

The  
formation of  
super-massive black holes  
and  
on the (probable?) very rapid initial  
metal & r-process enrichment

2nd lecture

17th Russbach School  
14-19 March 2022

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For recent progress on cosmology  
and  
the existence of dark matter particles  
(for those interested)

*"Dark Matter Kindergarten Stuff"*

<https://www.youtube.com/watch?v=O5MbOCgCMDs>

# Comment

This project was published  
*prior*  
to the  
black-hole Nobel Prize of 2020.

That is, there is no influence / corruption whatsoever of  
this project by that event.

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Based on :

Monthly Notices

of the

ROYAL ASTRONOMICAL SOCIETY



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## Very high redshift quasars and the rapid emergence of supermassive black holes

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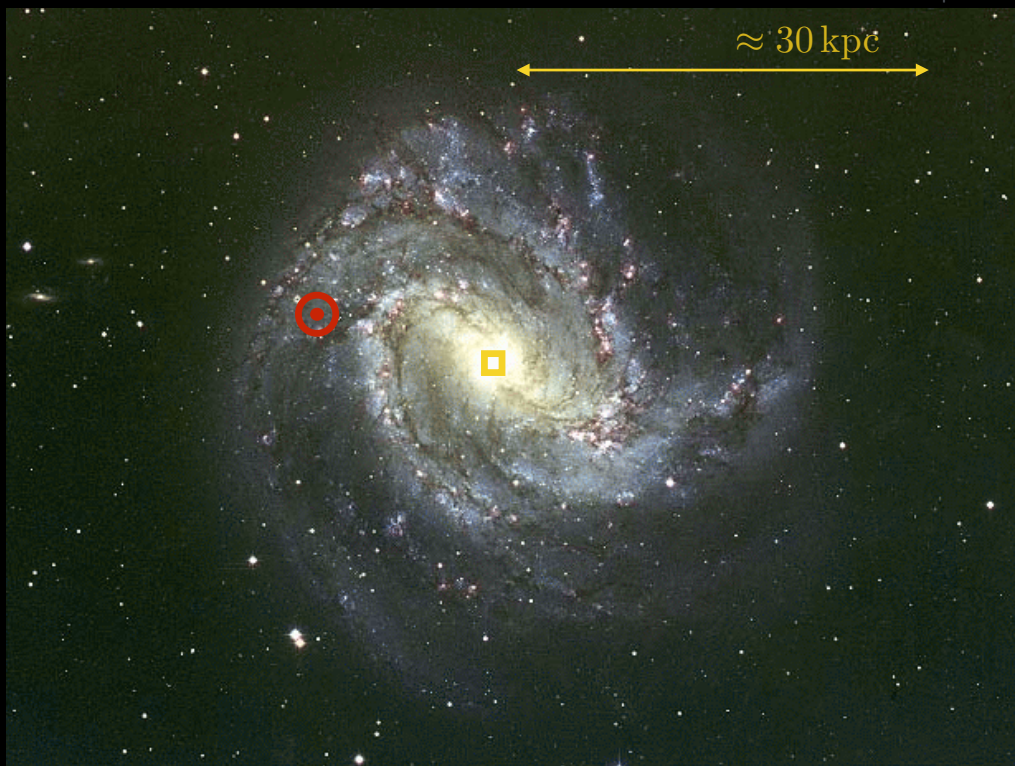
# Introduction

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## Milky Way

1pc = 3.26 light years



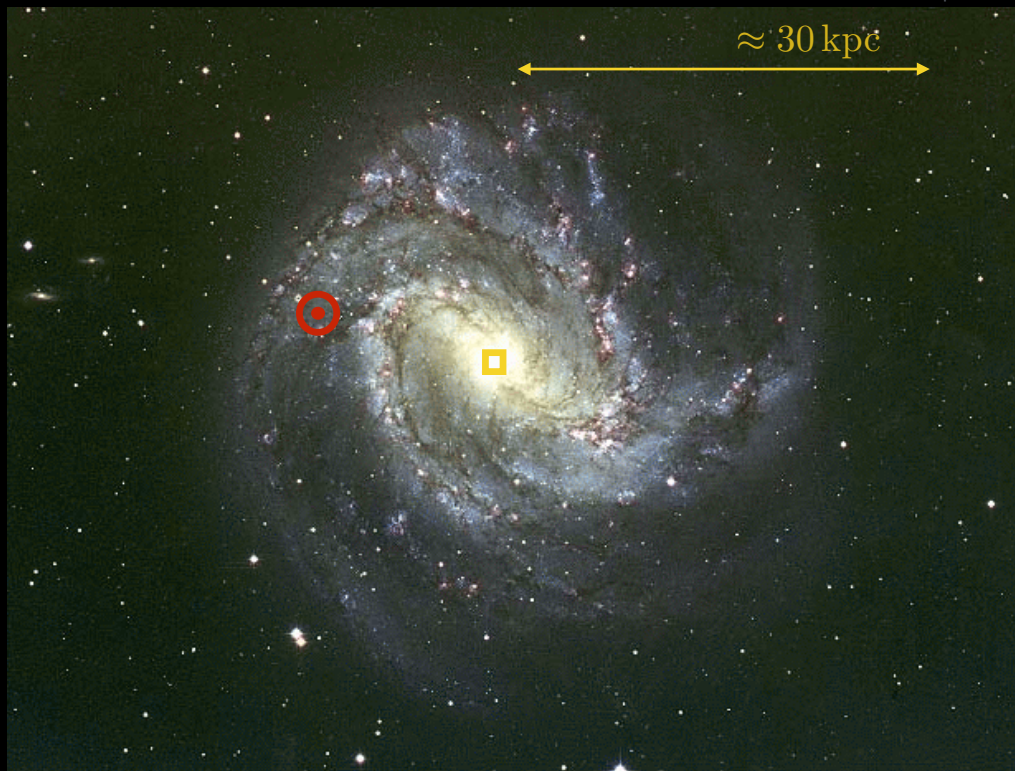
M83 © Anglo-Australian Observatory Photo by David Malin

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# $4.15 \times 10^6 M_{\odot}$ SMBH at centre of Milky Way

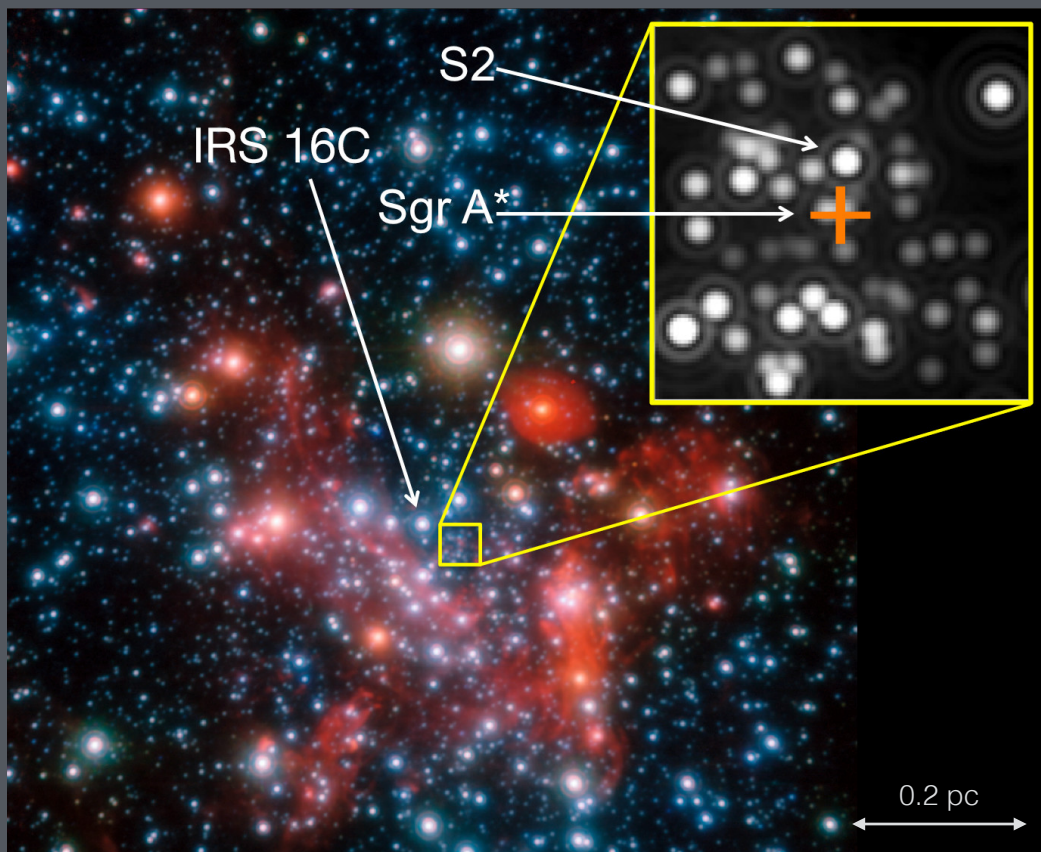
1 pc = 3.26 light years



M83 © Anglo-Australian Observatory Photo by David Malin

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# $4.15 \times 10^6 M_{\odot}$ SMBH at centre of Milky Way



ESO  
Credit: ESO/MPE/S.  
Gillessen et al.

<https://www.eso.org/public/images/eso1622b/>

1 pc = 3.26 light years

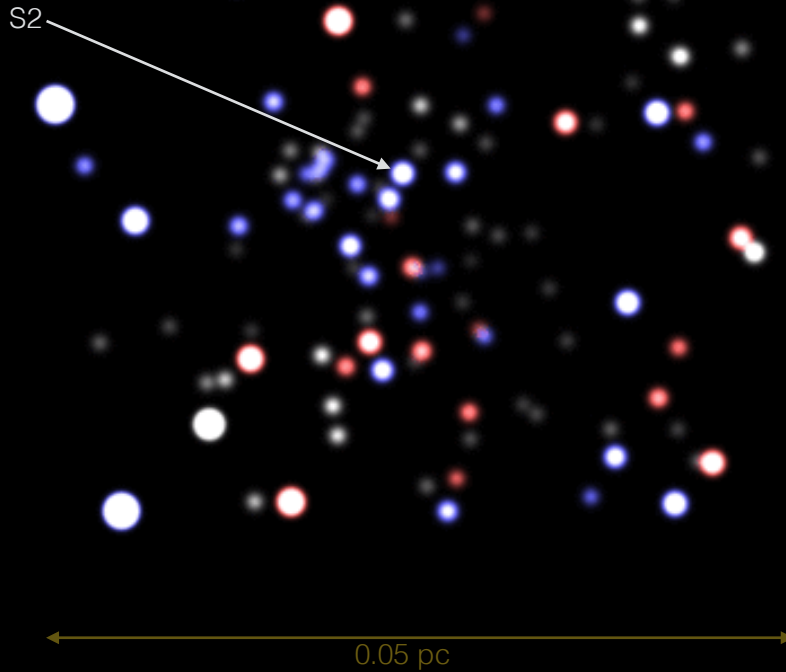


# $4.15 \times 10^6 M_{\odot}$ SMBH at centre of Milky Way

Max Planck Institute for Extragalactic Physics

Movement of stars in the central 3arcsec during 1992-2008.

