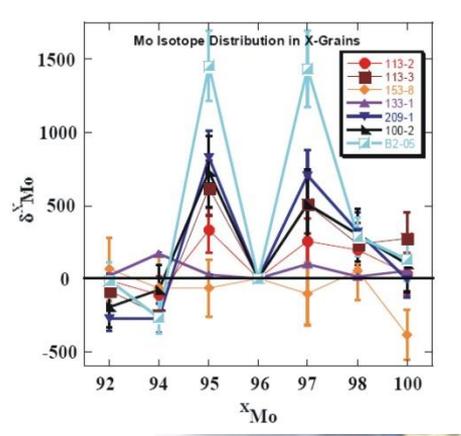
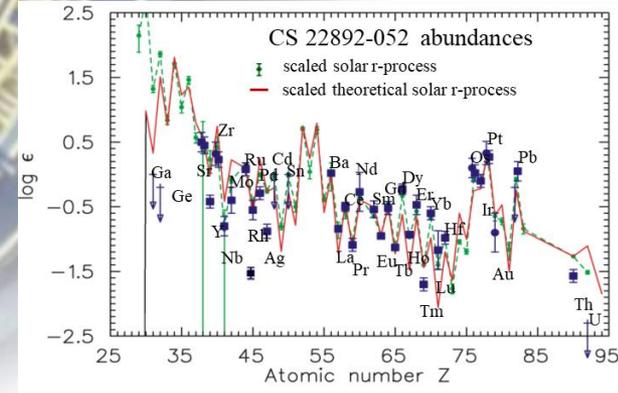
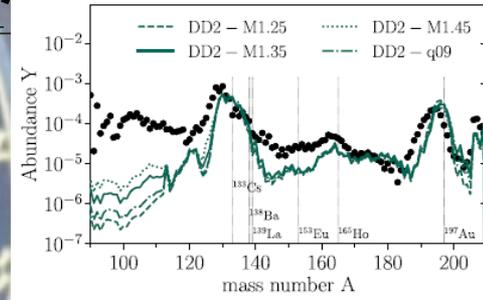


From the classical r-process to the multimessenger era



s-process path

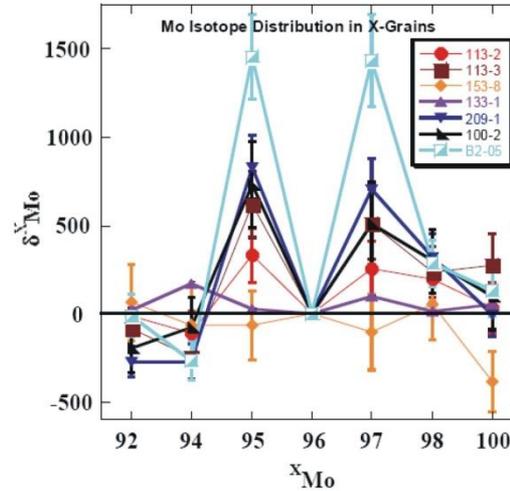
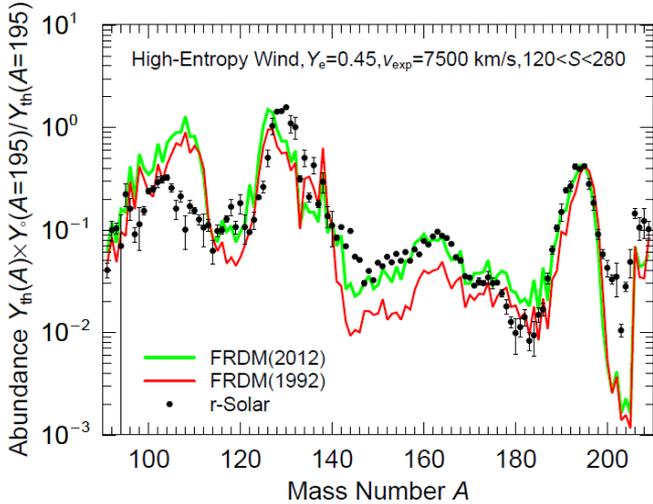
r-process path



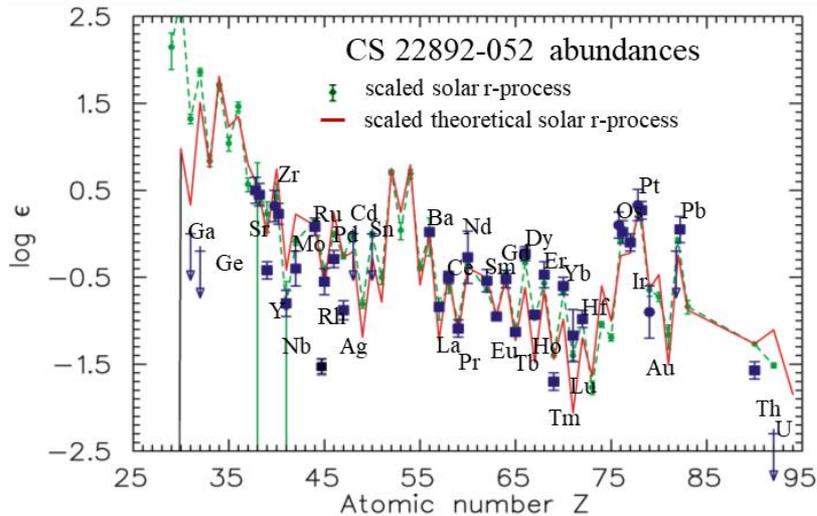
r-process observables today

Isotopic S.S.-abundances with better nuclear physics input

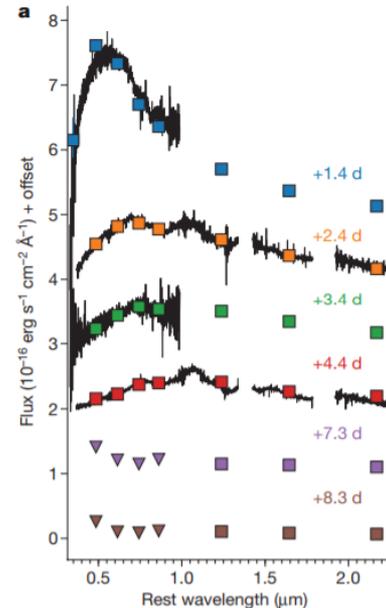
“FUN” anomalies in meteoritic samples and stardust



Presolar SiC grains;
isotopic composition of Sr, Zr, Mo, Ru, Ba...



Elemental abundances in UMP halo stars



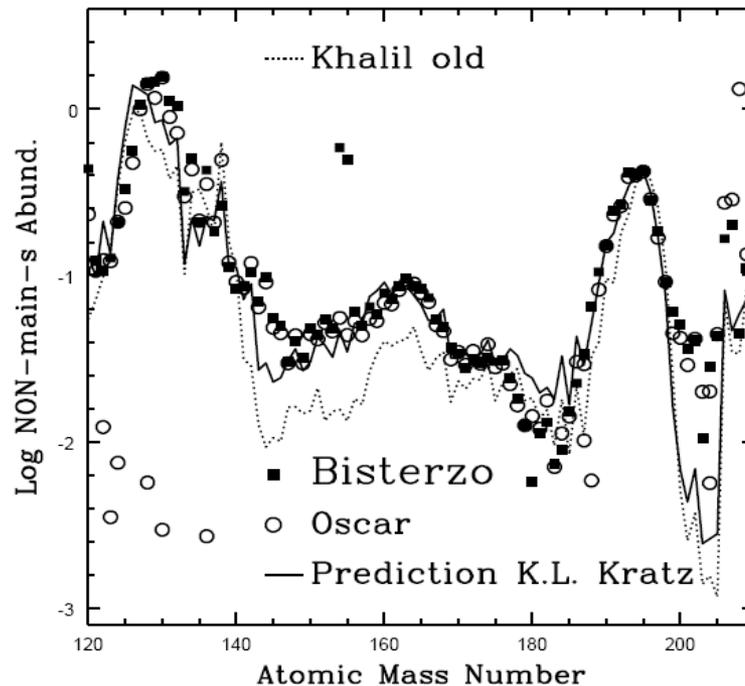
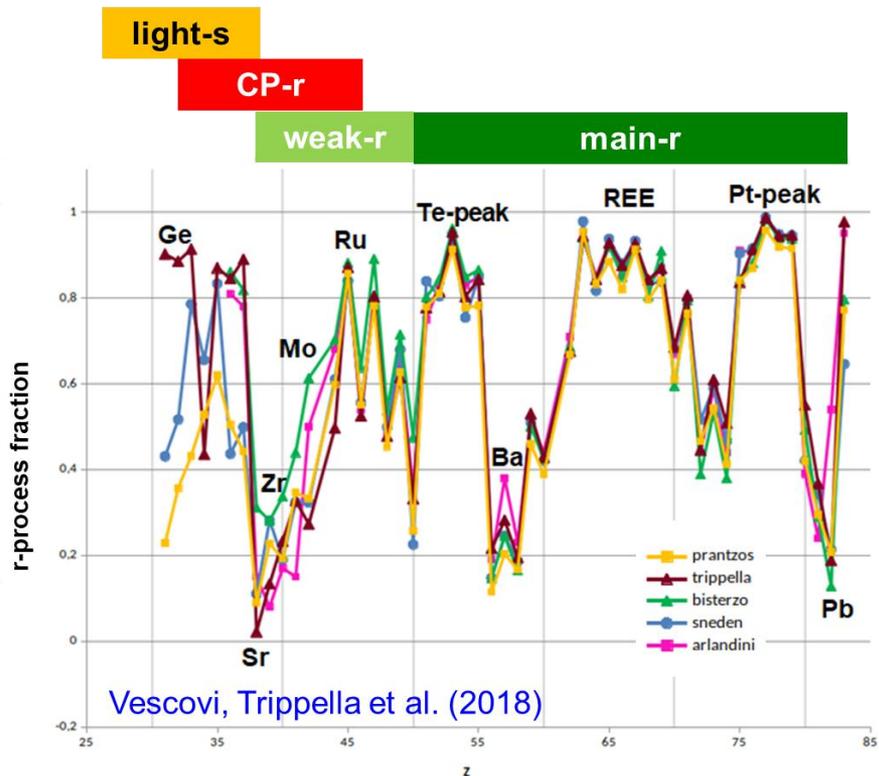
Neutron star merger event GW170817



kilonova AT2017gfo

Comparison of S.S.-r “residuals” with primary S.S.-r abundances

Ongoing Perugia-Mainz project
 ... identifying S.S.-s and S.S.-r
 uncertainties



“Khalil old” ⇒ HEW with **FRDM(1992)**

“Pred. KLK” ⇒ HEW with **FRDM(2012)**

Example ^{96}Zr r-“residual“:

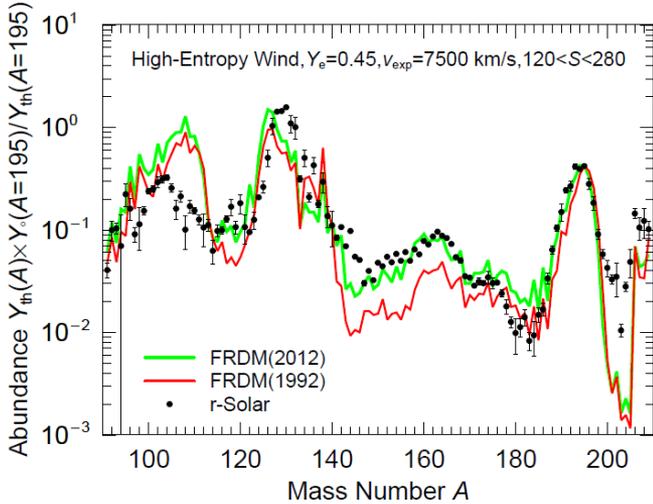
Käppeler '89	100 %
Arlandini '99	45.0 %
Bisterzo '11	48.7 %
Bisterzo '14	61.3 %
Tripella '16	98.6 %

to be compared to r-“primary“:

