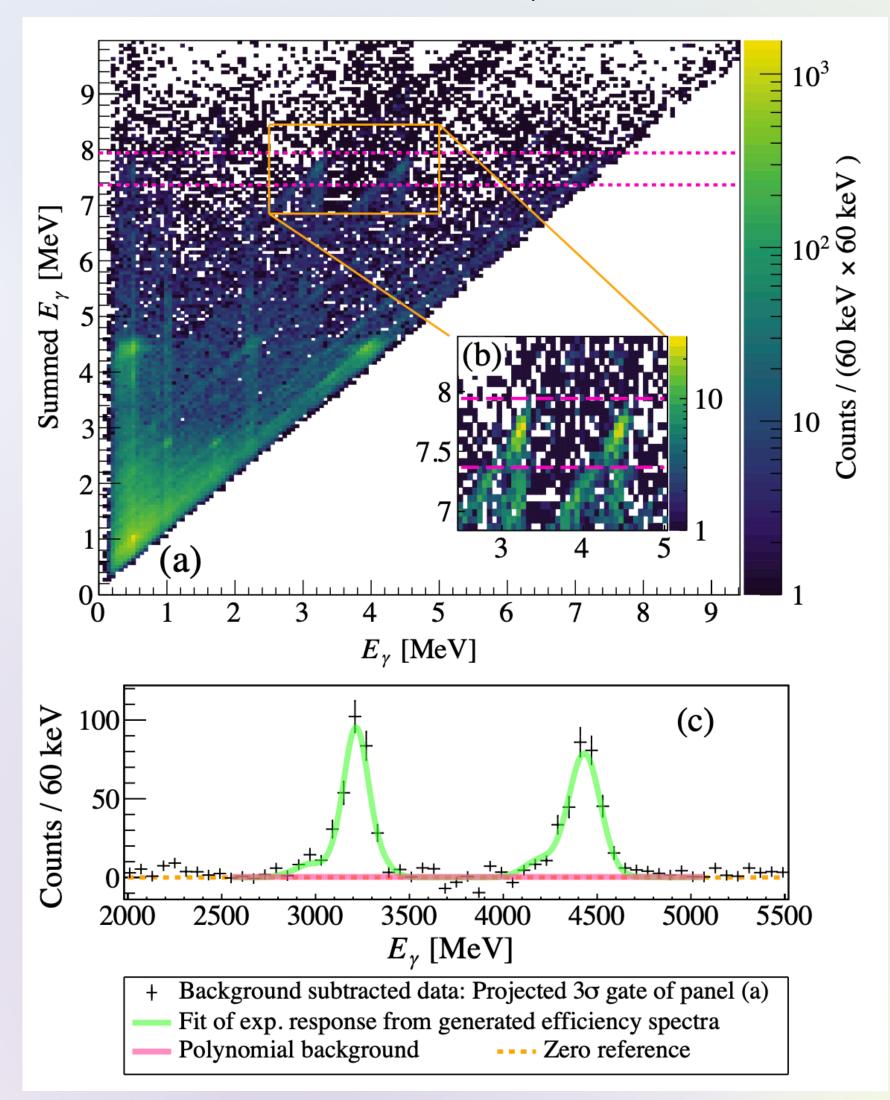
 3σ gate around $E_{\gamma}=4.44$ MeV from Hoyle state cascade of the $E_x=7.65$ MeV 0_2^+ in ^{12}C .