Young stars = blue  
old population = red



<https://www.mpe.mpg.de/369264/>

[https://www.mpe.mpg.de/369426/](https://www.mpe.mpg.de/369426/Publications)  
Publications

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## M87

$\approx 30$  kpc



M87 image: PD-HUBBLE

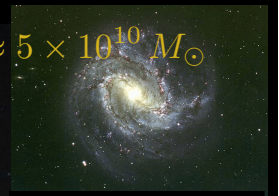
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$6.5 \times 10^9 M_{\odot}$  SMBH at centre of M87

cf  $M_{\text{MW}} \approx 5 \times 10^{10} M_{\odot}$

$\approx 30 \text{ kpc}$



M87 image: PD-HUBBLE

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$6.5 \times 10^9 M_{\odot}$  SMBH at centre of M87

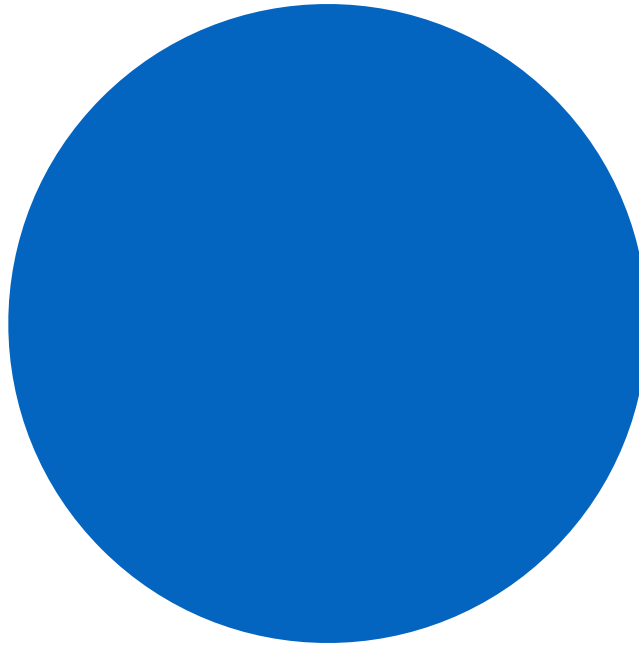
(The Event Horizon Telescope Collaboration, Akiyama et al. 2019, ApJL,)

$\approx 650 \text{ AU}$

"the asymmetric ring is consistent with earlier predictions of strong gravitational lensing of synchrotron emission from a hot plasma ( $10^{10} \text{ K}$ ) orbiting near the black hole event horizon."  
(2019, APJL, 875, L5)

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## Why "shadow" ?



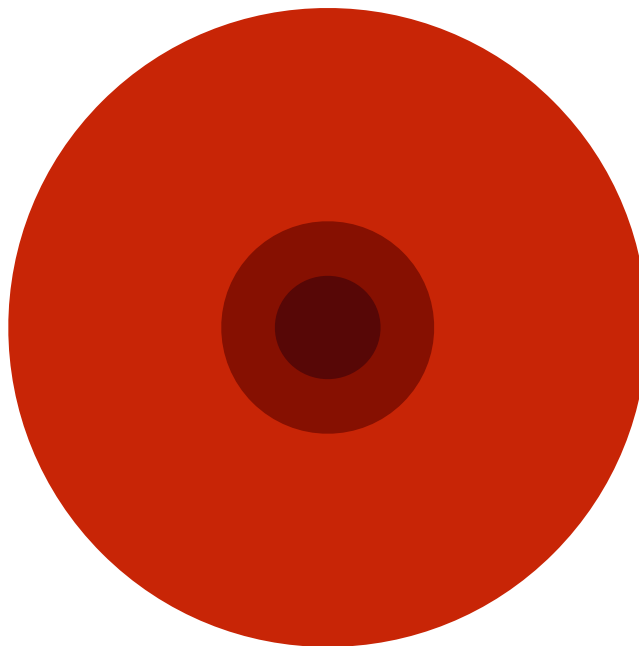
Extremely hot  
(blue emitting)  
accretion disk

The SMBH in it  
redshifts the light

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## Why "shadow" ?



Extremely hot  
(blue emitting)  
accretion disk

The SMBH in it  
redshifts the light

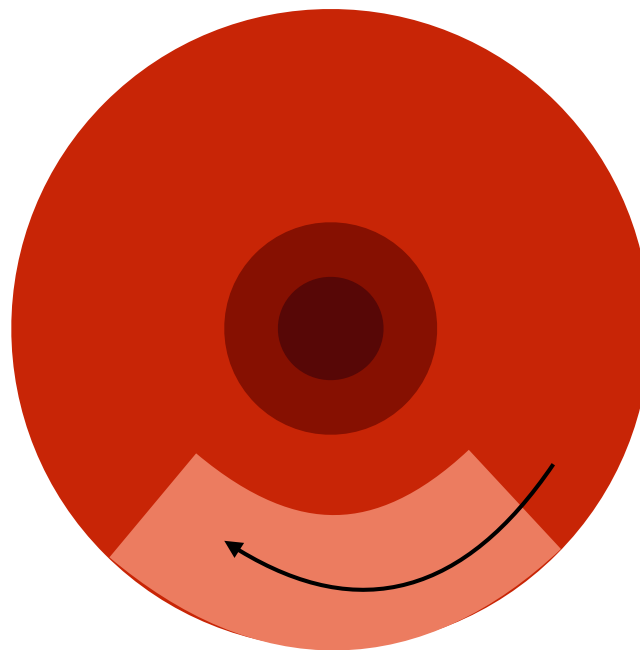
Rotation  
doppler boosts  
emission  
towards observer  
(here to the right)

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## Why "shadow" ?



Extremely hot  
(blue emitting)  
accretion disk

The SMBH in it  
redshifts the light

Rotation  
doppler boosts  
emission  
towards observer

(The Event Horizon Telescope Collaboration, Akiyama et al. 2019, ApJL **875**)

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## $6.5 \times 10^9 M_{\odot}$ SMBH at centre of M87

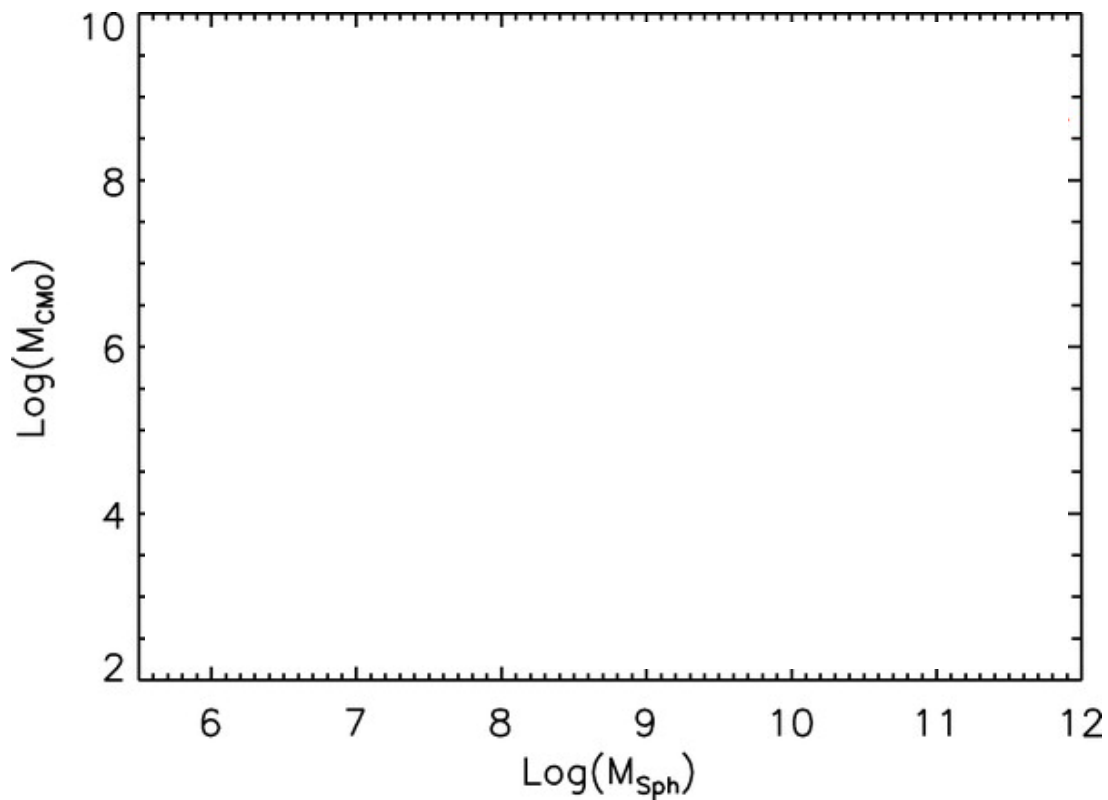
(The Event Horizon Telescope Collaboration, Akiyama et al. 2019, ApJL,)