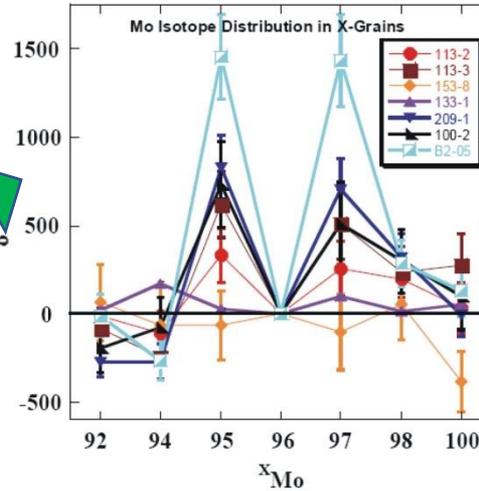
Kratz '19 **98.4 %**

r-process observables today

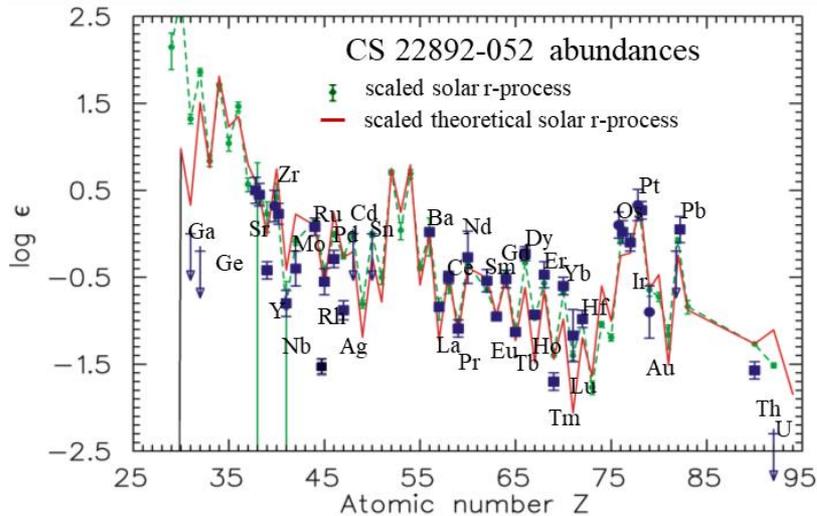
Isotopic S.S.-abundances with better nuclear physics input



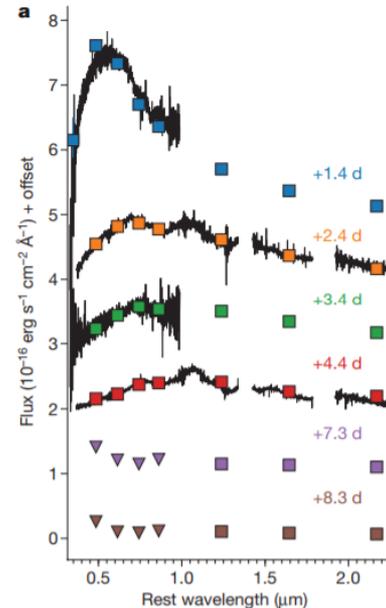
“FUN” anomalies in meteoritic samples and stardust



Presolar SiC grains; **isotopic composition** of Sr, Zr, Mo, Ru, Ba...



Elemental abundances in UMP halo stars



Neutron star merger event GW170817

kilonova AT2017gfo

Light p-process isotopes in the S.S.

Historical papers “p-process”

B²FH (1957)

Arnould (1976)

Woosley & Howard (1978)

Main goal:

explanation of nucleosynthetic origin of light p-nuclei, including ⁹²Mo/⁹⁴Mo

Selected subsequent papers / scenarios

Howard // Meyer et al. (1992, **2000**)

Hoffman et al. (1996, **2008**)

Schatz et al. (1998, 2003)

Rauscher et al. (2002)

Fisker et al., (2006)

Wanajo et al. (2009)

Farouqi et al. (**2009**)

Travaglio et al. (2011, **2018**)

Eichler et al. (2017)

Pignatari et al. (2018)

Kratz et al. (**2018**)

Sasaki et al. (2022)

n-burst in exploding massive stars

v-driven winds in SN II

rp-process in X-ray bursters

γ-process in pre-SN and SN

vp-process in SN II

p-production in EC-SN

light p, s, r in SN II at low S

p-process in SN Ia

nucleosynthesis in ccSN

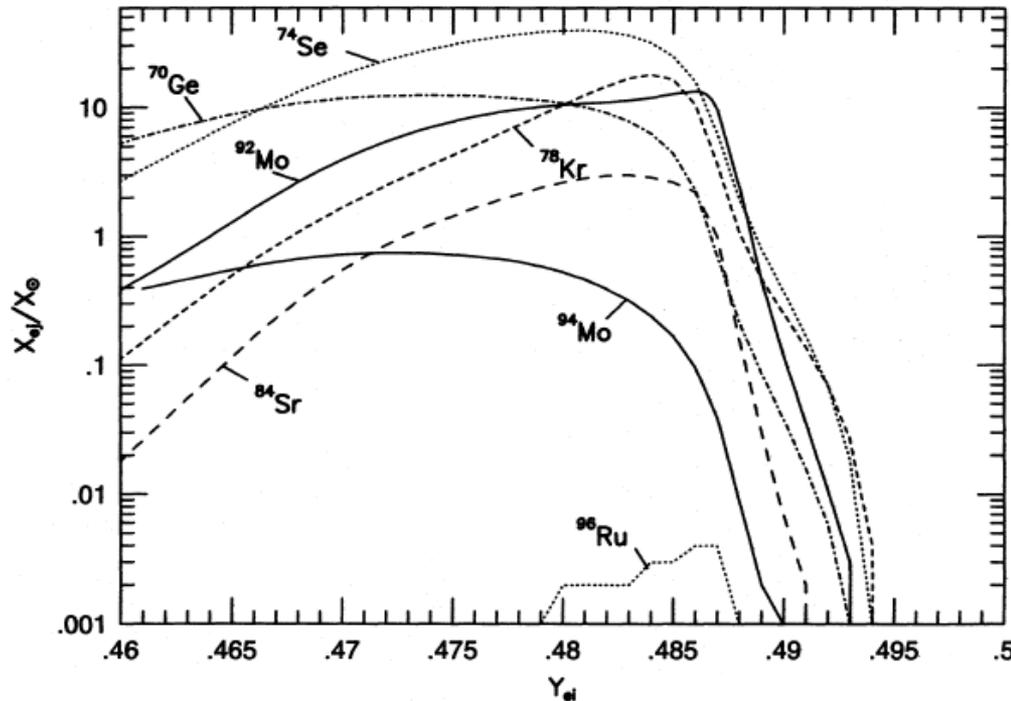
n-burst in He-shell of ccSN

light trans-Fe elements in SN-HEW

hypernova vp-process

Production of the light p-process nuclei in neutrino-driven winds

Hoffman, Woosley, Fuller, Meyer, ApJ 460 (1996)



“normalized production factors“

$$X_{ej}/X_{\odot} = f(Y_e)$$

individual Y_e 's; $S/(N_A k) \approx 50$

“No initial abundances of r- or s-process seed need be invoked

⇒ this component of the p-process is **primary** rather than secondary.“

Result on ^{92}Mo :

**Underproduction
relative to solar**

The authors give 3 possible explanations:

- 1) The νp -process is active, but ^{92}Mo is primarily produced at other sites
- 2) The νp -process is not active, so another explanation is needed
- 3) The νp -process is active, but the nuclear parameters (...) are incorrect

Abundances of light trans-Fe ISOTOPES in the ccSN-HEW scenario

Continuing the work of Hoffman, Woosley et al. (1996)...

Farouqi, Kratz & Pfeiffer;

Publications of the Astron. Soc. of Australia (PASA) 26 (2009)

"Co-production of light p-, s- and r-process isotopes in the high-entropy wind of type II supernovae"

Typical yields (M_{\odot}) for $Y_e = 0.46$			
^{64}Zn	$5.6 \cdot 10^{-5}$	^{78}Kr	$4.0 \cdot 10^{-8}$
^{70}Ge	$8.9 \cdot 10^{-6}$	^{84}Sr	$1.2 \cdot 10^{-8}$
^{74}Se	$5.4 \cdot 10^{-8}$	^{92}Mo	$2.6 \cdot 10^{-8}$

sizeable abundance yields, comparable to SN Ia of Travaglio et al. (2011, 2015)

Isotopic pairs (nucleosynth. origin)	Isotopic abundance ratios	
	S.S.	HEW
$^{64}\text{Zn}(\text{p}) / ^{70}\text{Zn}(\text{r})$	78.4	79.4
$^{70}\text{Ge}(\text{s,p}) / ^{76}\text{Ge}(\text{r})$	2.84	4.61
$^{74}\text{Se}(\text{p}) / ^{76}\text{Se}(\text{s})$	$9.4 \cdot 10^{-2}$	$9 \cdot 10^{-2}$
$^{74}\text{Se}(\text{p}) / ^{82}\text{Se}(\text{r})$	0.101	0.113
$^{78}\text{Kr}(\text{p}) / ^{86}\text{Kr}(\text{r,s})$	$2.1 \cdot 10^{-2}$	$8 \cdot 10^{-4}$
$^{84}\text{Sr}(\text{p}) / ^{86}\text{Sr}(\text{s})$	$5.7 \cdot 10^{-2}$	$4 \cdot 10^{-2}$
$^{90}\text{Sr}(\text{s,r}) / ^{96}\text{Zr}(\text{r,s})$	18.4	5.56
$^{92}\text{Mo}(\text{p}) / ^{94}\text{Mo}(\text{p})$	1.60	1.73
$^{96}\text{Ru}(\text{p}) / ^{98}\text{Ru}(\text{p})$	2.97	2.57

all historical p-, s- and r-**"only"** isotopes are co-produced, from ^{64}Zn to ^{104}Ru

Star-dust observables of Zr, Mo and Ru in SiC-X grains

Zr, Mo, Ru in **presolar SiC X-grains** (sub-micron size)

measured with **NanoSIMS** or **RIMS**

... ejecta of stars that contributed to the proto-solar nebula;
due to SiC's refractory nature, these grains survived S.S. formation;
type X-grains are believed to contain isotopic patterns from **presolar** explosive nucleosynthesis events.

Remember:

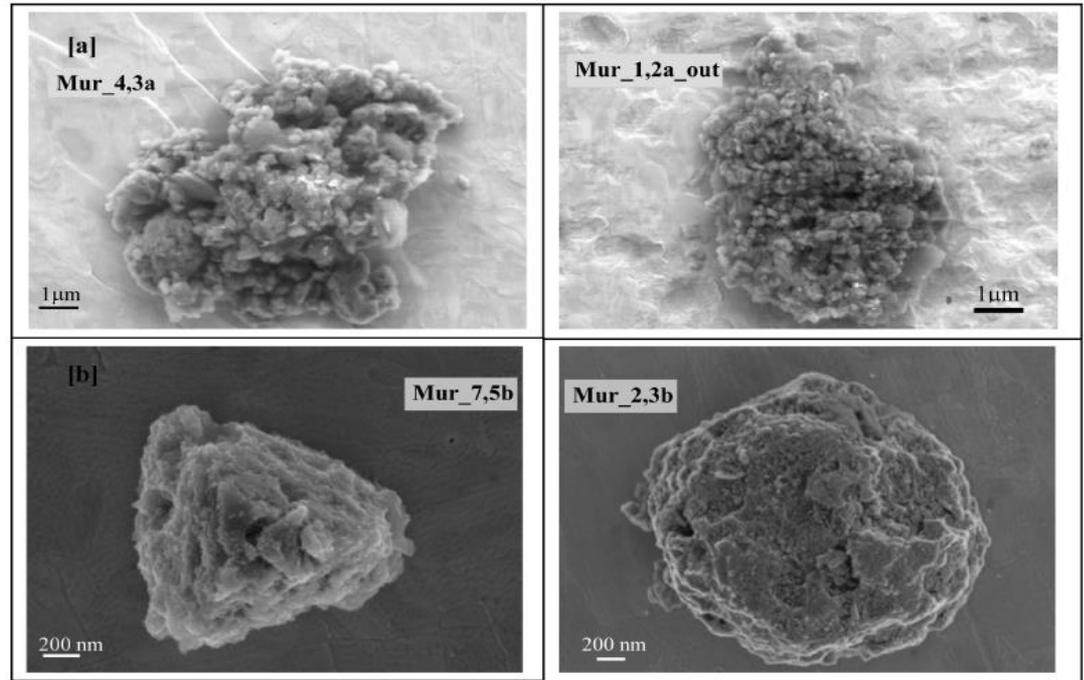
Mo of particular interest:

7 stable isotopes with $^{92,94}\text{Mo}$ "p-only"

^{96}Mo "s-only"

$^{95,97,98}\text{Mo}$ s+r

^{100}Mo "r-only"



Marhas, Ott & Hoppe, MPS 42 (2007)

Among suggested nucleosynthesis scenarios:

- "n-burst" in shocked He shell in SNe
- rp-process in X-ray bursters
- p-process in SN-Ia or EC-SN
- **v-driven wind in cc-SN-II**

Question:

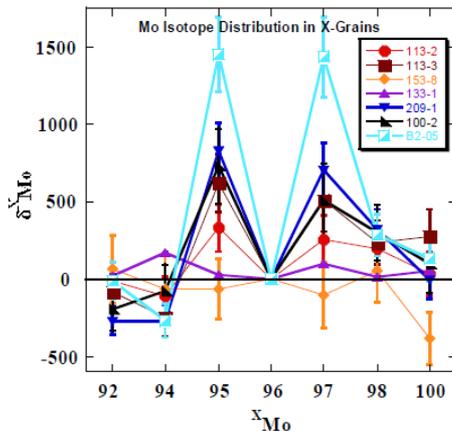
can the low-S CP-r component of the HEW r-process produce all 7 Mo isotopes at the same time?