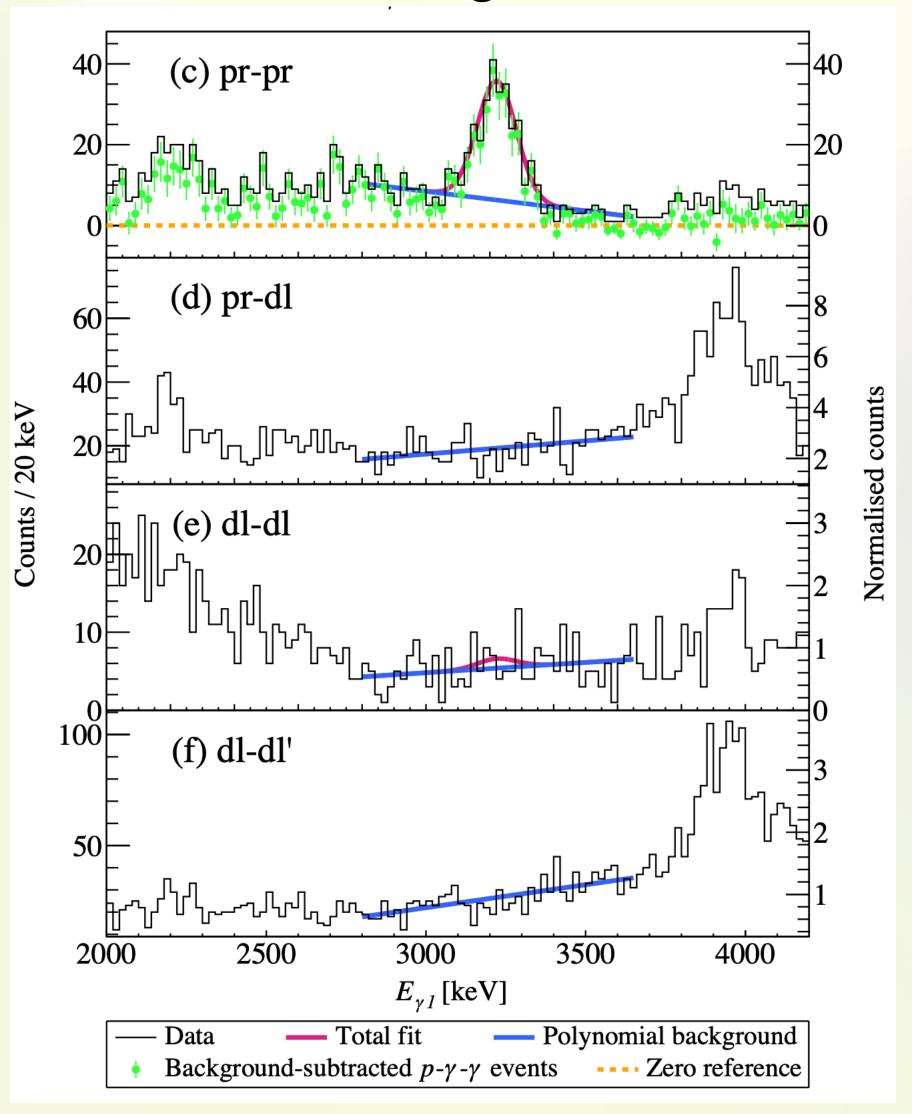


¹²C(p,p') 2014: Extracting triple-coincidence yields

Summed E_{\gamma}

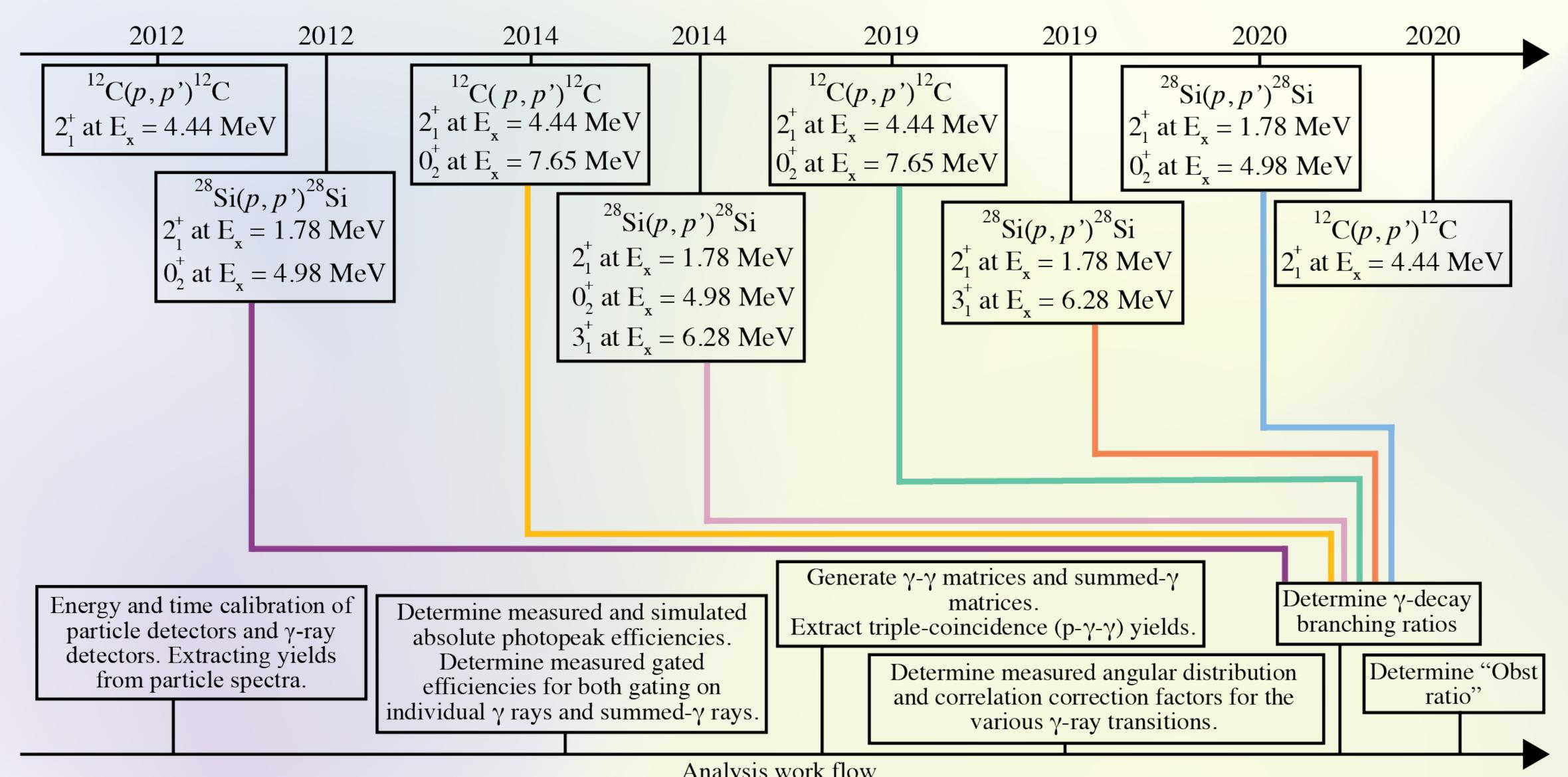


Gamma-gamma



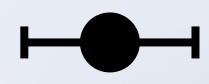


Measurements in this work and analysis pipeline





Results of this work



Original result as published



Published result is excluded



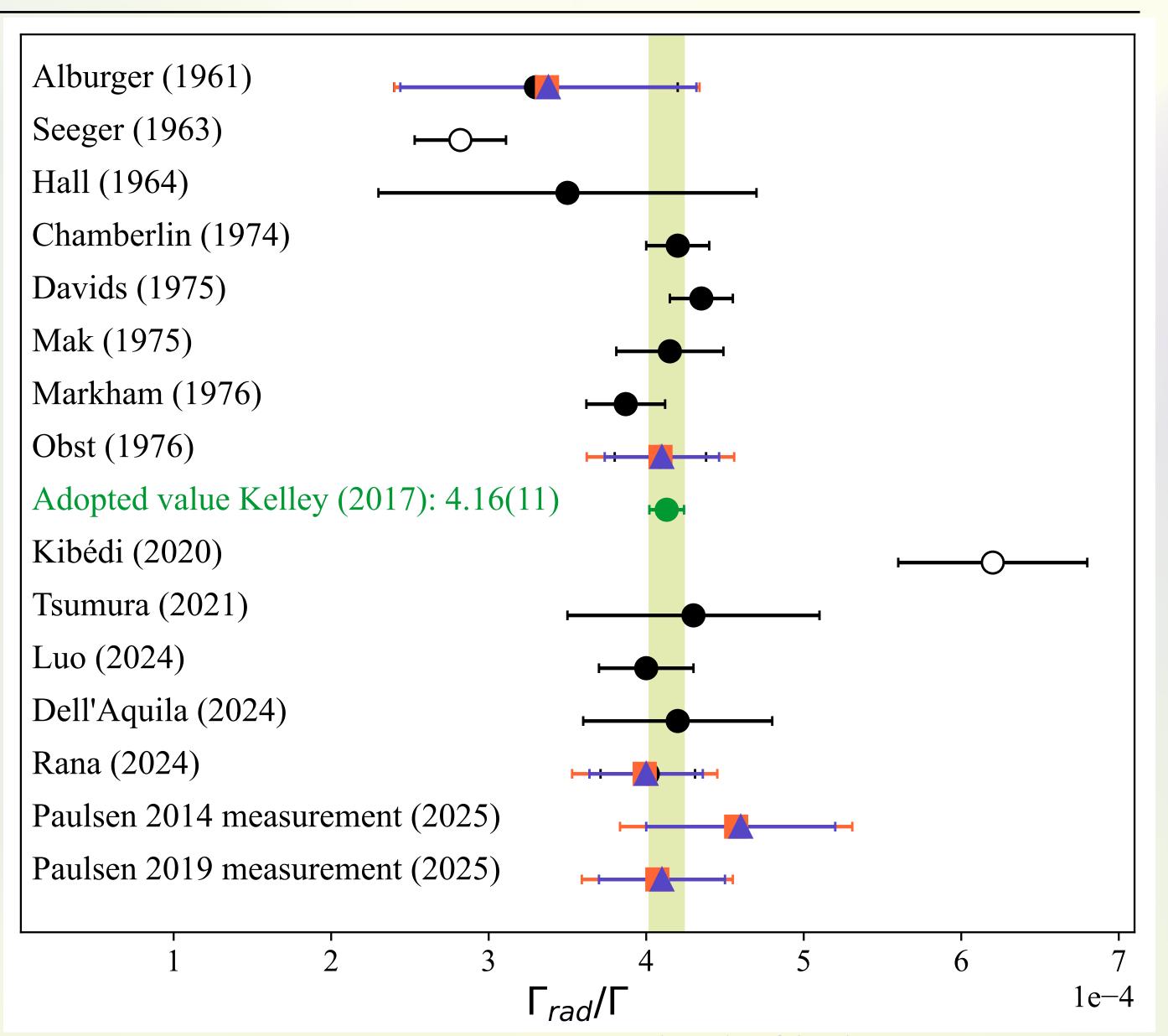
Indirect measurement utilizing $\Gamma \pi / \Gamma$ from Kelley *et al.* (2017)