$\approx 650$  AU

"the asymmetric ring is consistent with earlier predictions of strong gravitational lensing of synchrotron emission from a hot plasma ( $10^{10}$  K) orbiting near the black hole event horizon."  
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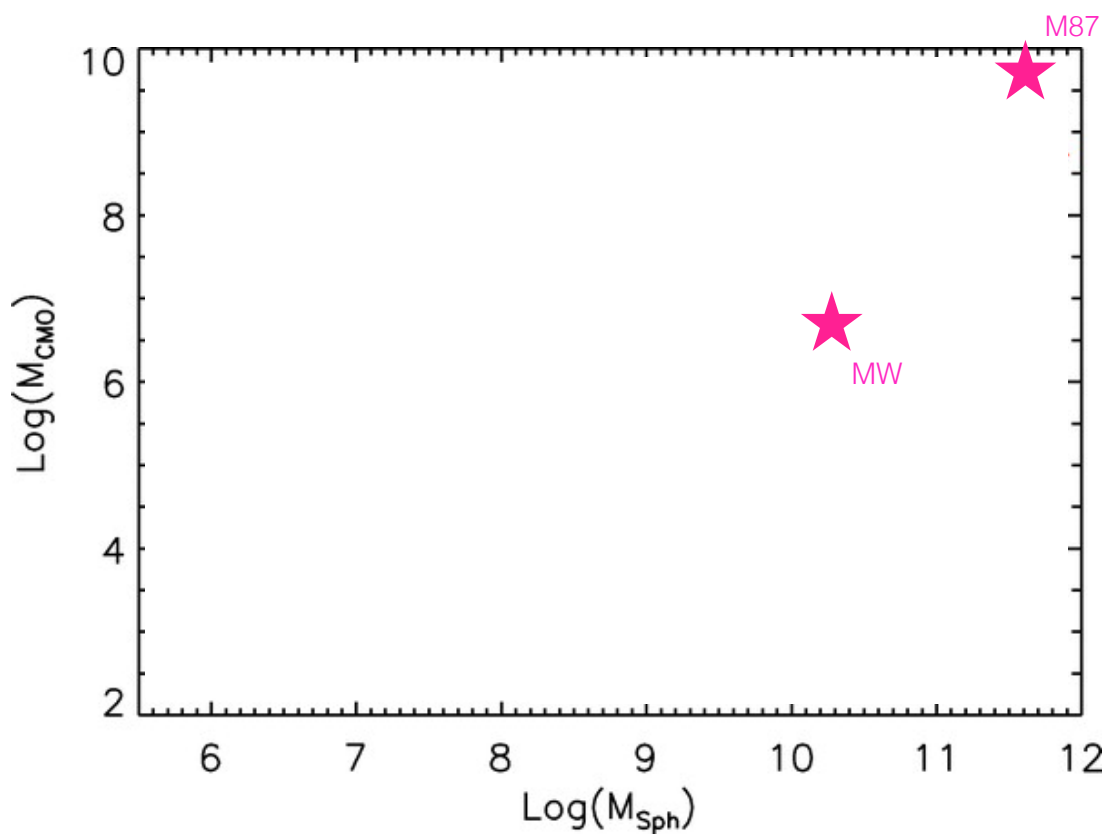
**SMBH mass vs host galaxy mass** (spheroid component: elliptical galaxy = classical bulge)  
(Gadotti & Kauffmann 2009)



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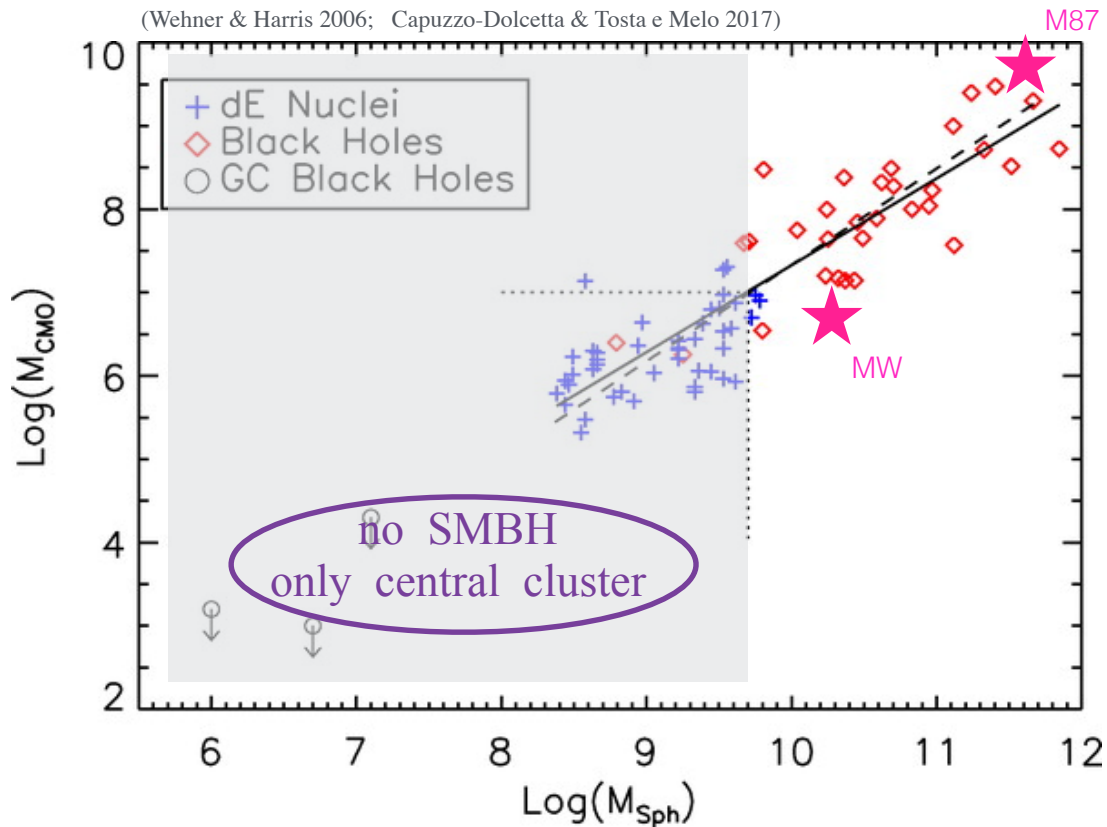
**SMBH mass vs host galaxy mass** (spheroid component: elliptical galaxy = classical bulge)  
(Gadotti & Kauffmann 2009)



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## SMBH mass vs host galaxy mass (spheroid component: elliptical galaxy = classical bulge) (Gadotti & Kauffmann 2009)



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## Spatial scales

(measurement of SMBH masses see review  
Peterson, B.M., 2014, Space Science Reviews)

$$R_{\text{horizon}} \equiv \frac{2 G M_{\text{SMBH}}}{c^2}$$

event horizon = Schwarzschild radius  
(exact solution of GR for  
spherical non-rotating mass)

$$\begin{aligned} M_{\text{SMBH}} &= 5.15 \times 10^6 M_{\odot} & R_{\text{horizon}} &= 0.106 \text{ AU} \\ M_{\text{SMBH}} &= 5.15 \times 10^9 M_{\odot} & R_{\text{horizon}} &= 106 \text{ AU} \end{aligned}$$

$$R_{\text{BHinfl}} \equiv \frac{G M_{\text{SMBH}}}{\sigma_*^2}$$

black-hole influence radius  
( $\sigma_*$  stellar velocity disp. of stars in bulge)

e.g. globular cluster :  $\sigma_* = 10 \text{ km/s}$  ,  $M_{\text{BH}} = 10^4 M_{\odot}$

$$\rightarrow R_{\text{BHinfl}} = 0.45 \text{ pc}$$

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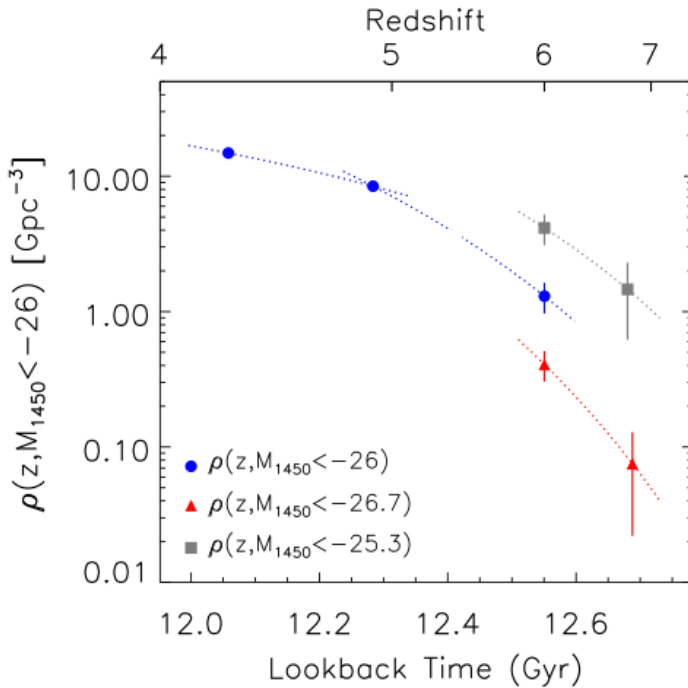
## SMBHs appear at very high redshift

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## SMBHs appear at very high redshift

THE ASTROPHYSICAL JOURNAL, 833:222 (17pp), 2016 December 20



(Jiang, McGreer et al. 2016)

13.6 13.8  
first stars  
thought to form











**Figure 10.** Density evolution of luminous quasars at  $z > 4$ . The blue circles, red triangles, and gray squares are the cumulative densities down to  $M_{1450} = -26.0$ ,  $-26.7$ , and  $-25.3$  mag, respectively. The data points at  $z \sim 4$  and  $5$  are from McGreer et al. (2013), the data points at  $z = 6$  are calculated from our new sample. The gray data point at  $z \sim 7$  is taken from Venemans et al. (2013), and the red data point at  $z \sim 7$  is estimated from two  $z > 6.5$  quasars in the UKIDSS area (see details in Section 5.1). The dotted lines are the power-law (Equation (4)) fits to the data points. The figure shows a rapid decline of the quasar spatial density from  $z \sim 5$  toward higher redshifts.