Types of presolar SiC grains

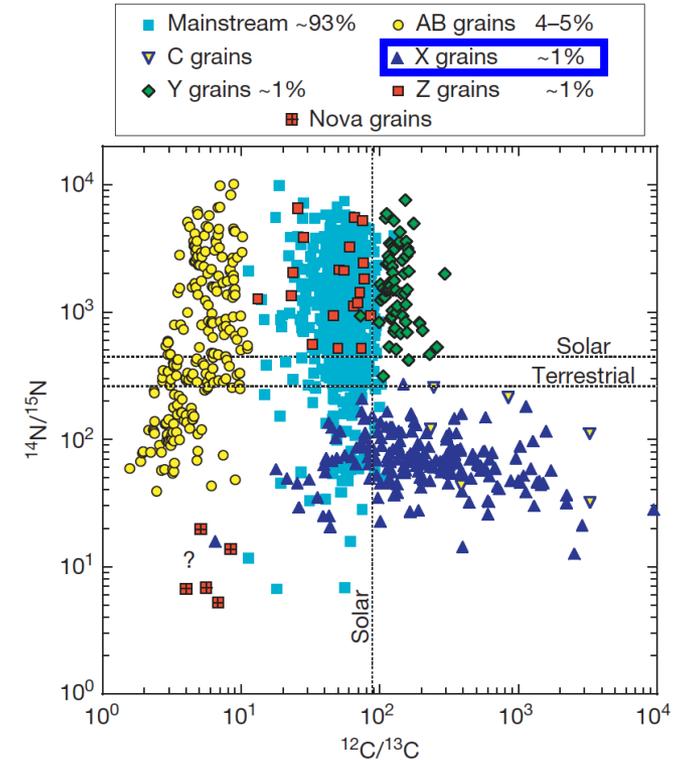
SiC grains:

- Fourth most abundant and one of the best-studied type of presolar grains
- Further divided into subgroups based on C, N, O & Si isotope ratios
- Most (93%) have C, N, O & Si isotope signatures consistent with TP-AGB stars → **mainstream grains**
- Just 1% have isotopic signatures consistent with explosive scenarios → **Type X grains**
- However, the light trans-Fe element composition (e.g. Zr, Mo, Ru) of Type X grains have so far defied a straightforward interpretation.

Pellin et al.: LPS (2006)



δ notation: permil deviation from S.S.



Zinner: Treatise on Geochemistry (2004)

Taking Mo as an example, rel. to ^{96}Mo :

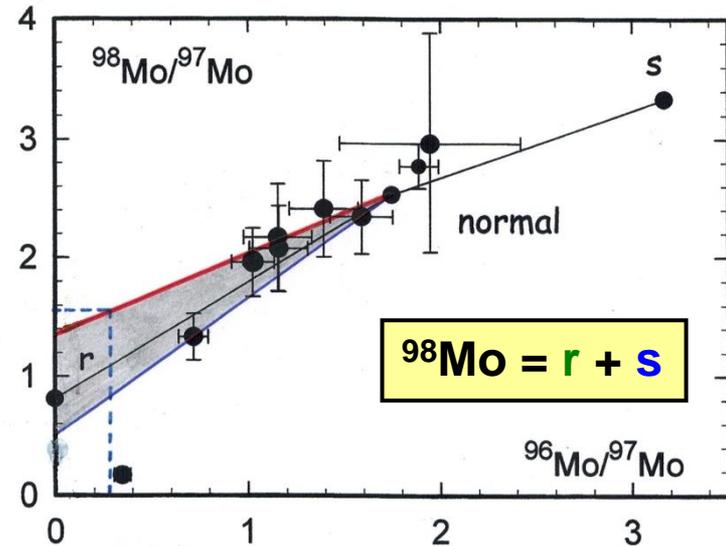
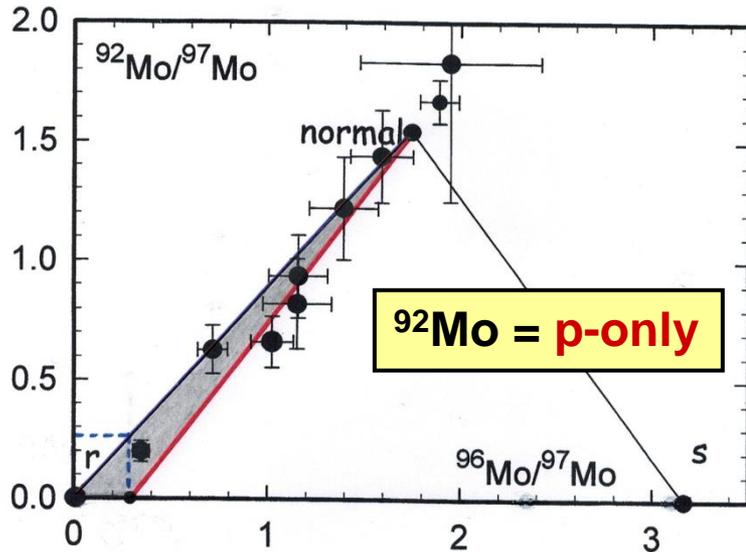
$^{92}, ^{94}\text{Mo}$ depleted

$^{95}, ^{97}, ^{98}\text{Mo}$ enriched

^{100}Mo approx. S.S.

“Clean” signature of ccSN–low-S component?

Cosmochemical Mo "three-isotope plots"



Ott, Kratz (2007)

Convention of cosmochemists:

"three-isotope plots"

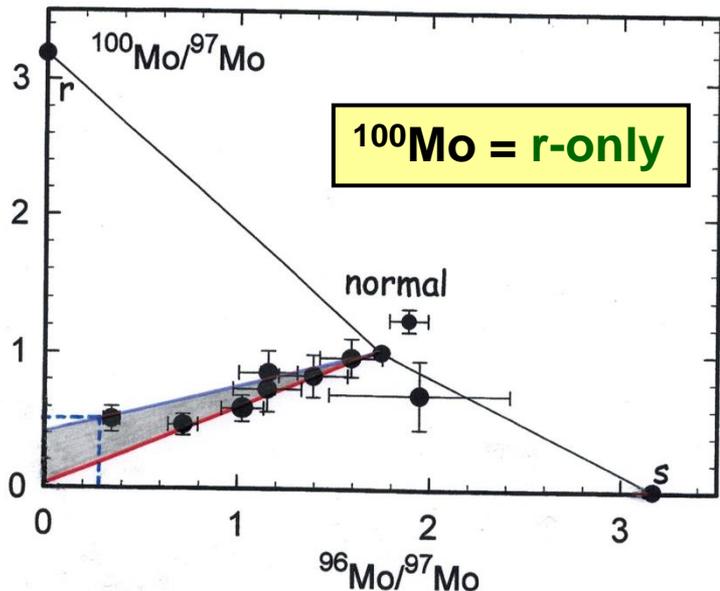
extrapolation of mixing lines with S.S.
yields **"clean"** nucleosynthesis signature

Here, S.S. data point **included** in mixing-line fits

X-axis: $^{96}\text{Mo} / ^{97}\text{Mo}$

Y-axis: $^X\text{Mo} / ^{97}\text{Mo}$

To be compared to model predictions:
definitely neither classical s nor r !



Comparison of Mo mixing-line results with model predictions

Astro-models (new analyses):

- "primary" **ccSN, HEW-CP**; $Y_e = 0.454 - 0.460$; $S_{\max} = 50 - 80$; $Y_n/Y_{\text{seed}} < 1$
- "secondary" **new n-burst**; Meyer (2018)

$x\text{Mo}/^{97}\text{Mo}$	Isotopic abundance ratios		
	SiC X-grains	This work	New "n-burst"
$^{92}\text{Mo}/^{97}\text{Mo}$	0.15	0.06	1.43 E-3
$^{94}\text{Mo}/^{97}\text{Mo}$	0.09	0.02	3.28 E-3
$^{95}\text{Mo}/^{97}\text{Mo}$	1.86	2.96	1.54
$^{96}\text{Mo}/^{97}\text{Mo}$	0.10	0.02	0.01
$^{98}\text{Mo}/^{97}\text{Mo}$	0.50	0.66	0.38
$^{100}\text{Mo}/^{97}\text{Mo}$	0.10	0.17	0.10
$^{92}\text{Mo}/^{94}\text{Mo}$	1.67	1.73	0.44 !

For $^{95}, ^{96}, ^{98}, ^{100}\text{Mo}/^{97}\text{Mo}$, HEW-CP and new n-burst yield similar results.

Not so for $^{92}, ^{94}\text{Mo}/^{97}\text{Mo}$ and $^{92}\text{Mo}/^{94}\text{Mo}$!

Comparison of Ru mixing-line results with model predictions

Astro-models (new analyses):

- "primary" **ccSN, HEW-CP**; $Y_e = 0.460 - 0.480$; $S_{\max} = 50 - 80$; $Y_n/Y_{\text{seed}} < 1$
- "secondary" **new n-burst**, Meyer (2018)

$x\text{Ru}/^{101}\text{Ru}$	Isotopic abundance ratios		
	SiC X-grains	This work	New "n-burst"
$^{96}\text{Ru}/^{101}\text{Ru}$	1.28	1.09	3.70 E-9
$^{98}\text{Ru}/^{101}\text{Ru}$	0.20	0.22	5.72 E-7
$^{99}\text{Ru}/^{101}\text{Ru}$	1.33	1.46	0.47
$^{100}\text{Ru}/^{101}\text{Ru}$	0.15	0.16	1.42 E-3
$^{102}\text{Ru}/^{101}\text{Ru}$	3.16	3.03	10.2
$^{104}\text{Ru}/^{101}\text{Ru}$	3.68	2.96	7.41

$^{96}\text{Ru}/^{98}\text{Ru}$

6.12

4.83

6.47 E-3 !

As for Mo, our HEW-CP results for Ru agree with measured grain data, whereas the **new n-burst clearly fails**.

Summary light trans-Fe isotopes

We find

- all historical p-, s- & r-isotopes in the light trans-Fe region (from ^{64}Zn to ^{104}Ru) co-produced in the **primary** CP component of a ccSN-HEW

As select example

- the ccSN-CP scenario can provide a consistent picture for all stable Zr, Mo and Ru isotopes in presolar SiC-X grains
- it can also reproduce the S.S. ratio of $^{92}\text{Mo}/^{94}\text{Mo} \approx 1.6$

“Clean” signature of low-S ccSN scenario

- from **“intercepts”** of SiC-X grain mixing lines

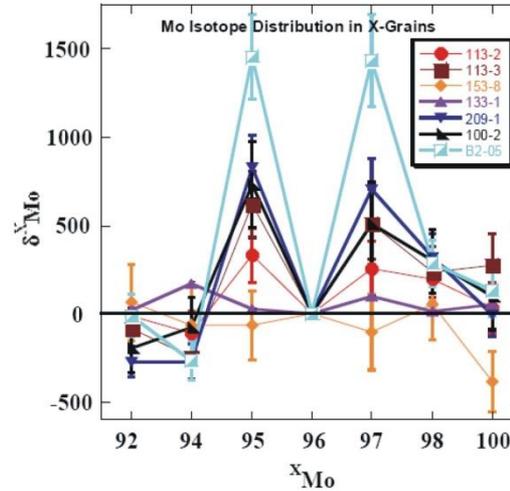
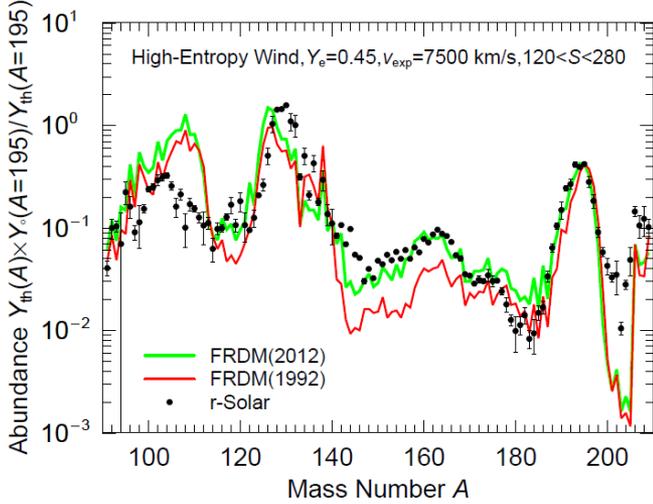
Main collaborators