Indirect measurement utilizing $\Gamma \pi / \Gamma$ from Eriksen *et al.* (2020)

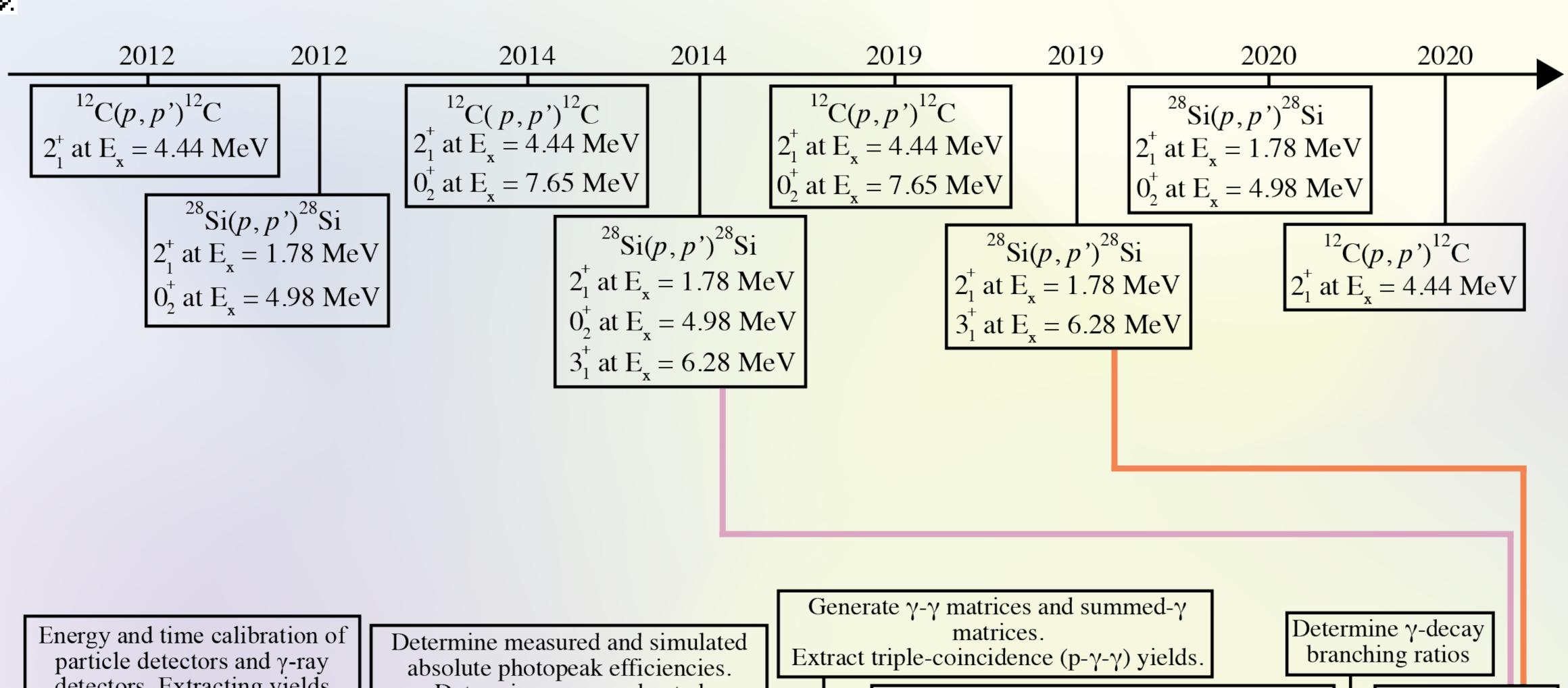
(Adopted value uncertainty reduced from 9% to 5%)

$$\frac{\Gamma_{\text{rad}}}{\Gamma} = \frac{\Gamma_{\gamma}^{E2} \left(1 + \alpha_{\text{tot}}\right) + \Gamma_{\pi}^{E0}}{\Gamma}$$





Measurements in this work and analysis pipeline



detectors. Extracting yields from particle spectra.