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... and at even higher redshift

## THE ASTROPHYSICAL JOURNAL LETTERS

### $\approx 700 \text{ Myr}$ $1.5 \times 10^9 M_{\odot}$ Pōniuā'ena: A Luminous $z = 7.5$ Quasar Hosting a 1.5 Billion Solar Mass Black Hole

Jinyi Yang<sup>1</sup> , Feige Wang<sup>1,13</sup> , Xiaohui Fan<sup>1</sup> , Joseph F. Hennawi<sup>2,3</sup> , Frederick B. Davies<sup>2,4</sup> ,  
Minghao Yue<sup>1</sup> , Eduardo Banados<sup>3</sup> , Xue-Bing Wu<sup>5,6</sup> , Bram Venemans<sup>3</sup> , Aaron J. Barth<sup>7</sup> 

[+ Show full author list](#)

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[The Astrophysical Journal Letters](#), Volume 897, Number 1

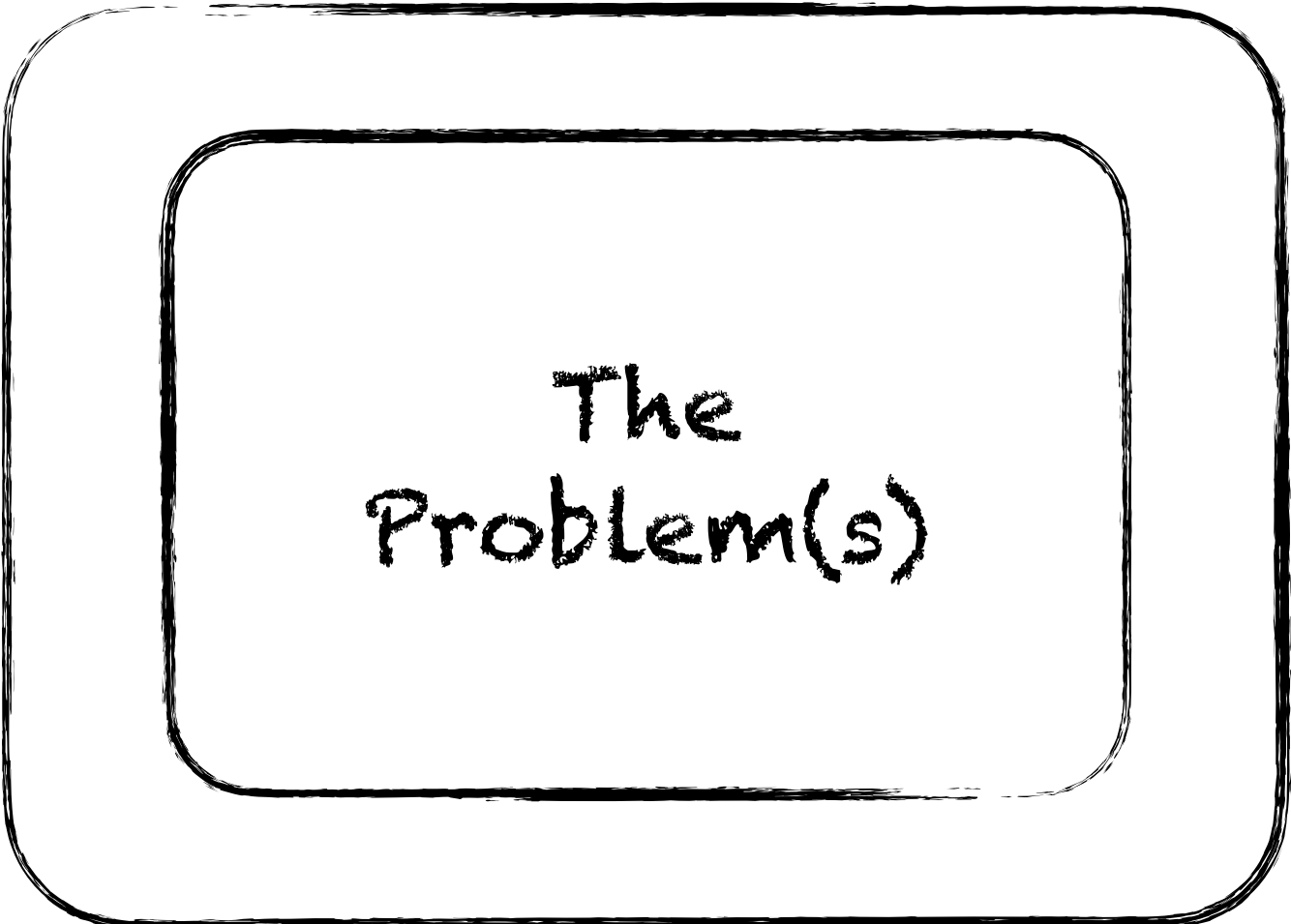
Citation Jinyi Yang et al 2020 *ApJL* 897 L14

Need  $10^4 M_{\odot}$  seed  
to grow continuously  
at superEddington rate  
since  $z=30$   
(100Myr after Big Bang).

[+ Article information](#)

### Abstract

We report the discovery of a luminous quasar, J1007+2115 at  $z = 7.515$  ("Pōniuā'ena"), from our wide-field reionization-era quasar survey. J1007+2115 is the second quasar now known at  $z > 7.5$ , deep into the reionization epoch. The quasar is powered by a  $(1.5 \pm 0.2) \times 10^9 M_{\odot}$  supermassive black hole (SMBH), based on its broad Mg II emission-line profile from Gemini and Keck near-IR spectroscopy. The SMBH in J1007+2115 is twice as massive as that in quasar J1342+0928 at  $z = 7.54$ , the current quasar redshift record holder. The existence of such a massive SMBH just 700 million years after the Big Bang



The  
Problem(s)

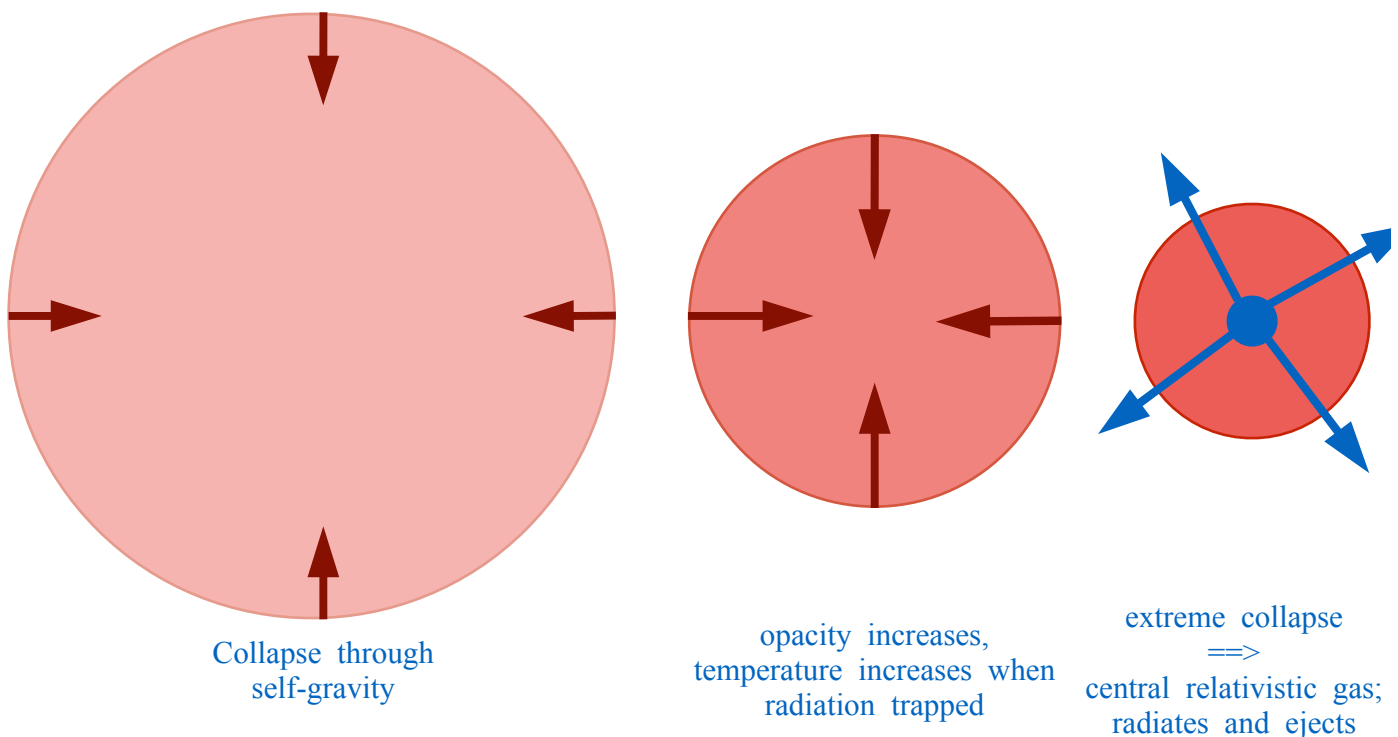
## Three problems:

- I) How can SMBHs even form ?  
(need to squeeze  $> 10^6 M_{\odot}$  of matter into extremely small space)
- II) Why do SMBH masses correlate with the masses of their hosting galaxies ?
- III) How can SMBHs form within a few 100 Myr after the Big Bang ?

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Why can a SMBH seed not form from direct collapse of a post-Big-Bang gas cloud ?



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This leads to self-radiation-limited growth

$$L_{\text{acc}} = \epsilon_r \dot{M} c^2$$

$$\epsilon_r \approx 0.1 - 0.5$$

fraction of rest-mass radiated

plus radiation pressure leads to accretion shutoff → difficult to form BH

$$M_{\text{BH}}(t) = M_{\text{BH},0} e^{\frac{f_{\text{Edd}}(t-t_0)}{\tau_{\text{Edd}}}}$$

$$f_{\text{Edd}} = \frac{1 - \epsilon_r}{\epsilon_r}$$

$$\tau_{\text{Edd}} = \frac{c \sigma_{\text{T}}}{4\pi G m_{\text{p}}} \approx 452 \text{ Myr}$$