W. Akram, K. Farouqi, O. Hallmann, U. Ott, B. Pfeiffer

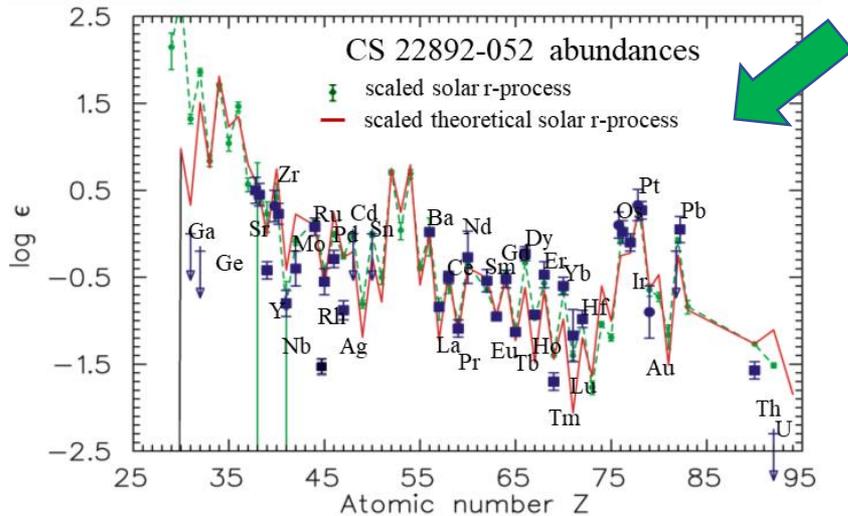
r-process observables today

Isotopic S.S.-abundances with better nuclear physics input

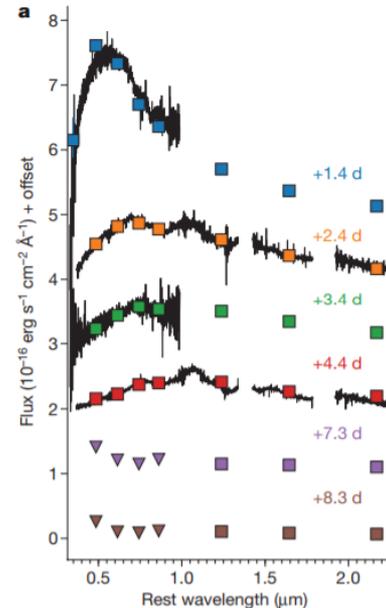
“FUN” anomalies in meteoritic samples and stardust



Presolar SiC grains; **isotopic** composition of Sr, Zr, Mo, Ru, Ba...



Elemental abundances in UMP halo stars



Neutron star merger event GW170817

kilonova AT2017gfo

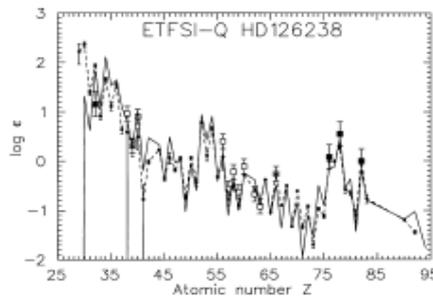
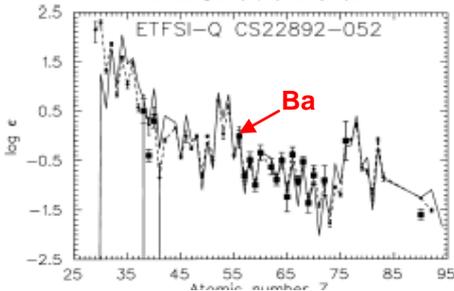
Early metal-poor halo stars (1999)

...our first involvement in UMP halo-star astronomy:

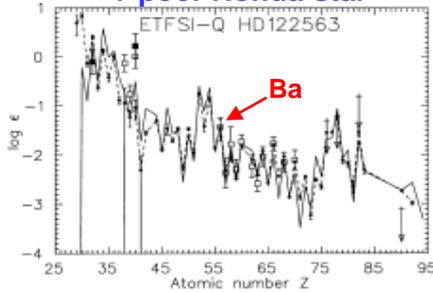
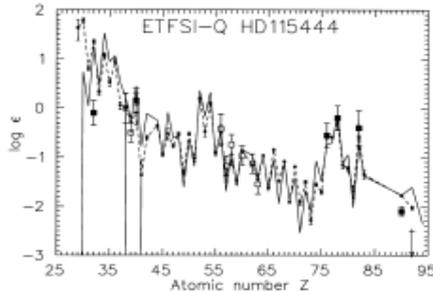
Cowan, Pfeiffer, Kratz, Thielemann, Sneden & Burles; ApJ 521 (1999)

“r-Process abundances and chronometers in metal-poor stars”

r-II Sneden-star



r-poor Honda-star



Comparison of observed abundances (filled squares) with $N_{r,\odot}$ (small filled circles, joined by a dashed line), and with $N_{r,calc}$ (solid line).

$[Fe/H] \leq -2$; $[Eu/Fe] \geq +1$; $[Ba/Eu] \leq -0.7$

Standard spectroscopic notation:

$$[A/B] \equiv \log(N_A/N_B)_{star} - \log(N_A/N_B)_{\odot}$$

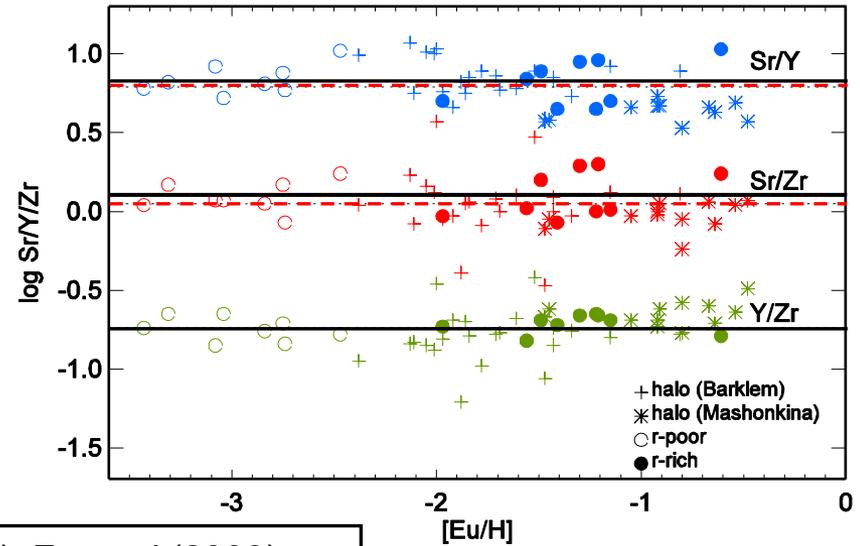
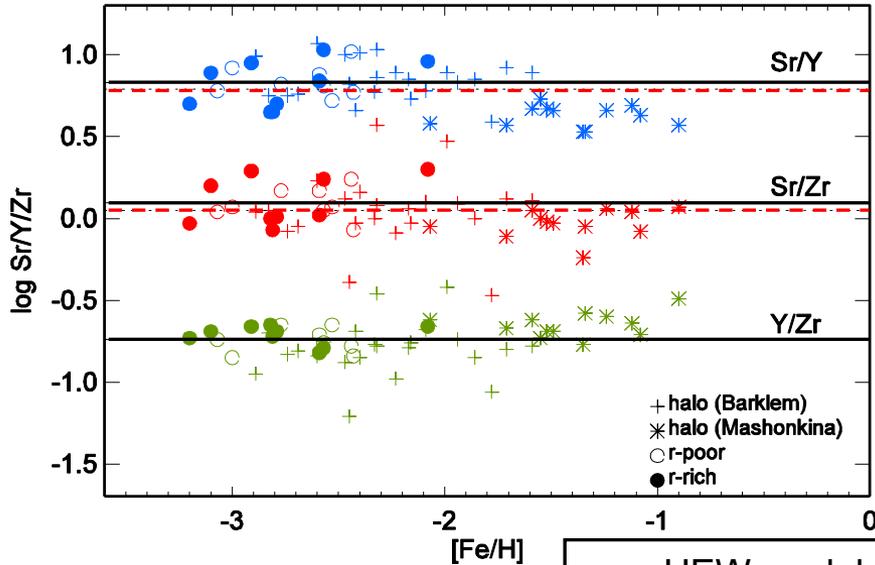
Conclusions at that time (!) :

The abundance comparisons indicate several striking results:

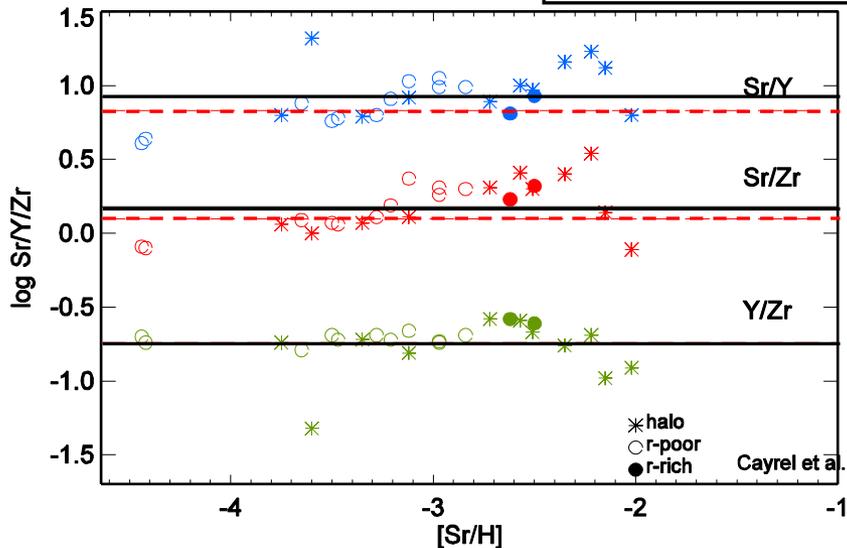
- Halo stars with $-1.7 \leq [Fe/H] \leq -3.1$ show the same S.S.-r pattern for $Z \geq 56$;
↻ in each hypothetical r-process site a continuous set of conditions.
- For $Z \geq 56$, the r-abundances seem not to have changed with GCE;
↻ one r-process site (later denoted as “main” r-process).
- The trend of the lighter n-capture elements is unclear; explainable in terms of metallicity dependent weak s-process?
- Or..., there are two r-process signatures (weak & main) reflecting different sites

- First comparison with theoretical predictions: WP and HEW

Halo stars vs. HEW model: Sr/Y/Zr as fct. of [Fe/H], [Eu/H] and [Sr/H]



— HEW model ($S \geq 10$); Farouqi (2009)
 - - - average halo stars; Mashonkina (2009)