Determine measured gated efficiencies for both gating on individual γ rays and summed- γ rays.

Determine measured angular distribution and correlation correction factors for the various γ -ray transitions.

Determine "Obst ratio"

Analysis work flow



Obst et al. (1976) utilised a $3^+ \rightarrow 2^+ \rightarrow 0^+$ transition from the $E_x = 6.28$ MeV 3^+ state in 28 Si to normalise their final result. The final equation used to obtain the γ -decay branching ratio consisted of five ratios:

$$rac{\Gamma_{\gamma}^{E2}}{\Gamma^{7.65}} = rac{N_{020}^{7.65}}{N_{320}^{6.28}} imes rac{N_{320}^{6.28}}{N_{020}^{4.98}} imes rac{N_{
m inclusive}^{6.28}}{N_{
m inclusive}^{7.65}} imes rac{N_{
m inclusive}^{4.98}}{N_{
m inclusive}^{6.28}} imes rac{\epsilon_{1.78}}{\epsilon_{4.44}}$$
 $m A B C D E$



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 ho_{020}
 $ho_$

In Kibédi *et al.* (2020) the following statement was published regarding this equation in Obst *et al.* (1976): "Despite some differences between their experiment and ours, various combinations of these ratios should agree within a few percent."



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The largest difference occurred for the ratio B x D, dubbed the "Obst" ratio. By utilising the equations for the γ -decay branching ratios of the $E_x = 4.98$ MeV 0^+ and $E_x = 6.28$ MeV 3^+ states we can express the Obst ratio as



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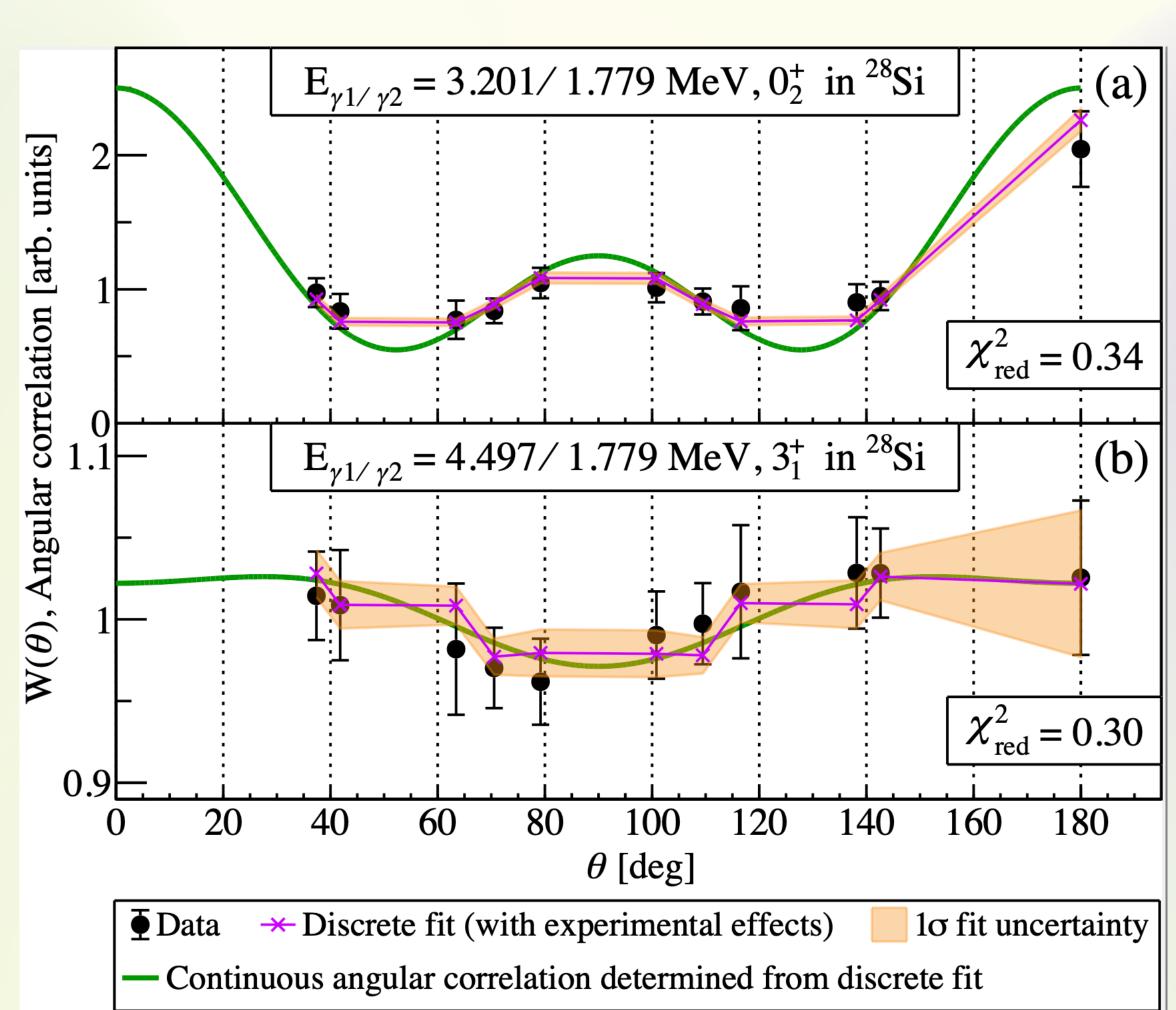
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$$B imes D = rac{\epsilon_{4.49}}{\epsilon_{3.20}} imes rac{W_{320}^{6.28}}{W_{020}^{4.98}} imes rac{\Gamma_{\gamma}^{E2}/\Gamma^{6.28}}{\Gamma_{\gamma}^{E2}/\Gamma^{4.98}}$$



The Obst ratio is highly dependent on the efficiency and the angular correlation correction factors of the detector setup.