$c$  speed of light

$\sigma_{\text{T}}$  Thompson scattering cross section

$m_{\text{p}}$  proton mass

Thus, to grow a

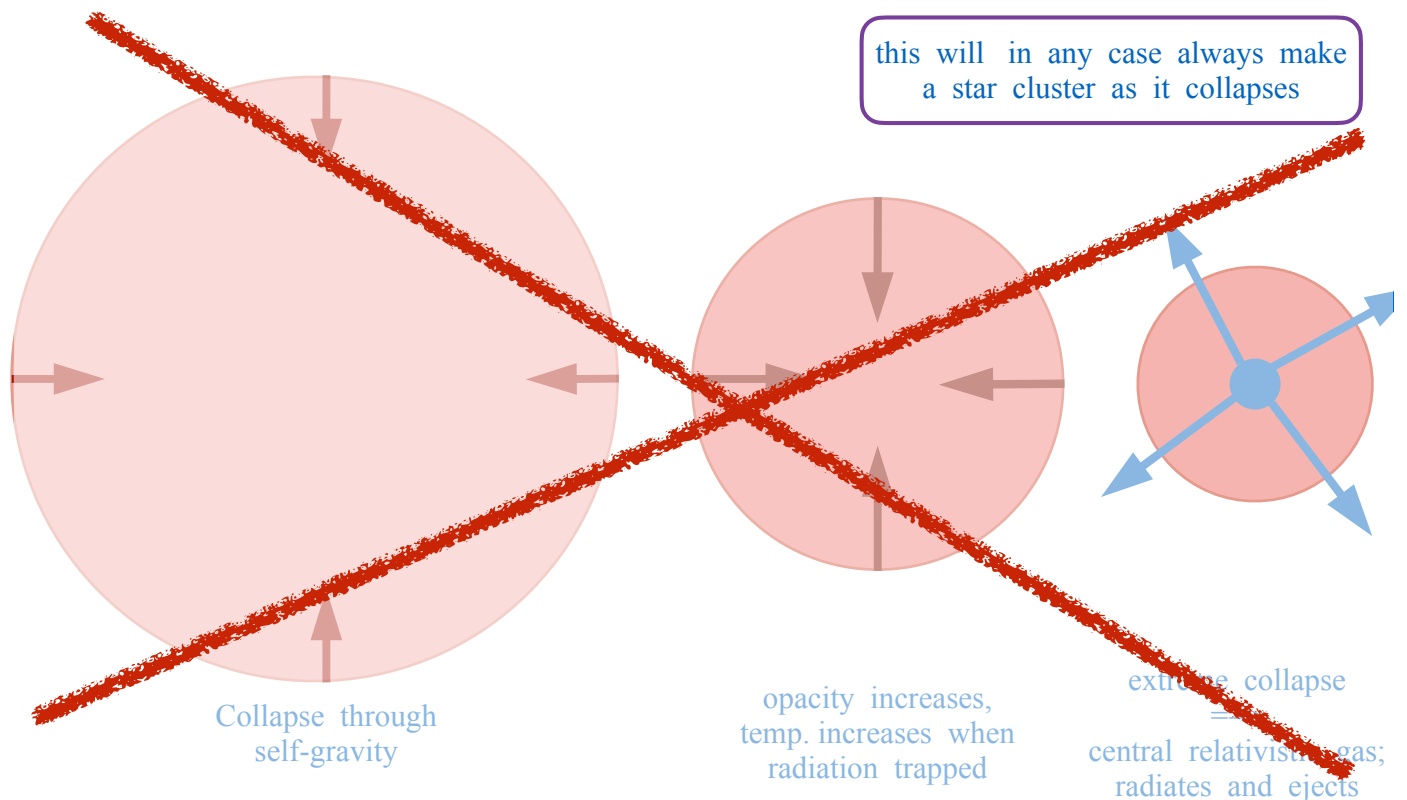
$M_{\text{BH},0} = 10 M_{\odot}$  seed to

$M_{\text{SMBH}} = 10^{10} M_{\odot}$  need sustained continuous accretion for  $\approx 1 \text{ Gyr}$  at the superEddington rate ( $\epsilon_r = 0.1$ ).

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Why not form an SMBH seed  
from direct collapse of post-Big-Bang gas cloud ?



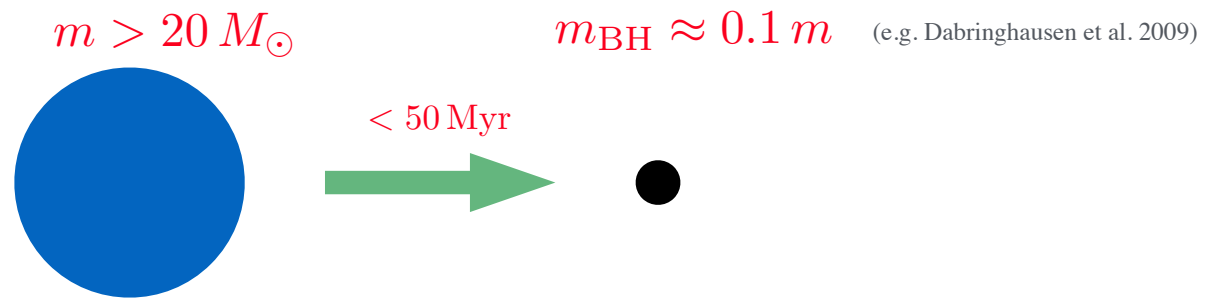
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## So, how to make SMBHs ? (Kroupa, Subr, Jerabkova, Wang 2020)

Need to *efficiently compactify* matter to a BH seed

Start with first massive stars :



Star cluster :

(e.g. Martinez, Fragione et al. 2020; Banerjee, S., 2021)



coalescence of BHs



negligible mass loss

coalescence of BHs ==> negligible mass loss :

coalescence of BHs ==> negligible mass loss :

Table III in Abbott et al. 2019; LIGO Scientific Collaboration and Virgo Collaboration)

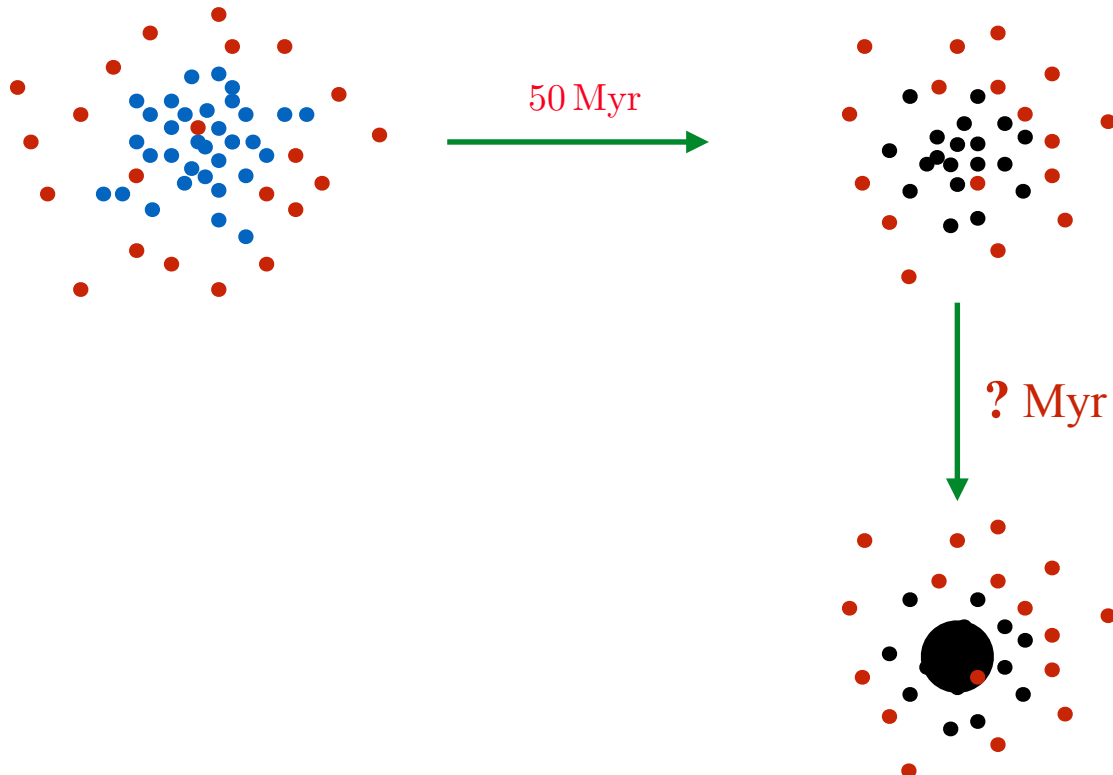
Event	$m_1/M_\odot$	$m_2/M_\odot$	$\mathcal{M}/M_\odot$	$\chi_{\text{eff}}$	$M_f/M_\odot$	$a_f$	$E_{\text{rad}}/(M_\odot c^2)$	$\ell_f$
GW150914	35.6 <sup>+4.7</sup> <sub>-3.1</sub>	30.6 <sup>+3.0</sup> <sub>-4.4</sub>	28.6 <sup>+1.7</sup> <sub>-1.5</sub>	-0.01 <sup>+0.12</sup> <sub>-0.13</sub>	63.1 <sup>+3.4</sup> <sub>-3.0</sub>	0.69 <sup>+0.05</sup> <sub>-0.04</sub>	3.1 <sup>+0.4</sup> <sub>-0.4</sub>	3.
GW151012	23.2 <sup>+14.9</sup> <sub>-5.5</sub>	13.6 <sup>+4.1</sup> <sub>-4.8</sub>	15.2 <sup>+2.1</sup> <sub>-1.2</sub>	0.05 <sup>+0.31</sup> <sub>-0.20</sub>	35.6 <sup>+10.8</sup> <sub>-3.8</sub>	0.67 <sup>+0.13</sup> <sub>-0.11</sub>	1.6 <sup>+0.6</sup> <sub>-0.5</sub>	3.
GW151226	13.7 <sup>+8.8</sup> <sub>-3.2</sub>	7.7 <sup>+2.2</sup> <sub>-2.5</sub>	8.9 <sup>+0.3</sup> <sub>-0.3</sub>	0.18 <sup>+0.20</sup> <sub>-0.12</sub>	20.5 <sup>+6.4</sup> <sub>-1.5</sub>	0.74 <sup>+0.07</sup> <sub>-0.05</sub>	1.0 <sup>+0.1</sup> <sub>-0.2</sub>	3.
GW170104	30.8 <sup>+7.3</sup> <sub>-5.6</sub>	20.0 <sup>+4.9</sup> <sub>-4.6</sub>	21.4 <sup>+2.2</sup> <sub>-1.8</sub>	-0.04 <sup>+0.17</sup> <sub>-0.21</sub>	48.9 <sup>+5.1</sup> <sub>-4.0</sub>	0.66 <sup>+0.08</sup> <sub>-0.11</sub>	2.2 <sup>+0.5</sup> <sub>-0.5</sub>	3.
GW170608	11.0 <sup>+5.5</sup> <sub>-1.7</sub>	7.6 <sup>+1.4</sup> <sub>-2.2</sub>	7.9 <sup>+0.2</sup> <sub>-0.2</sub>	0.03 <sup>+0.19</sup> <sub>-0.07</sub>	17.8 <sup>+3.4</sup> <sub>-0.7</sub>	0.69 <sup>+0.04</sup> <sub>-0.04</sub>	0.9 <sup>+0.0</sup> <sub>-0.1</sub>	3.
GW170729	50.2 <sup>+16.2</sup> <sub>-10.2</sub>	34.0 <sup>+9.1</sup> <sub>-10.1</sub>	35.4 <sup>+6.5</sup> <sub>-4.8</sub>	0.37 <sup>+0.21</sup> <sub>-0.25</sub>	79.5 <sup>+14.7</sup> <sub>-10.2</sub>	0.81 <sup>+0.07</sup> <sub>-0.13</sub>	4.8 <sup>+1.7</sup> <sub>-1.7</sub>	4.
GW170809	35.0 <sup>+8.3</sup> <sub>-5.9</sub>	23.8 <sup>+5.1</sup> <sub>-5.2</sub>	24.9 <sup>+2.1</sup> <sub>-1.7</sub>	0.08 <sup>+0.17</sup> <sub>-0.17</sub>	56.3 <sup>+5.2</sup> <sub>-3.8</sub>	0.70 <sup>+0.08</sup> <sub>-0.09</sub>	2.7 <sup>+0.6</sup> <sub>-0.6</sub>	3.
GW170814	30.6 <sup>+5.6</sup> <sub>-3.0</sub>	25.2 <sup>+2.8</sup> <sub>-4.0</sub>	24.1 <sup>+1.4</sup> <sub>-1.1</sub>	0.07 <sup>+0.12</sup> <sub>-0.12</sub>	53.2 <sup>+3.2</sup> <sub>-2.4</sub>	0.72 <sup>+0.07</sup> <sub>-0.05</sub>	2.7 <sup>+0.4</sup> <sub>-0.3</sub>	3.
GW170817	1.46 <sup>+0.12</sup> <sub>-0.10</sub>	1.27 <sup>+0.09</sup> <sub>-0.09</sub>	1.186 <sup>+0.001</sup> <sub>-0.001</sub>	0.00 <sup>+0.02</sup> <sub>-0.01</sub>	$\leq 2.8$	$\leq 0.89$	$\geq 0.04$	$\geq$
GW170818	35.4 <sup>+7.5</sup> <sub>-4.7</sub>	26.7 <sup>+4.3</sup> <sub>-5.2</sub>	26.5 <sup>+2.1</sup> <sub>-1.7</sub>	-0.09 <sup>+0.18</sup> <sub>-0.21</sub>	59.4 <sup>+4.9</sup> <sub>-3.8</sub>	0.67 <sup>+0.07</sup> <sub>-0.08</sub>	2.7 <sup>+0.5</sup> <sub>-0.5</sub>	3.
GW170823	39.5 <sup>+11.2</sup> <sub>-6.7</sub>	29.0 <sup>+6.7</sup> <sub>-7.8</sub>	29.2 <sup>+4.6</sup> <sub>-3.6</sub>	0.09 <sup>+0.22</sup> <sub>-0.26</sub>	65.4 <sup>+10.1</sup> <sub>-7.4</sub>	0.72 <sup>+0.09</sup> <sub>-0.12</sub>	3.3 <sup>+1.0</sup> <sub>-0.9</sub>	3.