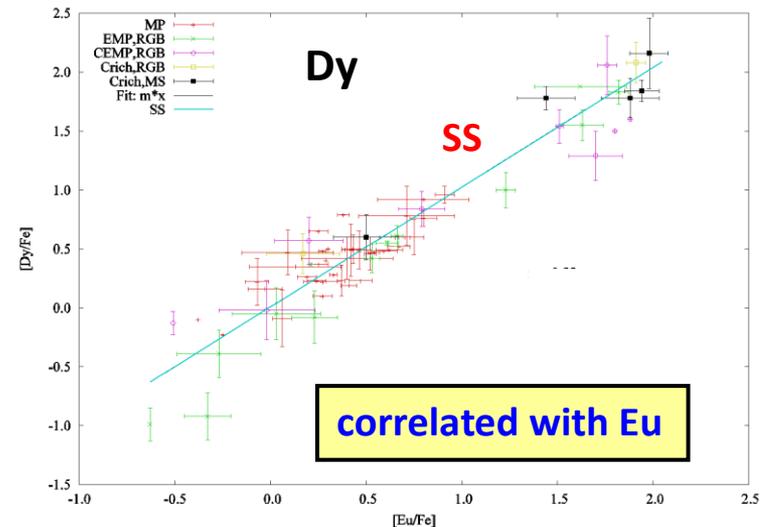
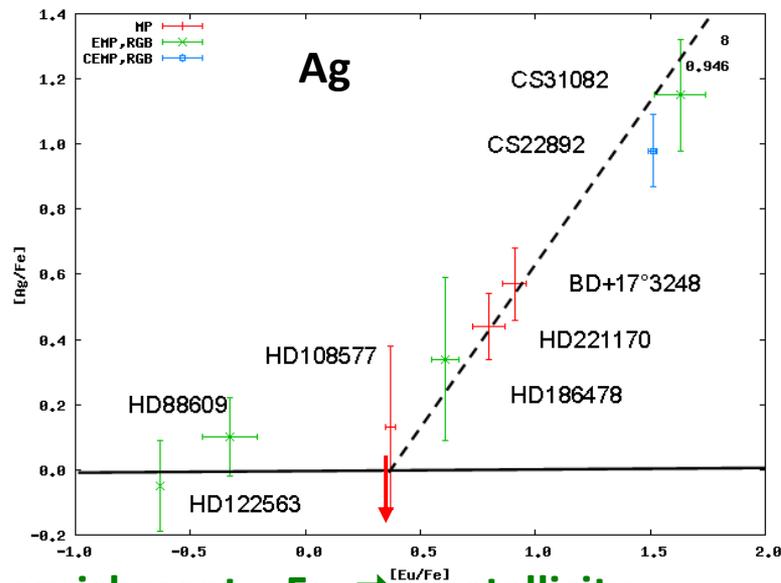
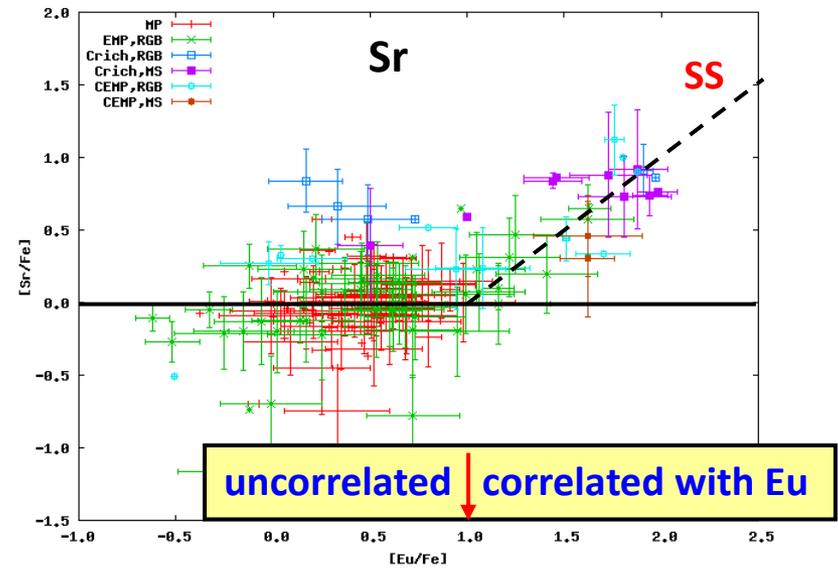
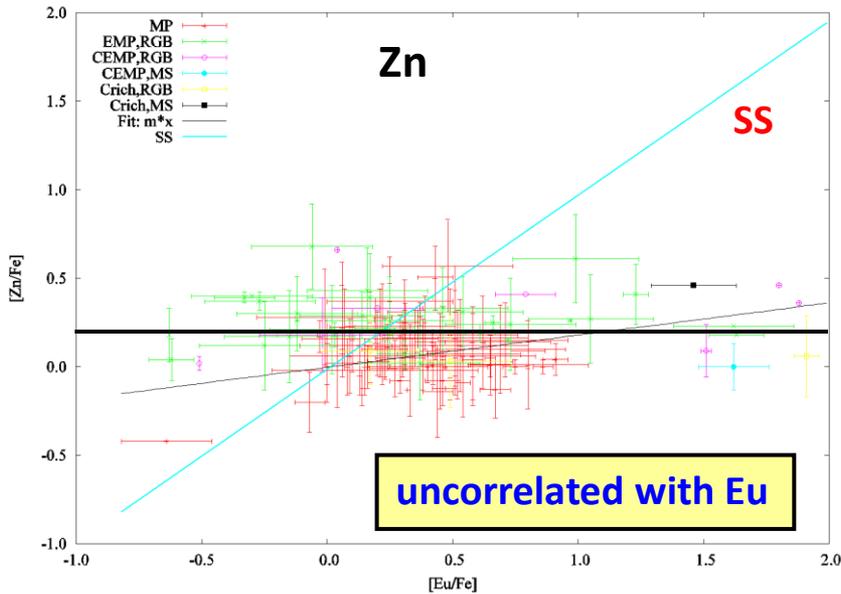
Robust Sr/Y/Zr abundance ratios,
independent of metallicity,
r-enrichment,
 α -enrichment.

↪ Same nucleosynthesis component:
CP-process, NOT n-capture r-process

Correlation with main r-process (Eu) ?

Astronomical observations, SAGA database: [X/Fe] vs. [Eu/Fe]

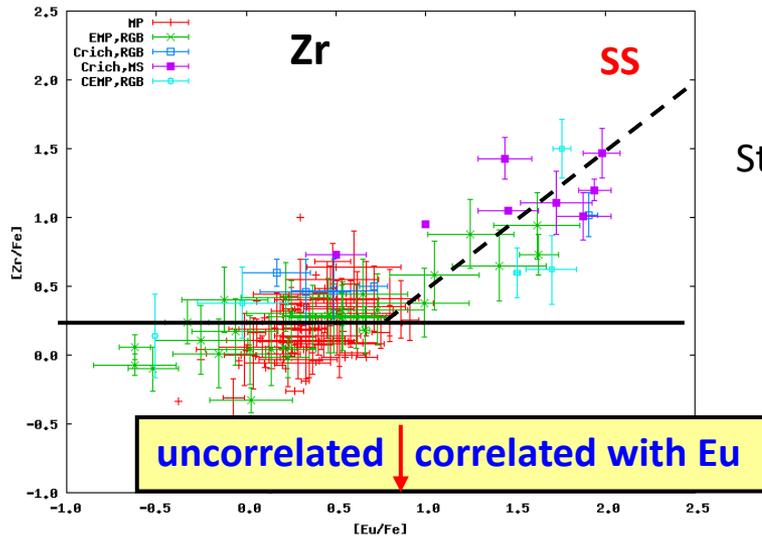
Transition from CP-r component via “weak” to “main” n-capture r-process



Eu \Rightarrow r-enrichment; Fe \Rightarrow metallicity

$$[A/B] = \log(N_A/N_B)_* - \log(N_A/N_B)_\odot$$

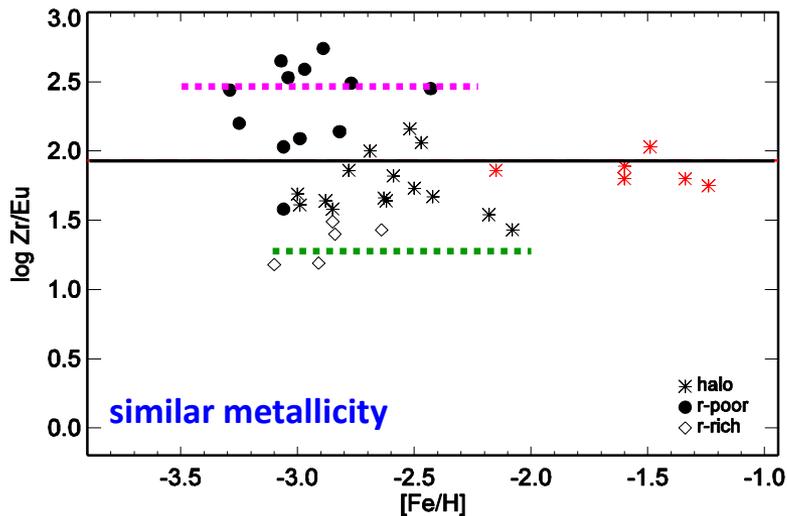
SAGA database: Zr in more detail



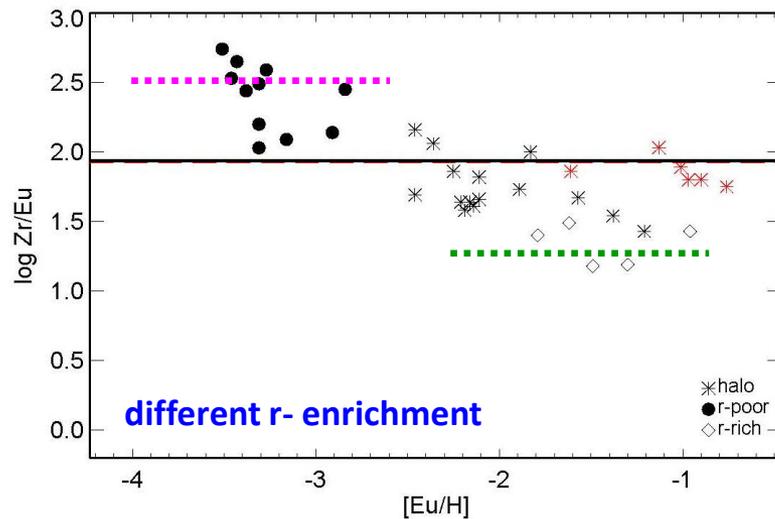
Strong Zr – Eu correlation
 ↷ SS diagonal

Zr in r-poor halo stars **overabundant**
 ↷ type “Honda star”
 Zr in r-rich halo stars **underabundant**
 ↷ type “Snedden star”

Mashonkina (2009); Farouqi (2009)



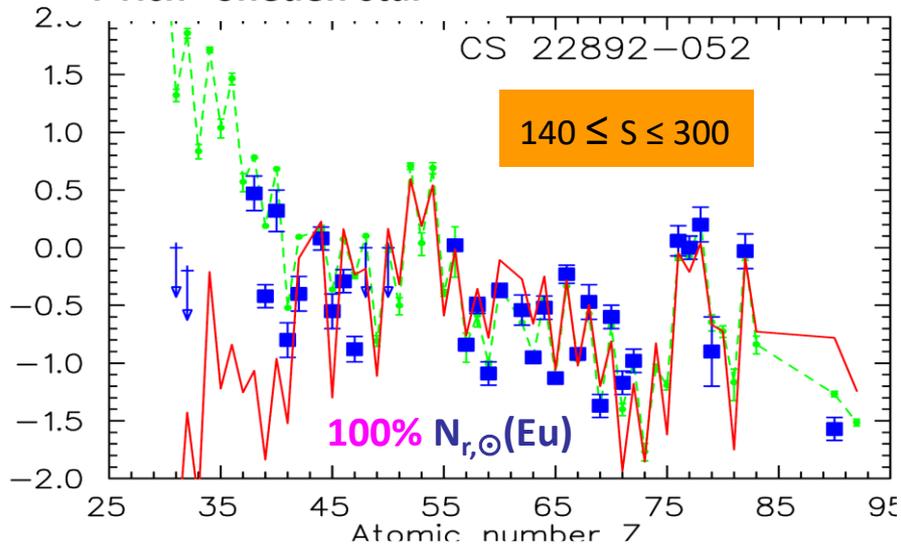
r-poor
 HEW (av.)
 r-rich



Clear differences observed already a decade ago...
 However, today's r-process consequences not fully understood

Extremes “r-rich” and “r-poor”: S-range optimized

r-rich “Sneden star”



full main r-process

Sr – Ag region **underabundant** by a mean factor ≈ 2 relative to $N_{r,\odot}$

$[\text{Eu}/\text{Fe}] = 1.52$; $[\text{Sr}/\text{Fe}] = 0.73$;

Sr/Eu = 26

(assumption by Travaglio et al. that this pattern is unique for all UMP halo stars)

➔ **missing part to $N_{r,\odot} = \text{“LEPP”}$**

incomplete main r-process

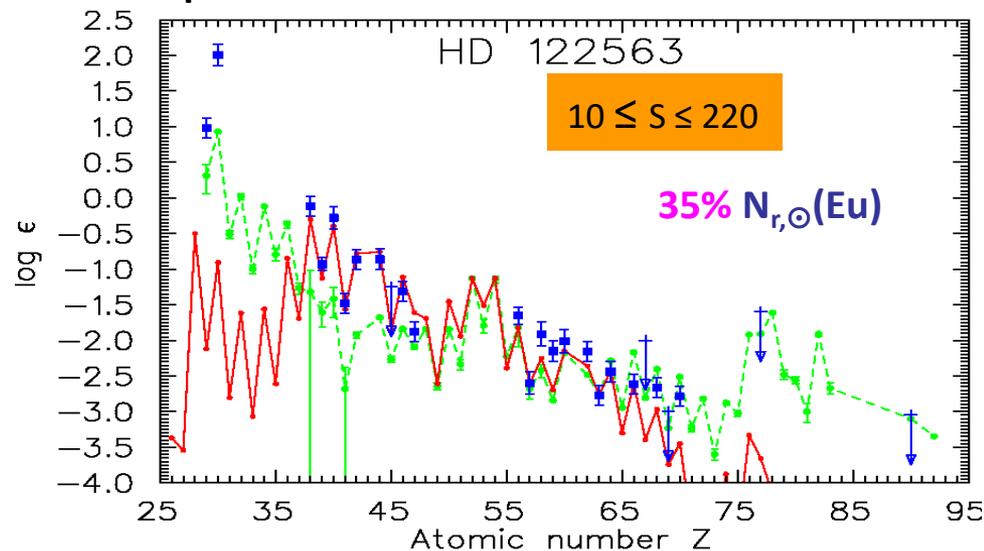
Sr – Cd region **overabundant** by a mean factor ≈ 10 relative to $N_{r,\odot}$

$[\text{Eu}/\text{Fe}] = -0.64$; $[\text{Sr}/\text{Fe}] = -0.27$;

Sr/Eu = 447

➔ **missing part to $N_{r,\odot} = \text{“HEPP”}$**
(today, NSM r-component)