$$B imes D = rac{\epsilon_{4.49}}{\epsilon_{3.20}} imes rac{W_{320}^{6.28}}{W_{020}^{4.98}} imes rac{\Gamma_{\gamma}^{E2}/\Gamma^{6.28}}{\Gamma_{\gamma}^{E2}/\Gamma^{4.98}}$$





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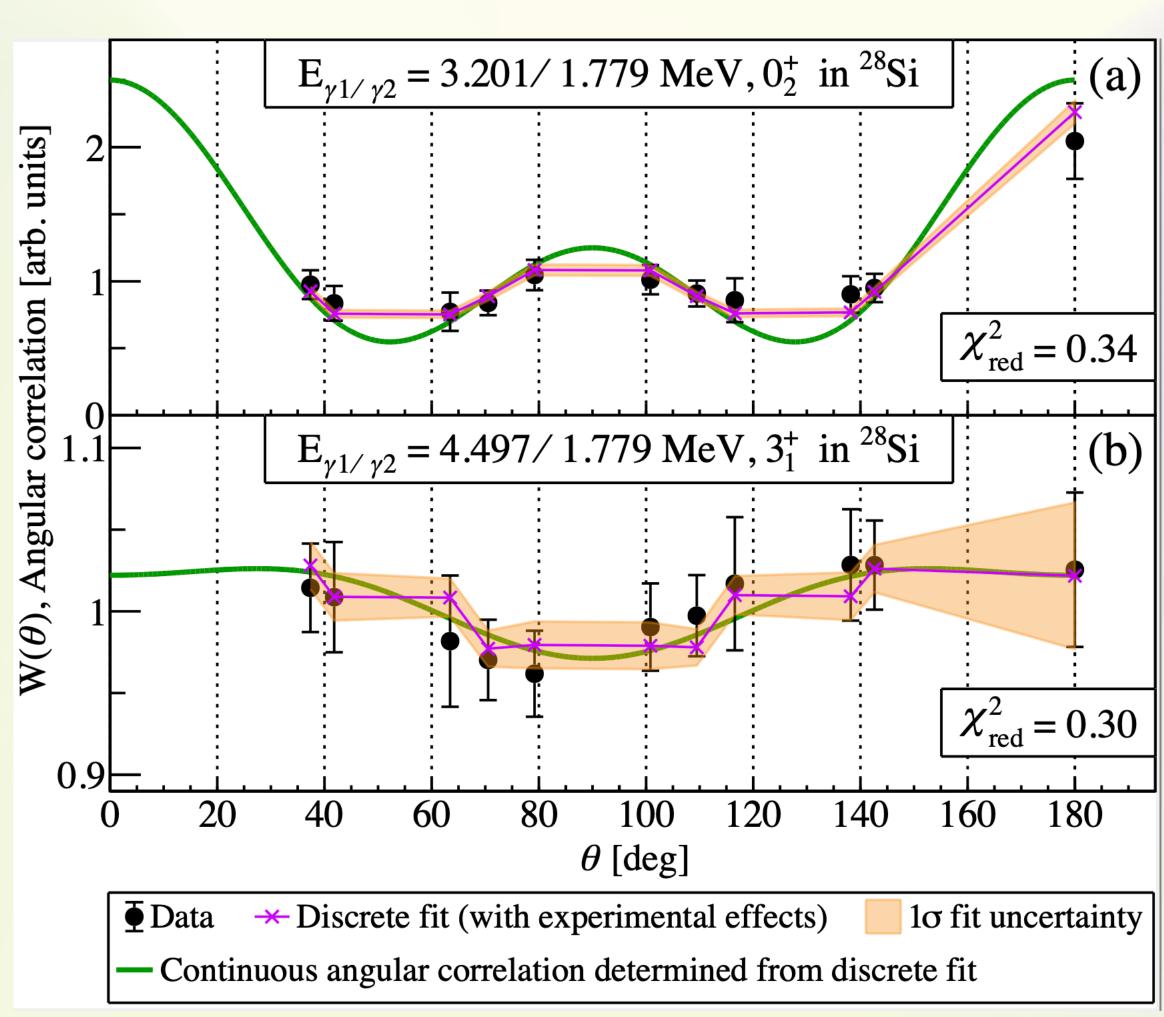
$$B imes D = rac{\epsilon_{4.49}}{\epsilon_{3.20}} imes rac{W_{320}^{6.28}}{W_{020}^{4.98}} imes rac{\Gamma_{\gamma}^{E2}/\Gamma^{6.28}}{\Gamma_{\gamma}^{E2}/\Gamma^{4.98}}$$

A GEANT4 simulation based on the description of the setup in Obst *et al.* (1976) [10] was performed. By comparing the angular correlation correction factors it is clear that

Simulation of Obst *et*
$$\frac{W_{320}^{6.28}}{al. (1976) [10] \text{ setup:}} = 0.787(2)$$

Kibédi *et al.* (2020) [9]:
$$\dfrac{W_{320}^{6.28}}{W_{020}^{4.98}} = 1.057(2)$$

Paulsen *et al.* (2025):
$$\frac{W_{320}^{6.28}}{W_{020}^{4.98}} = 1.047(1)$$





From the resulting angular correlation correction factors and the simulated Obst et al. (1976) [10] setup it is clear that that the ratios A-E can vary by more than a few percent.

The simulated Obst ratio of this work is $\approx 3\sigma$ away from Obst et al. (1976) [10]. This level of agreement is reasonable given the approximate nature of the simulation, with the geometry based on figures and text in Obst et al. (1976) [10].

$$B imes D = rac{\epsilon_{4.49}}{\epsilon_{3.20}} imes rac{W_{320}^{6.28}}{W_{020}^{4.98}} imes rac{\Gamma_{\gamma}^{E2}/\Gamma^{6.28}}{\Gamma_{\gamma}^{E2}/\Gamma^{4.98}}$$

Simulation of Obst et al. (1976) [10] setup:
$$\frac{W_{320}^{6.28}}{W_{020}^{4.98}} = 0.787(2)$$

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$$rac{W_{320}^{6.28}}{W_{020}^{4.98}} = 1.047(1)$$

TABLE IX. Summarised results of the Obst ratio (see Sec. III C).