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This is promising, but how to merge  $> 10^4$  BHs sufficiently quickly ?

Star cluster :

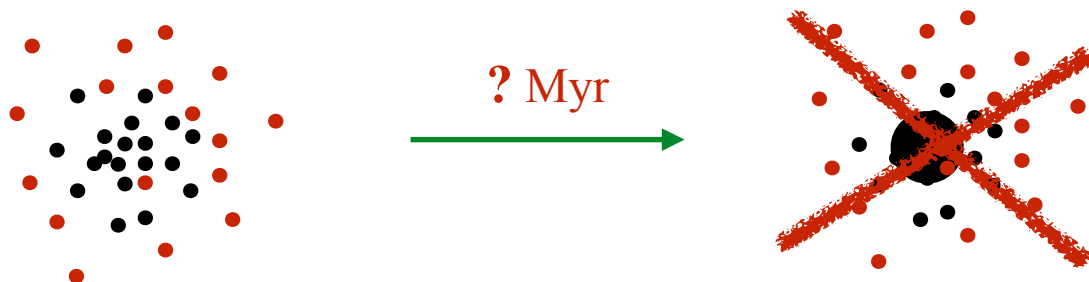


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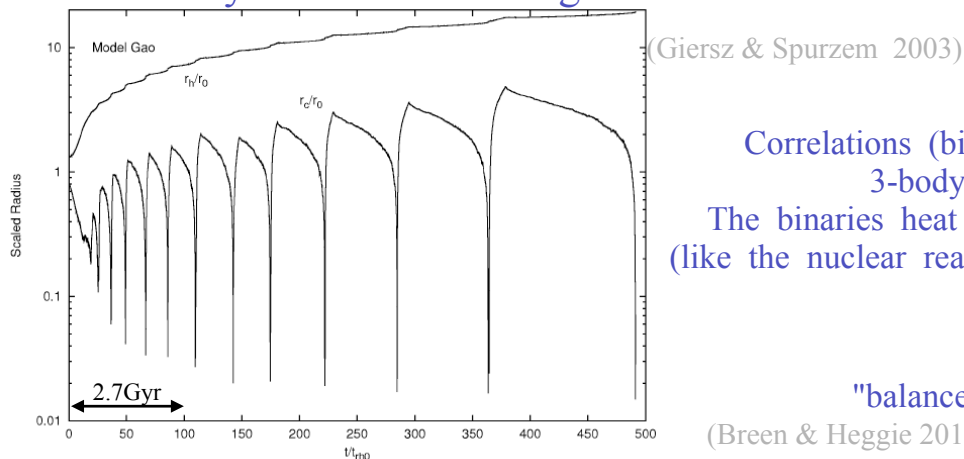
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This is promising, but how to merge  $> 10^4$  BHs sufficiently quickly ?



Stellar dynamical modelling shows such a cluster to be stable :



Correlations (binaries) form through 3-body encounters.  
The binaries heat the rest of the cluster (like the nuclear reactions in stellar interiors).

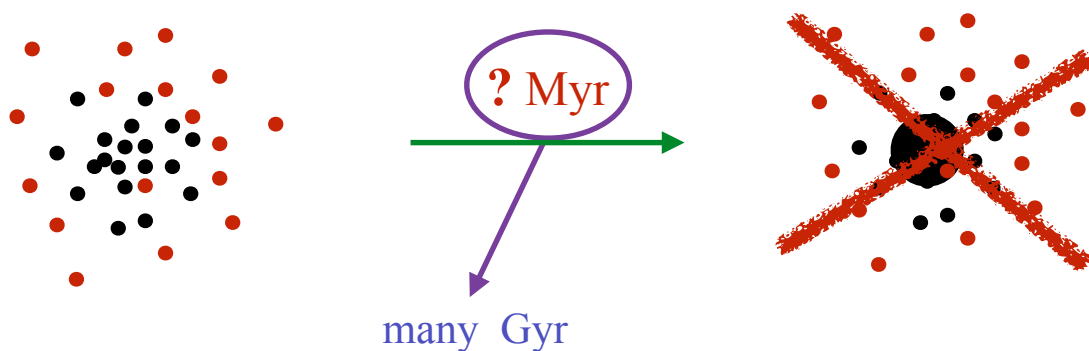


"balanced evolution"  
(Breen & Heggie 2013; Rodriguez et al. 2016)

**Figure 4.** Evolution of the core and half-mass radii (scaled by the scale-length of the Plummer model) as a function of time (scaled by the initial half-mass relaxation time).

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This is promising, but how to merge  $> 10^4$  BHs sufficiently quickly ?



Clusters of BHs cannot evolve to a SMBH seed within  $\approx 200$  Myr

# The Solution

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## Put this into the context of *galaxy formation and evolution*:

(Kroupa, Subr, Jerabkova, Wang 2020)

First-formed very metal-poor extremely massive star-burst star cluster forms at centre of *future* spheroid : (confirmed by Martin-Navarro et al. 2018 = Vazdekis IACanary team)

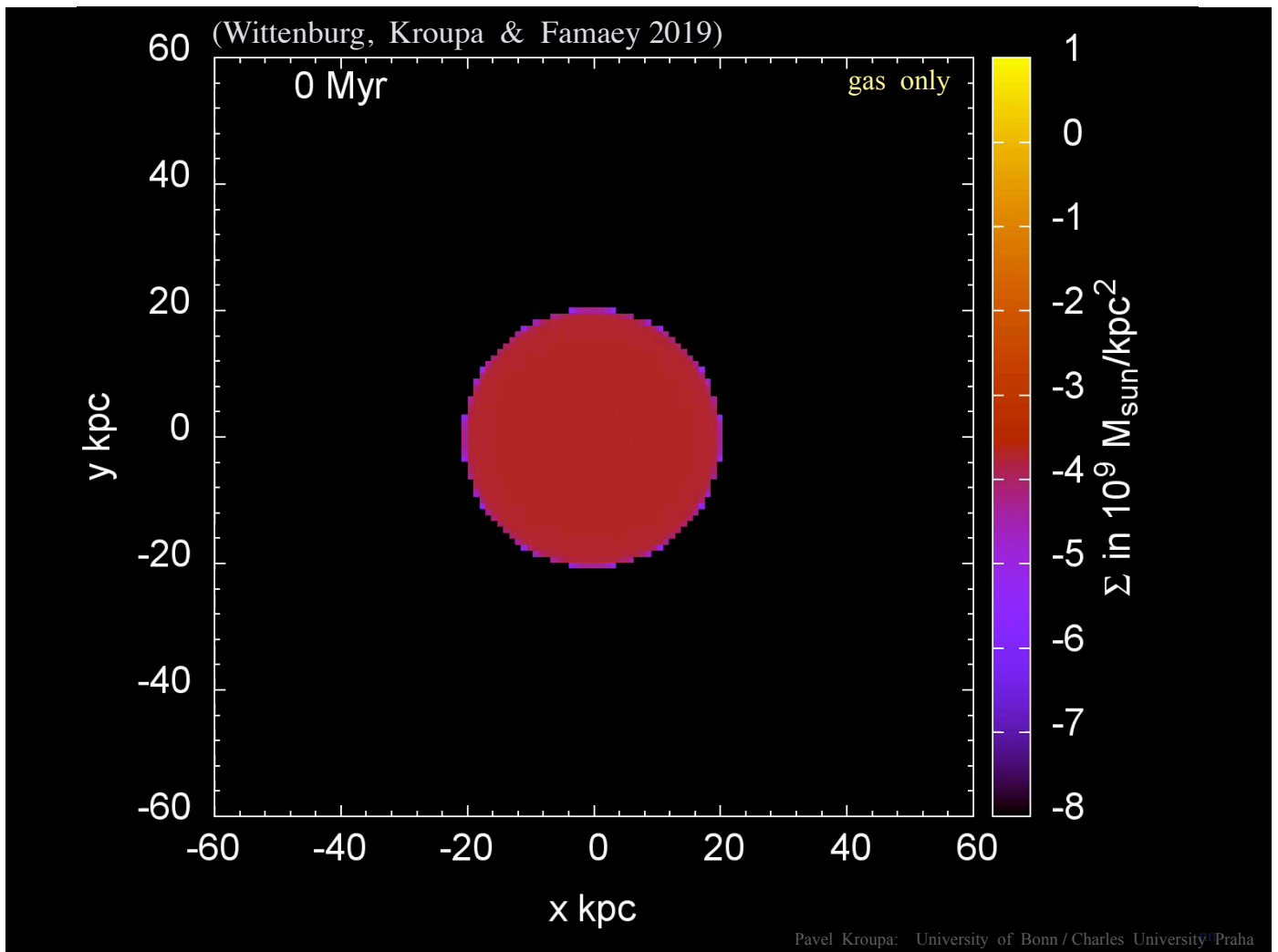
## Galaxy formation and evolution: (Wittenburg, Kroupa & Famaey 2019)