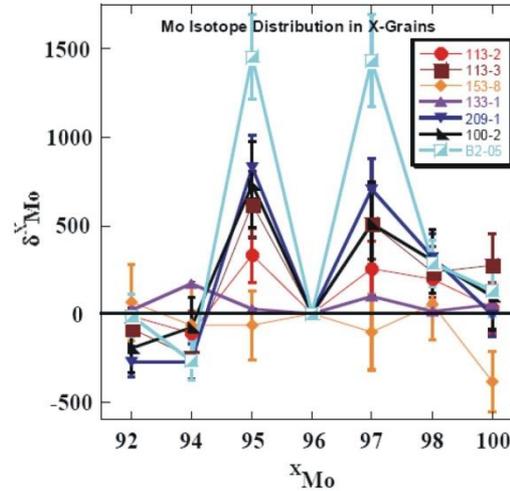
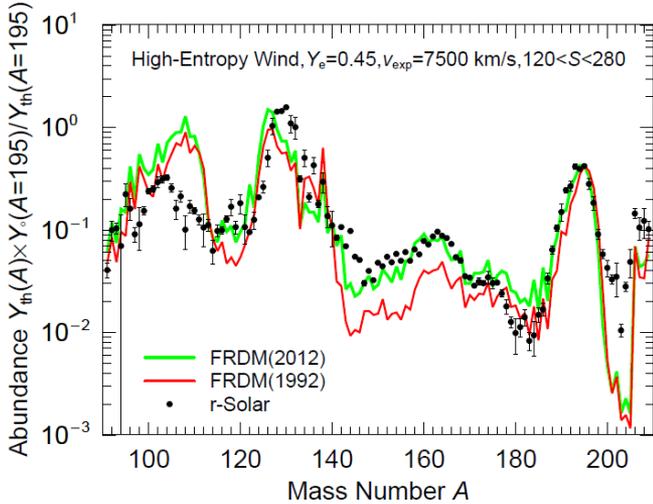
r-poor “Honda star”



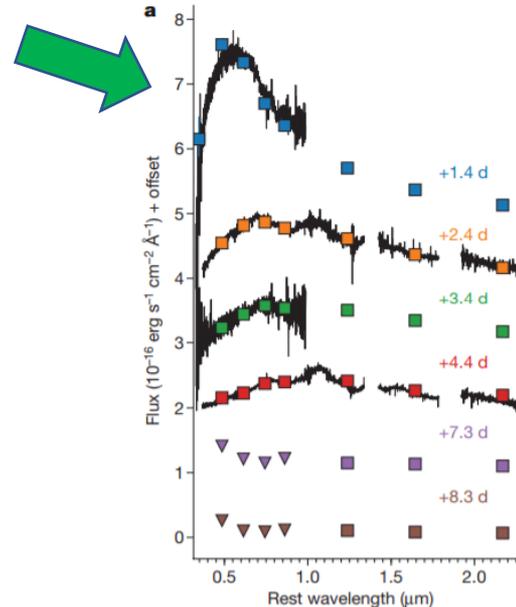
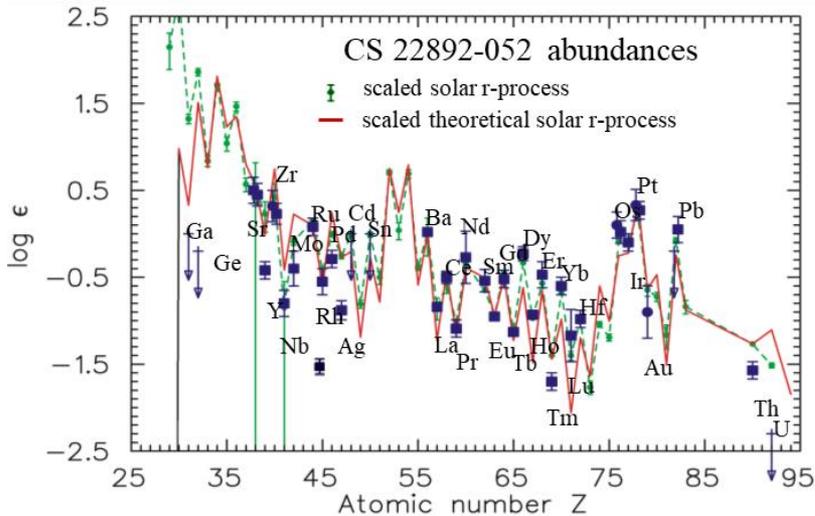
r-process observables today

Isotopic S.S.-abundances with better nuclear physics input

“FUN” anomalies in meteoritic samples and stardust



Presolar SiC grains;
isotopic composition of Sr, Zr, Mo, Ru, Ba...



Neutron star merger event GW170817

kilonova AT2017gfo

Elemental abundances in UMP halo stars

The Multimessenger Era → GW – NSM – Kilonovae (I)

Prediction NSM as promising r-process site **Lattimer & Schramm ApJ 213 (1974)**

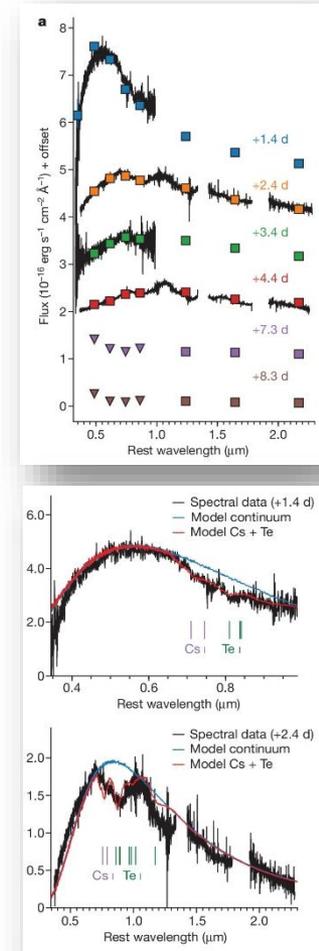
Over many years considered „exotic“, e.g. because the extreme gravity makes it difficult to eject possible r-process matter.

August 2017

- r-process nucleosynthesis in NSM in the multiwave follow-up observations of **kilonova / gravitational wave, GRB 170807A / GW 170817**
- **LIGO & VIRGO** ↪ GW (Tanvir et al., APJL 847; Abbott et al., PRL 119)
- **Fermi-GBM & INTEGRAL/SPI** ↪ γ -burst signal (Goldstein et al., ApJL 848; Savchenko et al., ApJL 848)
- **GROND** ↪ electromagn. Signal = **kilonova** spectrum peaked in infrared region → heavy elements (Ba & lanthanides)

From Kajino et al.

Prog. Part. & Nucl. Phys. 107 (2019)

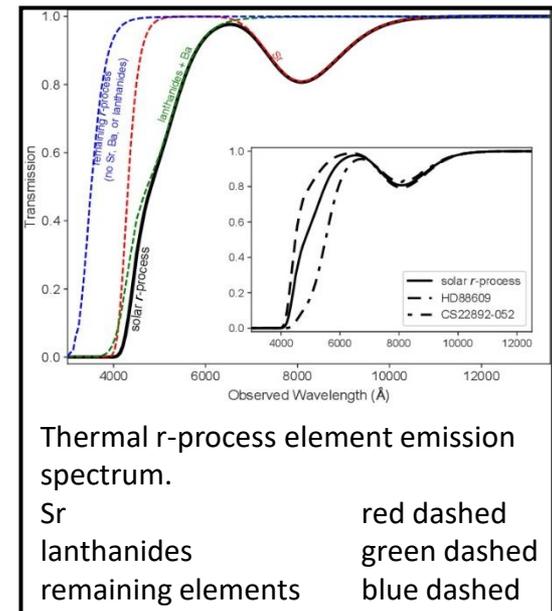
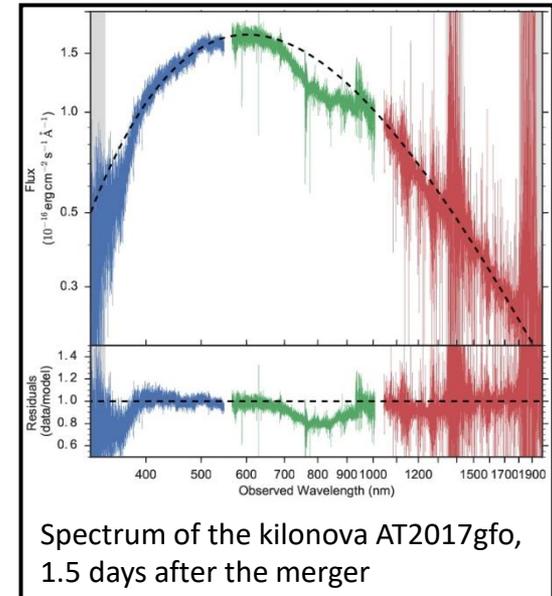


The Multimessenger Era – Identifications of Sr (II)

D. Watson et al., Nature 574 (2019)

- $Z = 38$, $N = 88$ **Sr** identified as first individual element from electromagnetic radiation of a NSM
- NSM ejecta with $Y_e \leq 0.1$ \curvearrowright heavy r-elements; increase of Y_e by weak interactions (changes of n to p) to eject the light r-elements
- Expanding material diluted – only after a few days „**red** wavelength emission“ of Ba & lanthanides. Lighter elements – at higher Y_e - visible earlier as „**blue** wavelength emission“

From S. Rosswog
Physik Journal 19 (2020)



UMP halo-stars – observations vs. calculations

Abundance ratio CP-r Sr / main-r Eu

- Lodders (2009); Bisterzo (2014); Trippella (2016)

$$N_{\odot} - N_{s,\odot} \approx N_{r,\odot} \text{ “residuals” } \curvearrowright (\text{Sr/Eu}) \approx 45$$

- Farouqi (2010)

$$\text{ccSN-HEW, } Y_e = 0.45 \quad \curvearrowright (\text{Sr/Eu}) \approx 115$$

- T. Hansen et al. (2018)

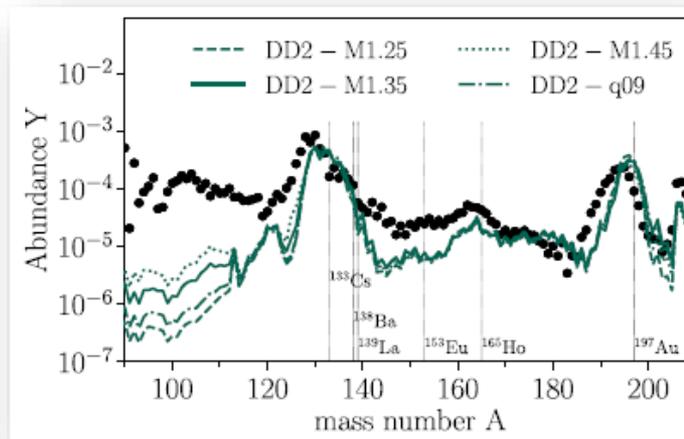
“The r-process alliance”

r-poor stars	$[\text{Eu}/\text{Fe}] < 0.3$	$(\text{Sr}/\text{Eu})_{\text{max}} \approx 780$	indicates ccSN
r-I stars	$0.3 < [\text{Eu}/\text{Fe}] < 1.0$	$(\text{Sr}/\text{Eu})_{\text{av}} \approx 45$	S.S.-r blend
r-II stars	$[\text{Eu}/\text{Fe}] > 1.0$	$(\text{Sr}/\text{Eu})_{\text{min}} \approx 2$	indicates NSM

- Bovard et al. (2017)

rel. r-abundances for diff. NSM models

$$(\text{Sr}/\text{Eu}) \approx 10^{-2} - 10^{-1}$$



Important question: where “clean” signatures for ccSN and NSM?

Relative r-process contributions of ccSN, MHDJet-SN & NSM

Farouqi, Kratz et al. (2010, 2019)

halo-star obs. & ejected r-matter as fct. Y_e

- ≈ **90 %** r-poor (Honda-type) stars
- ≈ **8 %** r-rich (Snedden-type) stars
- ≈ **2 %** r-strong (actinide-boost) stars

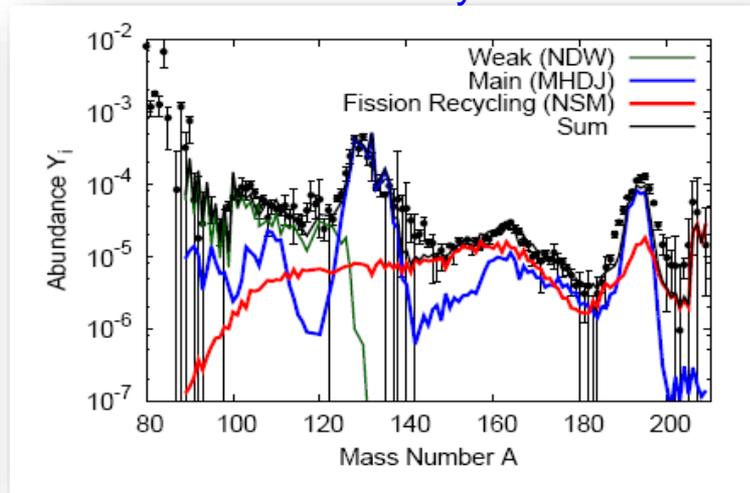
Wehmeyer, Pignatari & Thielemann (2015)

acc. to their GCE understanding

- ≈ **98 %** cc-SN (light r-elements)
- ≈ **1 %** Jet-SN (full r-process)
- ≈ **1 %** NSM (main r-process)

Shibagaki, Kajino et al. (2015)

fit of S.S.-r distribution by fractions of



- ≈ **79 %** HEW (weak r-process)
- ≈ **18 %** MHDJ (main r-process)
- ≈ **3 %** NSM (fission-recycling r-process)

...unfortunately, with highly questionable nuclear-physics input!