Reference	Obst ratio [Eq. (7)]
Obst <i>et al.</i> [19]	0.409(15)
Kibédi et al. [15]	0.80(4)
28 Si (p, p') data from 2014 (this work)	0.82(4)
28 Si (p, p') data from 2019 (this work)	0.70(2)
Simulation of Obst setup (this work)	0.52(3)



• Throughout the reanalysis of the 2014 measurement, several necessary corrections to Kibédi *et al.* (2020) [9] were discovered.

$$\frac{\Gamma_{\gamma}^{E2}}{\Gamma} = \frac{N_{020}^{7.65}}{N_{\text{inclusive}}^{7.65} \times \epsilon_{3.21} \times \epsilon_{4.44} \times c_{\text{det}} \times W_{020}^{7.65}}$$

$$\frac{\Gamma_{\gamma}^{7.65}}{\Gamma} = \frac{N_{020}^{7.65}}{N_{020}^{4.98}} \times \frac{N_{\text{inclusive}}^{4.98}}{N_{\text{inclusive}}^{7.65}} \times \frac{\epsilon_{1.78}}{\epsilon_{4.44}} \times \frac{\epsilon_{3.20}}{\epsilon_{3.21}} \times \frac{W_{020}^{4.98}}{W_{020}^{7.65}} \times \frac{c_{\text{det}}^{4.98}}{c_{\text{det}}^{7.65}}$$



- Throughout the reanalysis of the 2014 measurement, several necessary corrections to Kibédi *et al.* (2020) [9] were discovered.
- The absolute photopeak efficiencies presented in the Kibédi et al. (2020) [9] are not absolute, but relative.
 - Efficiencies in Kibédi et al. (2020) [9] are simulated using PENELOPE.
 - Approximately a factor $\sqrt{2}$ difference from the experimental efficiencies obtained in this work.

$$\frac{\Gamma_{\gamma}^{E2}}{\Gamma} = \frac{N_{020}^{7.65}}{N_{\text{inclusive}}^{7.65} \times \epsilon_{3.21} \times \epsilon_{4.44} \times c_{\text{det}} \times W_{020}^{7.65}}$$

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- The detector combinations used by Kibédi *et al.* (2020) [9] was $c_{det} = 325$. The true number of detector combinations should be $c_{det} = 650$.

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- Throughout the reanalysis of the 2014 measurement, several necessary corrections to Kibédi *et al.* (2020) [9] were discovered.
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- The detector combinations used by Kibédi *et al.* (2020) [9] was $c_{det} = 325$. The true number of detector combinations should be $c_{det} = 650$.
- The relative photopeak efficiencies utilised in all results by Kibédi *et al.* (2020) [9] did **not** take the events in the **smooth Compton continuum** into account.

$$\frac{\Gamma_{\gamma}^{E2}}{\Gamma} = \frac{N_{020}^{7.65}}{N_{\text{inclusive}}^{7.65} \times \epsilon_{3.21} \times \epsilon_{4.44} \times c_{\text{det}} \times W_{020}^{7.65}}$$

$$\frac{\Gamma_{\gamma}^{7.65}}{\Gamma} = \frac{N_{020}^{7.65}}{N_{020}^{4.98}} \times \frac{N_{\text{inclusive}}^{4.98}}{N_{\text{inclusive}}^{7.65}} \times \frac{\epsilon_{1.78}}{\epsilon_{4.44}} \times \frac{\epsilon_{3.20}}{\epsilon_{3.21}} \times \frac{W_{020}^{4.98}}{W_{020}^{7.65}} \times \frac{c_{\text{det}}^{4.98}}{c_{\text{det}}^{7.65}}$$



Has the collective efforts of the community reduced the uncertainty?

Converting from radiative branching ratio to radiative width

$$\frac{\Gamma_{\text{rad}}}{\Gamma} = \frac{\Gamma_{\gamma}^{E2} \left(1 + \alpha_{\text{tot}}\right) + \Gamma_{\pi}^{E0}}{\Gamma}$$

 \longrightarrow

$$\Gamma_{
m rad} = \left[rac{\Gamma_{
m rad}}{\Gamma}
ight] imes \left[rac{\Gamma}{\Gamma_{\pi}^{
m E0}}
ight] imes \left[\Gamma_{\pi}^{
m E0}
ight]$$

Radiative branching ratio

Radiative width

Direct measurement average of all measurements. γ -decay branching ratio Kelley *et al.* (2017) [14] Pair-decay branching ratio Kelley *et al.* (2017) [14]

$$\Gamma_{\text{rad}} = 3.87(39) \text{ meV} (10.1\%)$$



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→

$$\Gamma_{
m rad} = \left\lceil \frac{\Gamma_{
m rad}}{\Gamma} \right
ceil imes \left\lceil \frac{\Gamma}{\Gamma_{\pi}^{
m E0}}
ight
ceil imes \left[\Gamma_{\pi}^{
m E0}
ight
ceil$$

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Weighted average

$$\Gamma_{\text{rad}} = 3.80(14) \text{ meV} \quad (3.8\%)$$

Non-weighted average

$$\Gamma_{\text{rad}} = 3.76(28) \text{ meV} (7.4\%)$$



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→

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$$\Gamma_{\text{rad}} = 3.76(28) \text{ meV} (7.4\%)$$

Direct measurement average of all measurements. γ -decay branching ratio average of all measurements. Pair-decay branching ratio Eriksen *et al.* (2020) [15]

Weighted average

$$\Gamma_{\text{rad}} = 3.357(99) \text{ meV } (3.0\%)$$

Non-weighted average

$$\Gamma_{\text{rad}} = 3.32(25) \text{ meV} (7.4\%)$$



Summary

- A new measurement of the gamma-decay branching ratio of the Hoyle state in ¹²C was performed at OCL.
 - The results agree well with the previously adopted value from Kelley *et al.* (2017) of $\Gamma_{rad}/\Gamma = 4.16(11) \times 10^{-4}$.
- An independent reanalysis of the measurement published by Kibédi et al. (2020) was performed.
 - Several necessary corrections to the results published by Kibédi et al. (2020) was found.
- A reanalysis of the data published by Kibédi et al. (2020) was performed.
 - The results agree well with the previously adopted value from Kelley *et al.* (2017) of $\Gamma_{rad}/\Gamma = 4.16(11) \times 10^{-4}$.
 - The source of the discrepancy in Kibédi *et al.* (2020) was discovered; The main contribution to the discrepancy originates in the efficiencies utilised.
- The scientific community has successfully reduced the uncertainty of the radiative width of the Hoyle state further.