The evolution over 10 Gyr of a spherical gas cloud of mass  $M_{\text{gas}} = 6.4 \times 10^9 M_{\odot}$  and  $r_{\text{sph}} = 20$  kpc and with an initial cylindrical rotational law with  $\eta = 0.025 \text{ Myr}^{-1}$

Actual E galaxy-formation simulations are underway  
(Eappen, Kroupa, Wittenburg & Famaey, in prep.)

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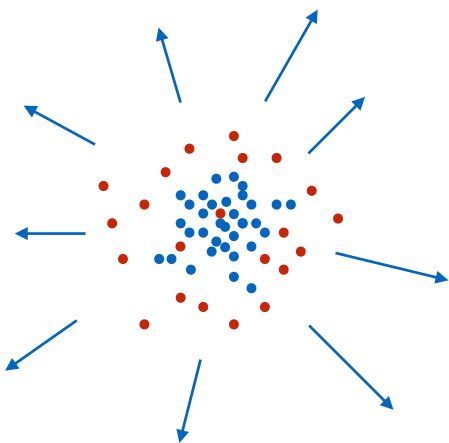
Pavel Kroupa: University of Bonn / Charles University Praha



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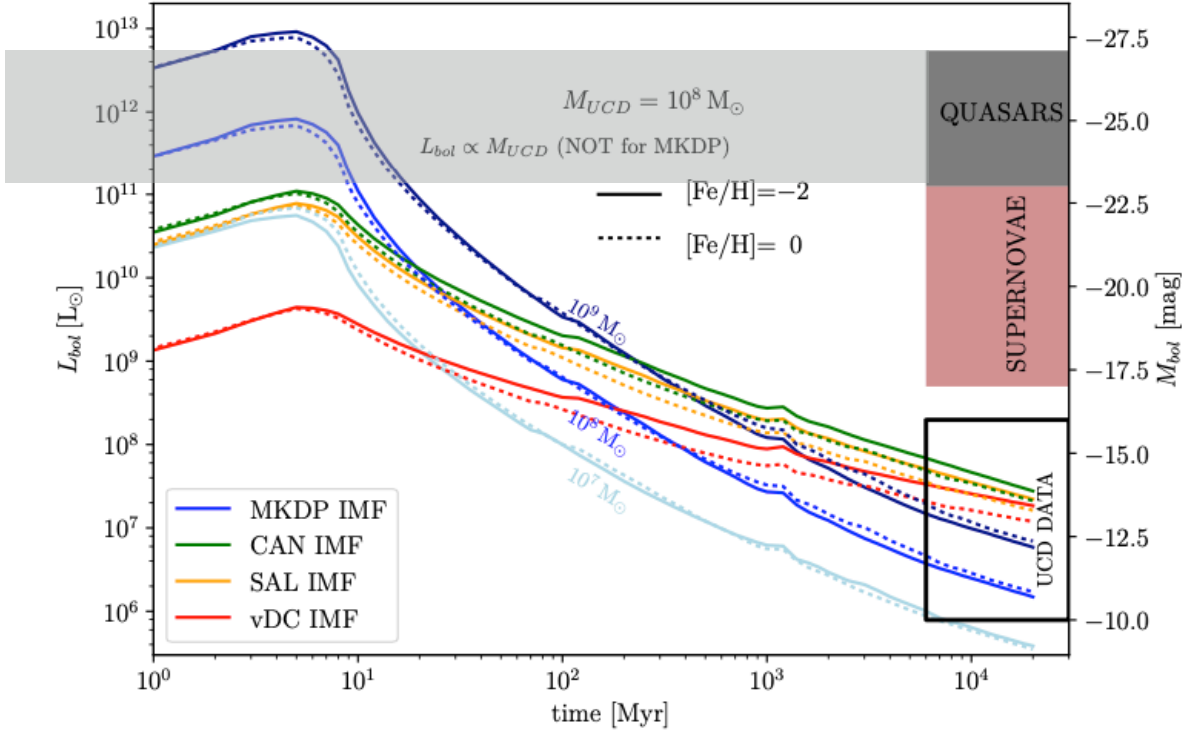


extreme radiation field and outwards wind stops gas infall from surrounding forming spheroid (Ploekinger et al. 2019)

## First-formed hyper-massive star-burst cluster :

(Jerabkova, Kroupa, Dabringhausen, Hilker & Bekki 2017)

T. Jeřábková et al.: The formation of UCDs: Testing for a variable stellar IMF



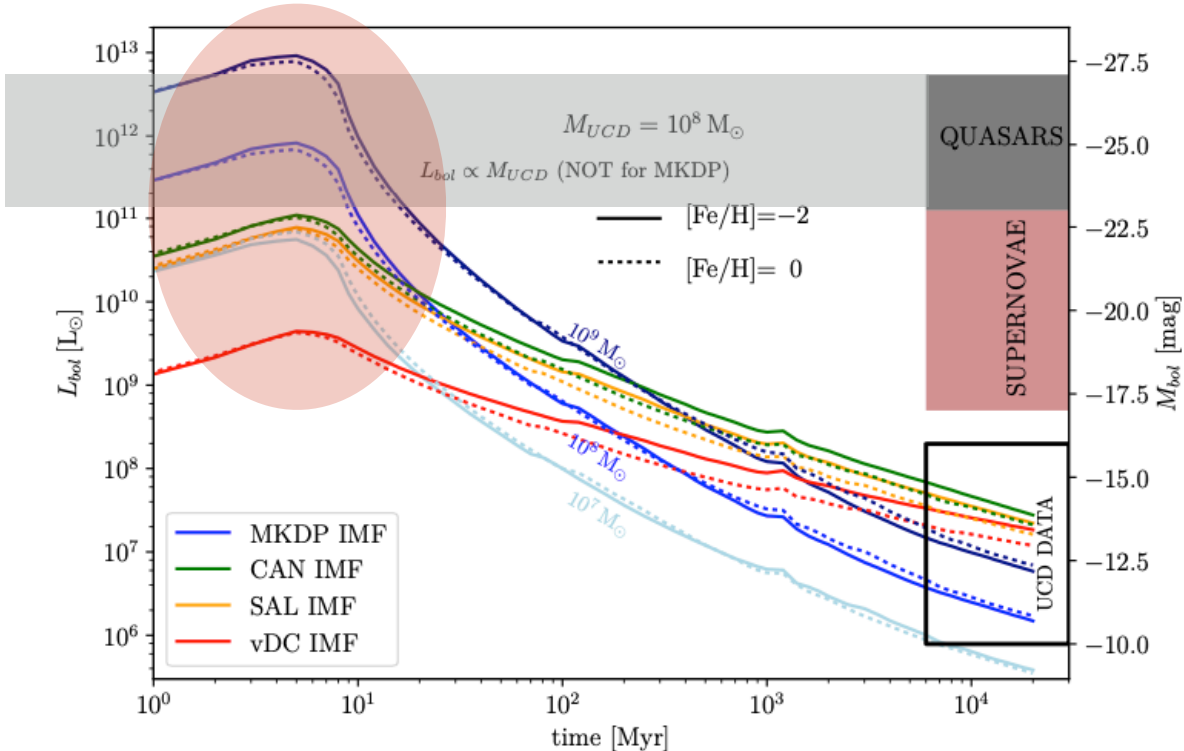
**Fig. 3.** Time evolution of the bolometric luminosity for different IMFs. The MKDP IMF changes with the initial mass of the UCD and does not scale linearly with its mass. In contrast, the vDC, SAL, and CAN IMFs have UCD-mass-independent slopes and scale proportionally with  $M_{\text{UCD}}$ . The grey panel shows the typical luminosities of quasars (Dunlop et al. 1993, 2003; Souchay et al. 2015) and the brown panel shows the luminosity span for the peak luminosities supernovae (Gal-Yam 2012; Lyman et al. 2016), which might cause luminosity variations in  $L_{\text{bol}}$  of UCDs younger than about 50 Myr according to SNe rates.

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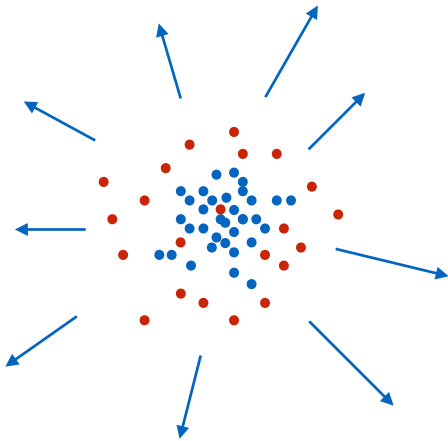
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**Put this into the context of *galaxy formation and evolution*:**

(Kroupa, Subr, Jerabkova, Wang 2020)

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extreme radiation field and outwards wind stops gas infall from surrounding forming spheroid (Ploekinger et al. 2019)

e.g. for 50 Myr, cluster of  $10^8 M_{\odot}$

luminosity of  $10^{12} L_{\odot}$

drives metal-rich outflow at  $2 M_{\odot}/\text{yr}$

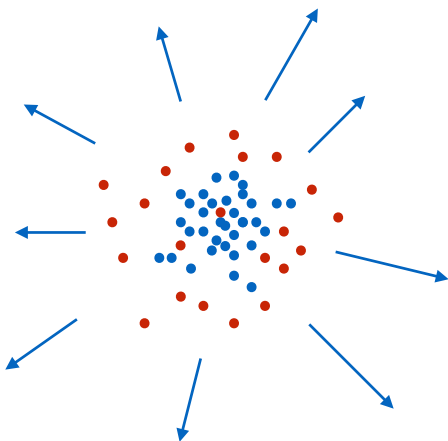
at few  $10^3 \text{ km/s}$

Might well be mistaken for a  $z > 6$  quasar.