Ji & Frebel (2018)

acc. to estimated event production

- only **1 NSM** every ≈ **2000 ccSNe**;
- however, admittedly much lower than currently inferred rates based on Abbott et al. (2017) & Taylor et al. (2014) of ≈ **1/100**

Correlation of r-process elements in VMP halo stars

When Khalil Farouqi and I started in 2018, our main goal was to distinguish between

- r-elements **correlated** (co-produced?) with Fe, and
- r-elements **uncorrelated** (not produced?) with Fe

In contrast to the numerous model-speculation papers after the GW-NSM event, our approach primarily based on experimental “facts”:
databases for UMP halostars SAGA (and JINAbase); $[\text{Fe}/\text{H}] \leq -2.5$

Choice of 3 “typical” r-elements:

- $Z = 38$ Sr  classical “**weak-r**” element \rightarrow SN-type ?
- $Z = 63$ Eu  classical “**main-r**” element \rightarrow Merger-type ?
- $Z = 90$ Th  classical “**actinide-boost**” \rightarrow Merger-type ?

Choice of “typical” r-parameters:

- $[\text{Eu}/\text{Fe}]$  “r-enrichment” \rightarrow historical stellar classes r-poor, r-I, r-II
- (Sr/Eu)  “**weak-r**”/“**main-r**” \rightarrow indication of fractions SN & Merger ?
 \rightarrow indication of “pure” SN and/or Merger signatures ?
 \rightarrow correlation with metallicity $[\text{Fe}/\text{H}]$?

Combination of exp. “facts” with statistical-model correlation coefficients **SCC** & **PCC**

SAGA database: [Fe/H] mean & (Sr/Eu) mean as function of [Eu/Fe]

What do we learn from the astronomical observations (facts!) ?

[Eu/Fe] range	No. stars	[Fe/H] mean	(Sr/Eu) mean	Stellar classes
- 0.65 to - 0.3	11	- 3.09	399	“r-poor” e.g. Honda-star HD122563
- 0.3 to 0	34	- 2.92	278	
0 to 0.2	45	- 2.90	207	
0.2 to 0.4	34	- 2.85	140	“r-I” e.g. Westin-star HD115444
0.4 to 0.6	37	- 2.71	106	
0.6 to 0.8	28	- 2.80	70	
0.8 to 1.0	23	- 2.81	57	“r-II” e.g. Sneden-star CS22892-052
1.0 to 1.4	22	- 2.90	39	
1.4 to 1.95	24	- 2.79	30	

- **With increasing [Fe / H]**
 - increasing r-process enrichment
 - decreasing (Sr/Eu) ratio

- **Indication of**
 - different r-process sites
 - different galactic times for r-sites
 - different frequencies of r-sites (?)
 - different r-matter ejecta (?)

From observations to mathematical correlations



Spearman & **Pearson**
correlation coefficients

J. Hauke & T. Kosowski; Questiones Geographicae (2011)

Correlations between “variables” can be measured with the use of different indices (coefficients); among the most popular are:

- Spearman (rank) correlation coefficient (SCC)
- Pearson correlation coefficient (PCC)

Spearman’s “rho”

- is a non-parametric (distribution-free) rank-statistic
- is a measure of monotone association of variables in a somewhat „**qualitative**“ way
- does not require the assumption that the relationship between the variables is linear
- does not require the variables to be measured on interval scales

Pearson’s product-moment correlation coefficient

- treats data in a “**quantitative**“ way
- assumes the normality of the variables
- is a measure of the linear association of variables
- prefers data variance to be homogeneous (“homoscedascity“)
- requires that no outliers be present in the data

Astronomy & Astrophysics manuscript no. rProcessCorrelation
July 9, 2021

©ESO 2021

arXiv:2107.03486v1 7 Jul 2021

Correlations of r-Process Elements in Very Metal-Poor Stars as Clues to their Nucleosynthesis Sites

K. Farouqi¹, F-K. Thielemann^{2,3}, S. Rosswog⁴ and K.-L. Kratz^{5,6}

Accepted for publication by *Astronomy and Astrophysics* in January 2022

Possible r-process sites

Single stars

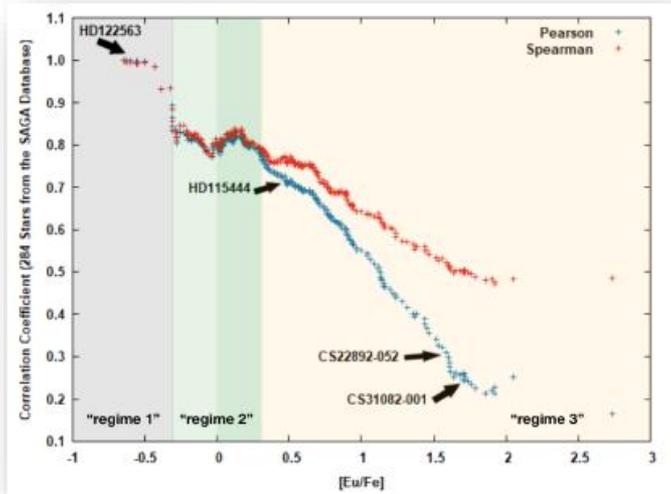
Astrophys. site	r-ejecta/event	frequency
Regular ccSNe	weak	high
QD-SNe	weak	low
MHD-Sne	from weak to strong (?)	medium
EC-SNe	very weak	uncertain (!)
Collapsars / Hypernovae	strong (?)	low

Compact binary mergers

Event type	r-ejecta/event	frequency
NS-NS	strong	low
BH + torus		
mass. NS + torus		
NS-BH	strong	low

Example of PCC & SCC for r-element correlations

PCC and SCC for Eu (r-enrichment) and Fe metallicity) for halo-stars with $[Fe/H] \leq -2.5$



Our 4 “typical” stars:

- 1) HD122563, **Honda-star**, r-poor / incomplete-r
- 2) HD115444, **Westin-star**, complete r-I
- 3) CS22892, **Snedden-star**, complete r-II
- 4) CS3108-001, **Cayrel-star**, complete r-II & actinide boost

...at $[Eu/Fe] \approx 0.3$ PCC & SCC begin to diverge from each other. At this point the CC ≈ 0.75 is still high. Fe and Eu are well correlated / co-produced (?)

PCCs for $[Eu/Fe] > 0.3$ weak(er) correlation several contributors, e.g. SNe and NSM

Star-Type	[Eu/Fe]	PCC	strength	No. stars
all stars	- 0.64 – 1.9	0.14	very weak	282
r-I + r-II	0.3 – 1.9	0.15	very weak	166
r-II	> 1.0	0.34	moderate	51
r-I	0.3 – 1.0	0.65	strong	115
r-poor	< 0.3	0.83	very strong	168

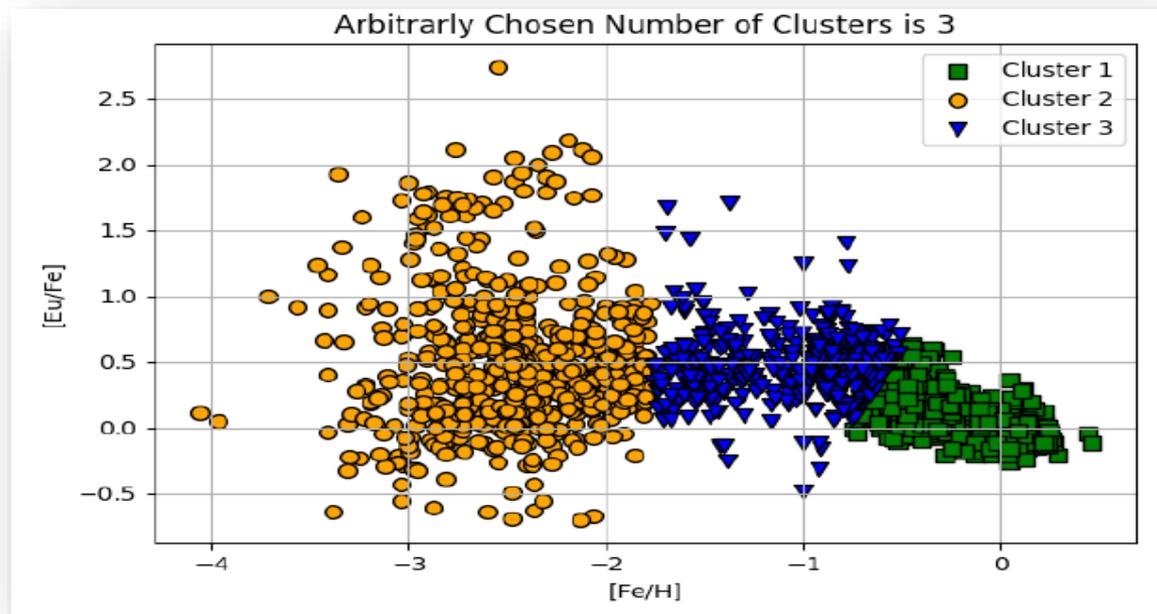
Cluster analysis techniques

Cluster analysis

... a statistical technique to group data with common characteristics; however without explanation, why the clustering exists. Typically used in the exploratory phase of a research project with the aim to guide further analyses.

K-means clustering

... treats observations in data as objects having locations & distances from each other. Each cluster is characterized by its mean or central point.

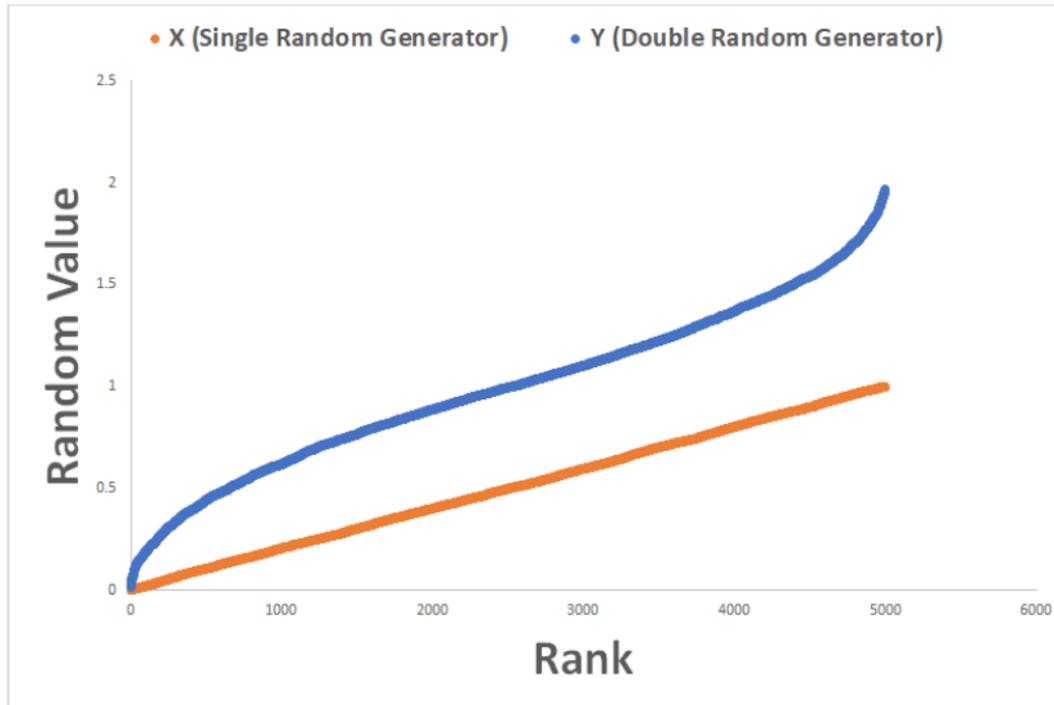


In the **3-Cluster Analysis** of [Eu/Fe] vs. [Fe/H] one can recognize:

- (1) for low-metallicity stars ($[\text{Fe}/\text{H}] < -2$) with large scatter ($\approx 10^3$) \rightarrow contributions from **individual rare** or **different events**;
- (2) for $-2 < [\text{Fe}/\text{H}] < -1.5$ with already small scatter \rightarrow **averaging / mixing** of events;
- (3) for $[\text{Fe}/\text{H}] > -1.5$ \rightarrow additional Fe-contribution from **SN-Ia**

Rank tests

- ... usually applied to abundance observations of individual elements as function of “rank”
- ➔ indicates whether only **one** nucleosynthesis source, or **several** contributed to the element