Thank you to all our collaborators



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Special thanks to

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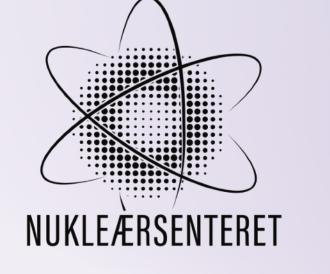
F. Zeiser

P. Adsley

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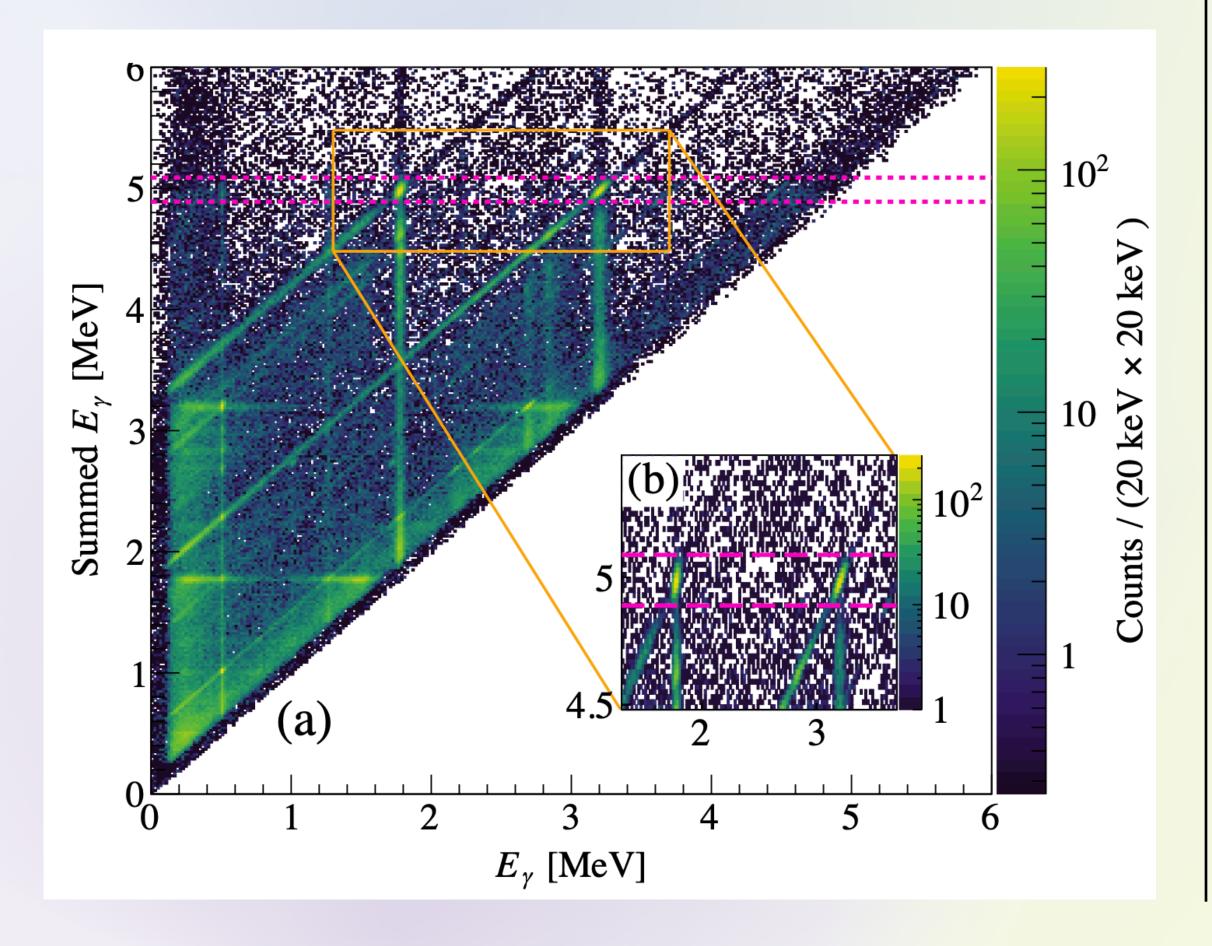
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²⁸Si(p,p') ²⁰²⁰: Extracting triple-coincidence yields

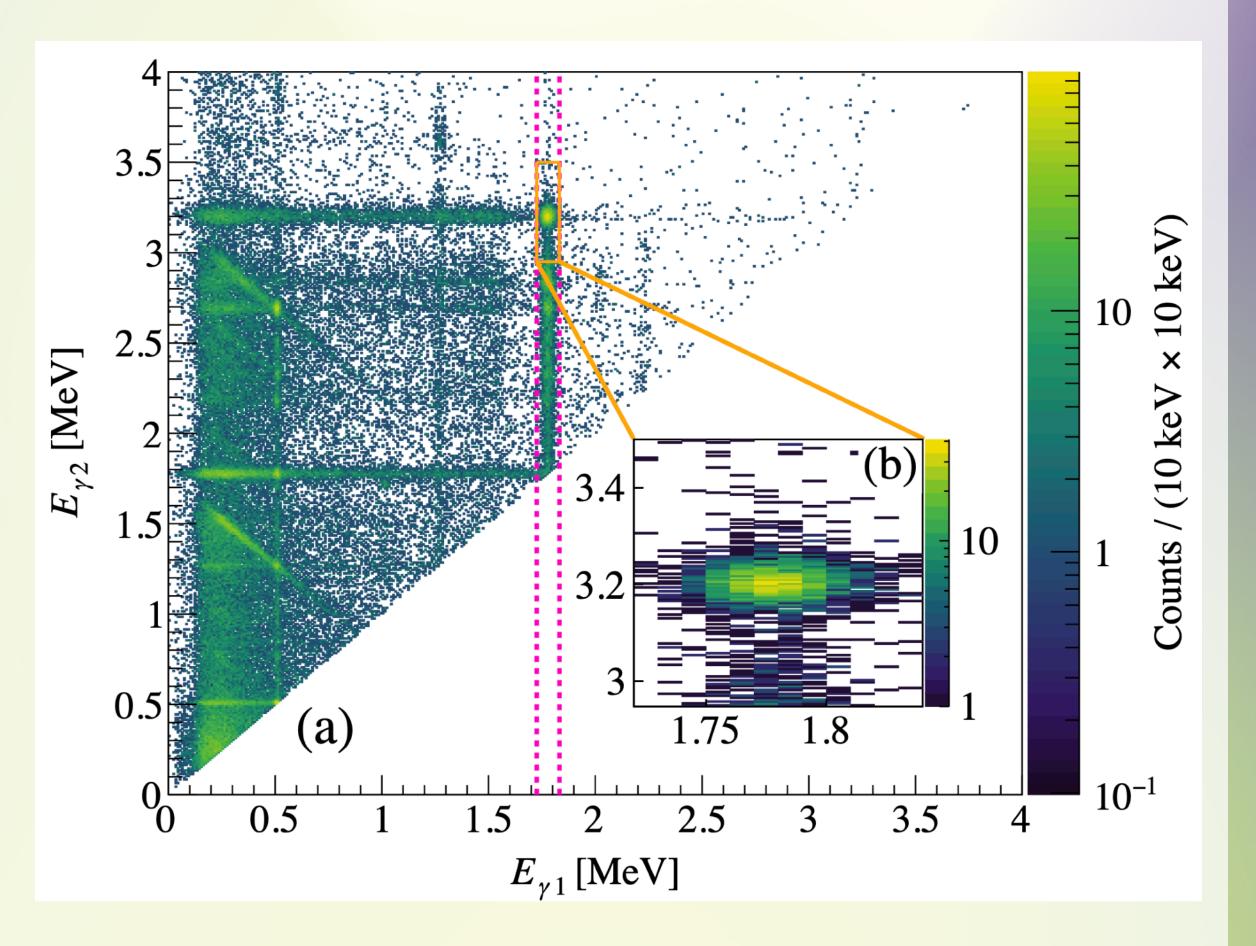
Summed E_{\gamma}

 3σ gate around $E_{\gamma}=4.98$ MeV and diagonal following the Compton scattered $E_{\gamma}=3.20$ MeV γ ray from the $E_{x}=4.98$ MeV 0_{2}^{+} in 0_{2}^{+}



Gamma-gamma

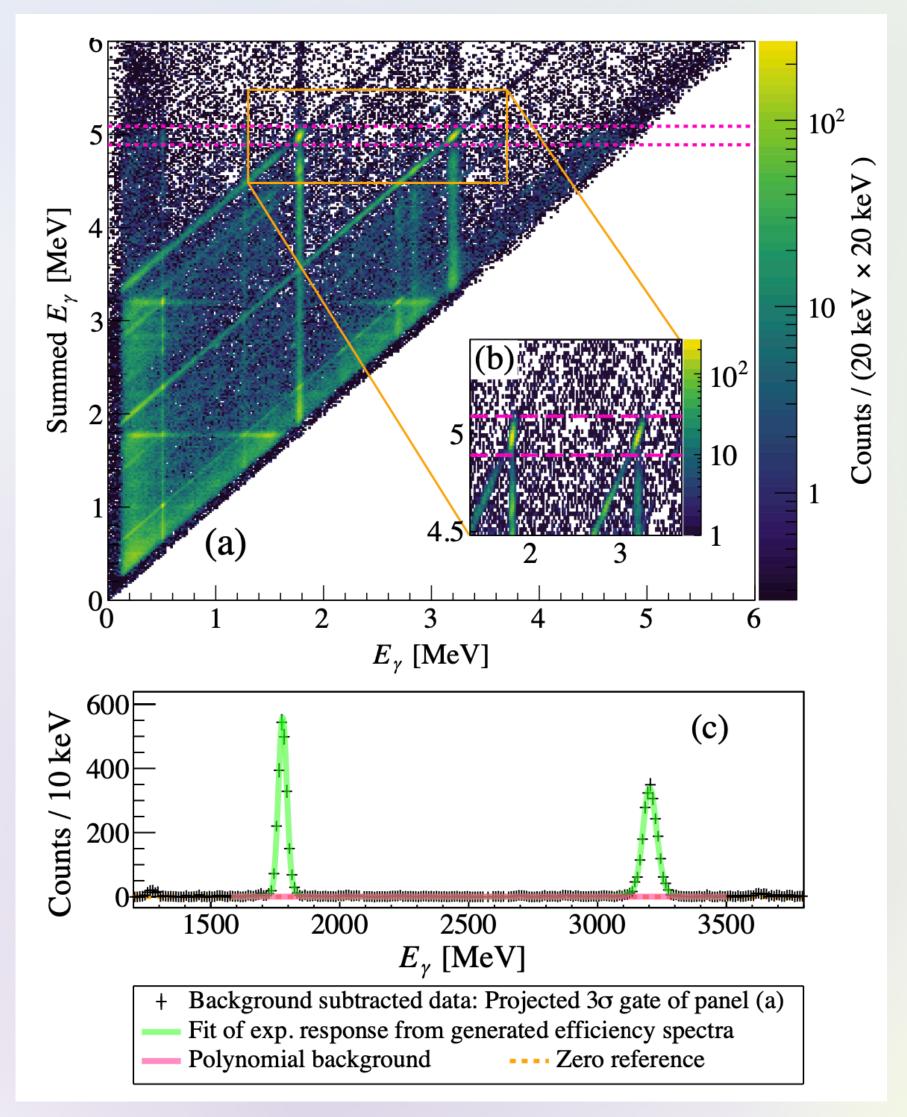
 3σ gate around $E_{\gamma}=1.79$ MeV from the cascade from $E_x=4.98$ MeV 0_2^+ in 28 Si.





²⁸Si(p,p') ²⁰²⁰: Extracting triple-coincidence yields

Summed E_{\gamma}



Gamma-gamma