Orange curve:

a **single** random-number operator X, ordering values according to their size, giving them integer entries (“ranks”)

⇒ linear relation between random numbers and ranks

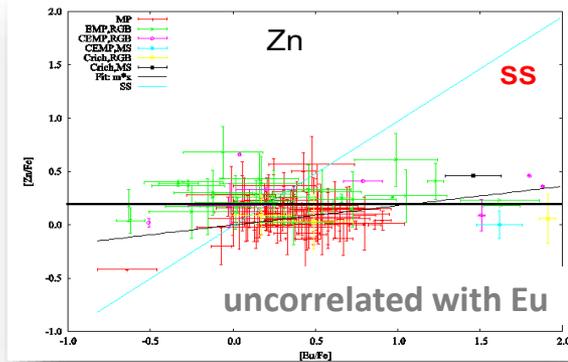
Blue curve:

two random-number generators, adding their values $X_1 + X_2 = Y$; plotted as function of its ranks

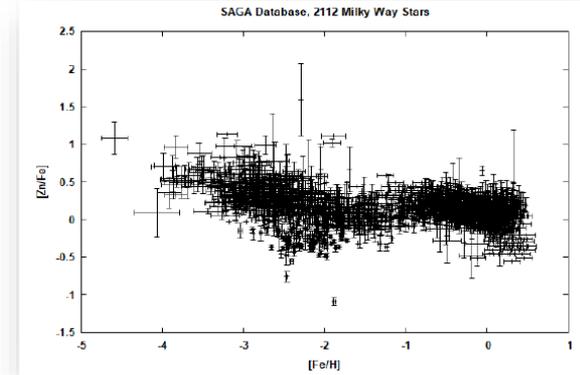
⇒ deviation from a linear relation between Y and its ranks

Zn vs. Fe & Eu: 2008 and today

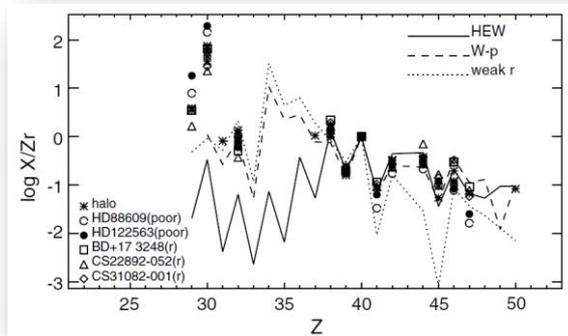
Kratz et al., New Astron.Rev. 52 (2008)
based on the SAGA data at that time



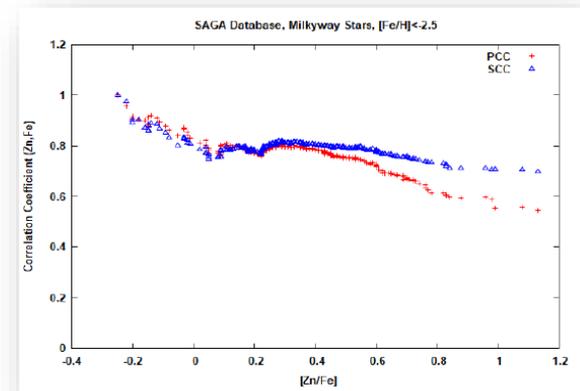
Farouqi et al., arXiv: 2107.03486 (2021)
based on today's SAGA data



... the rise of $[Zn/Fe]$ below $[Fe/H] < -2$ points to an additional event to ccSNe \rightarrow alpha-rich freeze-out of hypernovae/collapsars

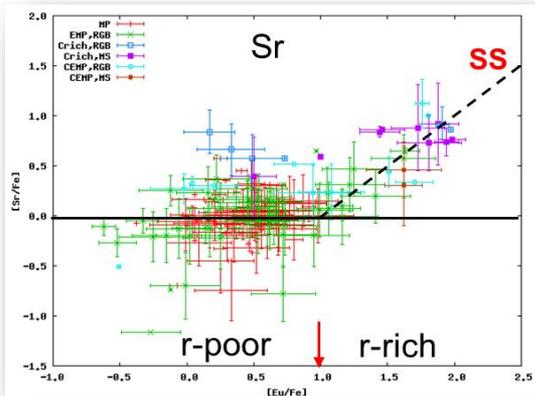


... the minimal conclusion to be drawn right now is that the high abundances of Cu ($Z=29$) and Zn ($Z=30$) are not produced together with the $Z \geq 38$ (Sr-Ag) elements



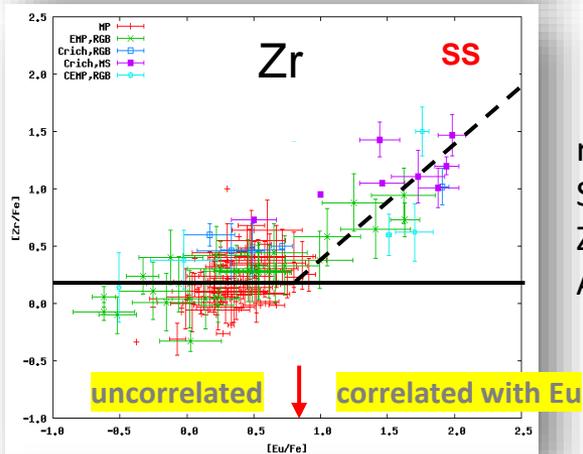
... consistent with decrease of PCCs for high $[Zn/Fe] \geq 0.3 \rightarrow$ high Zn not necessarily from regular ccSNe

Sr, Zr → Ag vs. Fe & Eu: 2008 and 2021

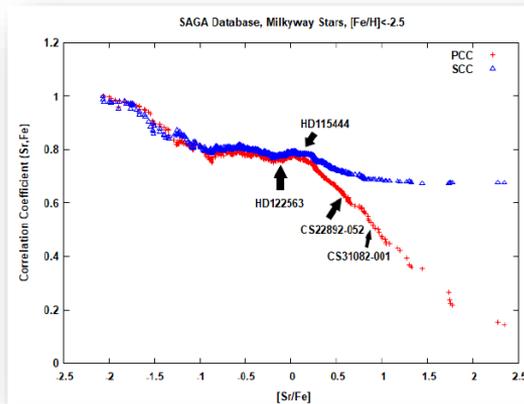
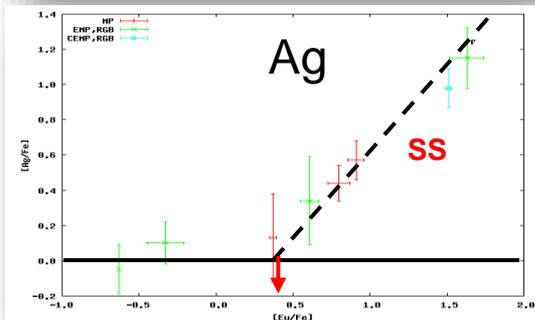


2008

partial correlation with
“main-r” Eu;
from (Z=38) Sr on,
increasing fractions of
“main-r” material

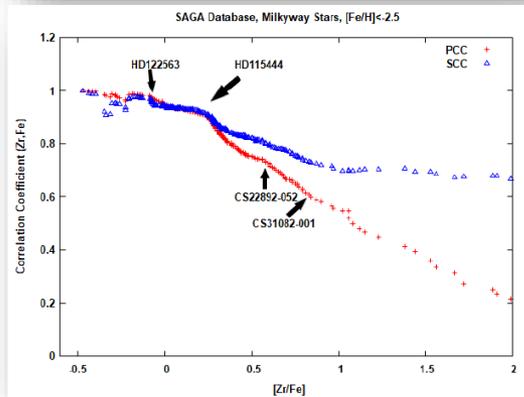


r-poor/r-rich “cuts”:
Sr - [Eu/Fe] ≈ 1.0
Zr - [Eu/Fe] ≈ 0.8
Ag - [Eu/Fe] ≈ 0.4



today

SCC & PCC
of Fe for Sr and Zr
in stars with [Fe/H]
< -2.5



SCC / PCC „cuts“
Sr - [Sr/Fe] ≈ 0.1
Zr - [Zr/Fe] ≈ 0.25

Correlation coefficients (X/Fe) **high** for r-poor and
r-I → **SNe**

low for r-II → **Mergers**

Selected r-poor & r-I halo stars: Comparison of data with Fe-Sr-Eu correlations

What do we learn from comparison of astronomical **observations** with r-element **correlations** ?

Stellar ID	[Eu/Fe]	[Fe/H]	(Sr/Eu)	%Sr with Fe	%Eu with Fe	%Sr w/o Fe	%Eu w/o Fe
HD 122563	-0.64	-2.53	589	100	100	0	0
HE 0048-6408	-0.50	-3.75	107	100	100	0	0
BD - 185550	-0.21	-3.06	40	100	100	0	0
CS 22897-008	-0.03	-3.83	1122	100	100	0	0
CS 22891-209	0.10	-3.49	759	100	100	0	0
HE 0139-2826	0.21	-3.46	4.3	100	100	0	0
CS 22190-007	0.33	-2.57	170	80	51	20	49
CS 22955-174	0.35	-3.10	251	100	80	0	20
CS 22879-029	0.59	-2.55	562	15	34	85	66
HD 115444	0.68	-2.84	56	100	46	0	54
HE 2158-0348	0.79	-2.71	155	48	33	52	67

“r-poor”

“r-I”

“r-poor” stars

- lowest metallicity $[\text{Fe}/\text{H}]_{\text{av}} \approx -2.93$
early in galaxy
- large scatter (Sr/Eu), min. 40; max. 1122
- Sr & Eu completely correlated with Fe

“pure” SN signature

“r-I” stars

- slightly higher $[\text{Fe}/\text{H}]_{\text{av}} \approx -2.78$
- again, large scatter (Sr/Eu), min. 4.3; max. 562
- Sr still predominantly correlated with Fe (90%);
Eu \approx 60% correlated with Fe

“blends” of SN & NSM

Selected r-I & r-II halo stars: Comparison of data with PCC & SCC

Again – what can we learn?

Stellar ID	[Eu/Fe]	[Fe/H]	(Sr/Eu)	%Sr with Fe	%Eu with Fe	%Sr w/o Fe	%Eu w/o Fe
CS 22190-007	0.33	-2.57	170	80	51	20	49
CS 22879-029	0.59	-2.55	562	15	34	85	66
HD 115444	0.68	-2.84	56	100	46	0	54
CS 22875-029	0.92	-2.69	191	29	25	71	75
HE 0336+0113	1.22	-2.73	776	4	15	96	85
CS 22892-052	1.53	-2.91	25	84	14	16	86
* CD -24_17504	1.37	-3.19	0.54	100	27	0	73
* CD -27_14351	1.71	-2.63	240	3.4	4.3	97	96
CS 31082-001	1.72	-2.79	7.9	93	5.9	7.0	94
HE 0243-3044	1.92	-2.58	26	17	2.5	83	97

“r-I”

“r-II”

“r-I” stars

- 90% Sr correlated with Fe
- 60% Eu correlated with Fe
- “blends” of SN & Merger

“r-II” stars

[Fe/H] av. \approx -2.78, similar to r-I

74 % Sr corr. with Fe \rightarrow SN

77 % Eu uncorr. with Fe \rightarrow Merger

CD-27_14351 „clean“ NSM with low [Fe/H]

CD-24_17504 no Sr from NSM-HEW

Deconvolution of Sr & Eu from SNe and Mergers

Example: r-II **Sneden star** (CS22892-052) $[\text{Eu}/\text{Fe}] = 1.53$
 $(\text{Sr}/\text{Eu}) = 25$

84% Sr & 14% Eu correlated with Fe \Rightarrow **SNe**

16% Sr & 86% Eu uncorrelated with Fe \Rightarrow **Mergers**

↪ „clean“ **SN** part $(\text{Sr}/\text{Eu}) \approx 147$
„clean“ **Merger** part $(\text{Sr}/\text{Eu}) \approx 4.6$

↪ „clean“ **SN** part $[\text{Eu}/\text{Fe}] \approx 0.30$
„clean“ **Merger** part $[\text{Eu}/\text{Fe}] \approx 1.46$

... rough estimate: „Sneden-star Merger“ contaminated by 6 SNe

Near future: similar analyses for „typical“
r-I, r-II and actinide-boost stars

Summary based on astronomical “facts”

- First indications of different r-process types & sites, **already more than a decade ago**
- Statistical analyses (PCC, SCC ranks, K-means clusters) confirm the old ideas; improvements from qualitative to quantitative
- To understand the total abundance pattern (from Sr to Th) of **S.S.-r „blend“**, in addition to Merger-type contributions, also sizeable fractions of SN-types required;

e.g. $\approx 90\%$ S.S.-r Strontium
 $\approx 50\%$ S.S.-r Europium } from SNe

Summary based on nucleosynthesis models

Six decades of r-process nucleosynthesis research:

From a secondary process with Fe-seed in SN-I (B²FH, Cameron, Coryell) to a primary process in SN-II to the present „multi-scenarios“.