**Put this into the context of *galaxy formation and evolution*:**

(Kroupa, Subr, Jerabkova, Wang 2020)

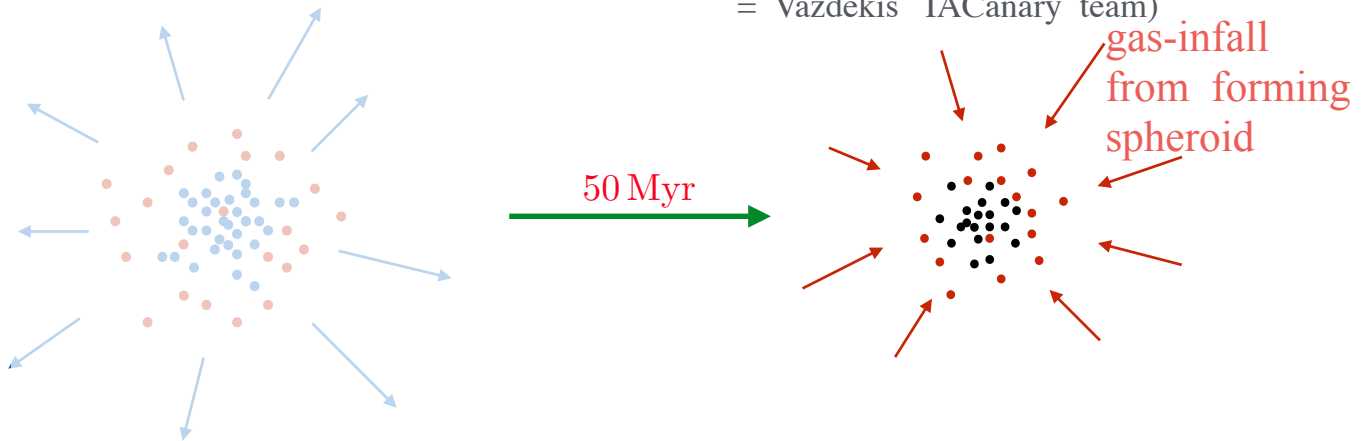
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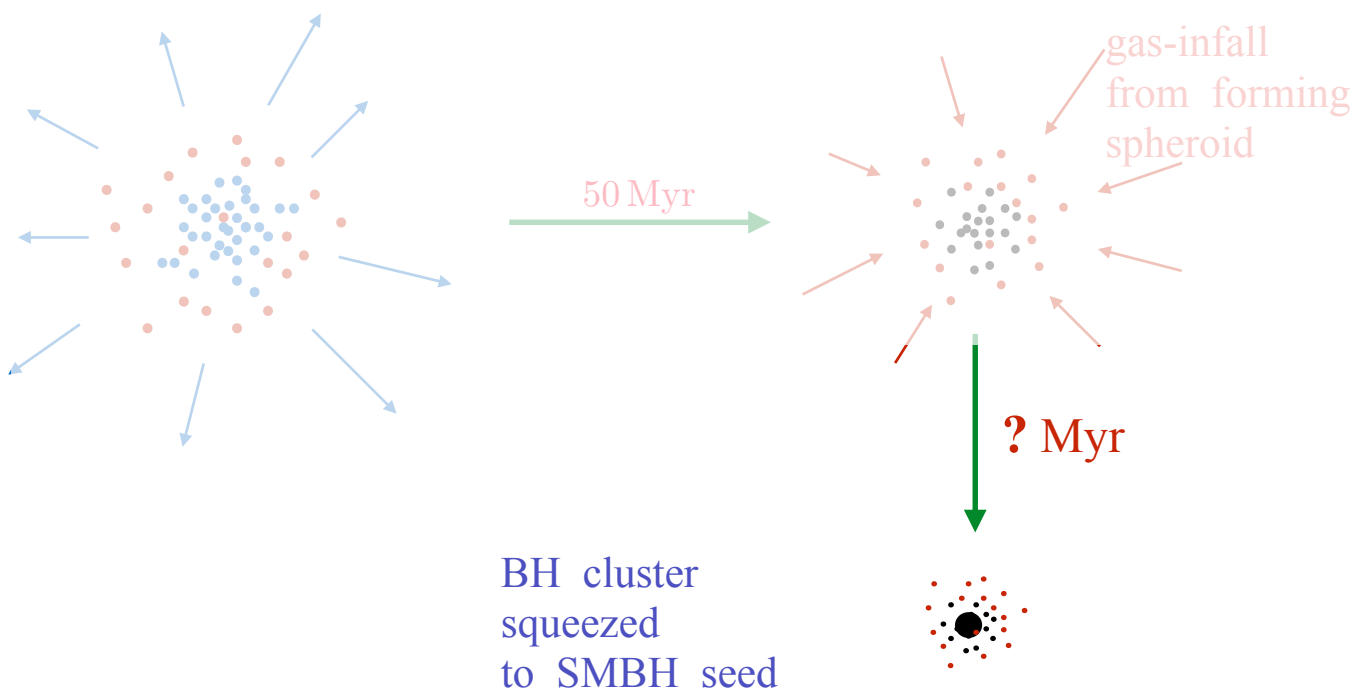
43

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**Put this into the context of *galaxy formation and evolution*:**

(Kroupa, Subr, Jerabkova, Wang 2020)

First-formed very metal-poor extremely massive star-burst star cluster forms at centre of *future* spheroid:



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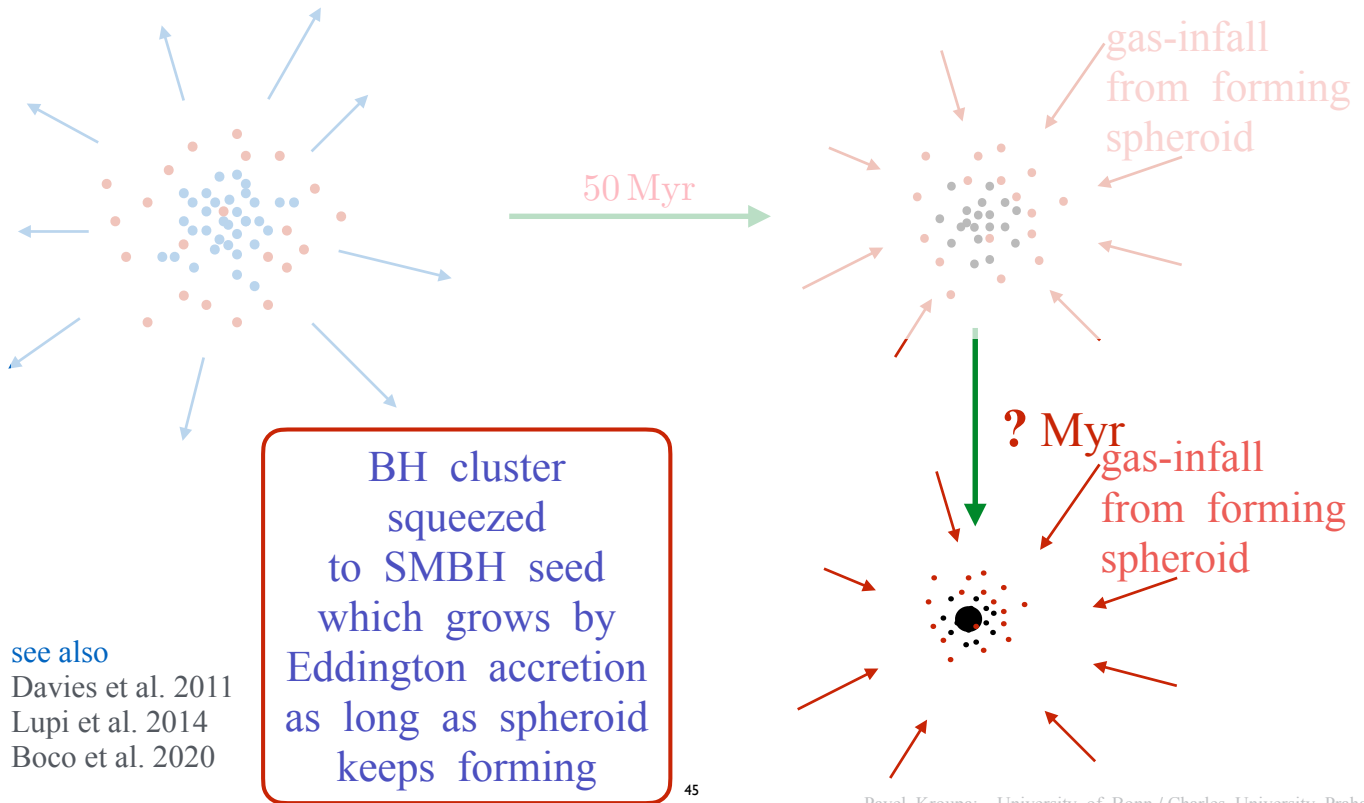
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## Put this into the context of *galaxy formation and evolution*:

(Kroupa, Subr, Jerabkova, Wang 2020)

First-formed very metal-poor extremely massive star-burst star cluster forms at centre of *future* spheroid:



## Evolution of BH cluster as gas in-falls

(Kroupa, Subr, Jerabkova, Wang 2020)

$$E(t) = \frac{G (M_{\text{gas}}(t) + N m_{\text{BH}}(t))^2}{R(t)} = N m_{\text{BH}}(t) \sigma(t)^2$$

potential energy; cluster in virial equilibrium at any time.

$$\sigma(t) = \left( \frac{G (M_{\text{gas}}(t) + N m_{\text{BH}}(t))^2}{R N m_{\text{BH}}(t)} \right)^{\frac{1}{2}}$$

velocity dispersion of BH cluster

$$\dot{R} = \left( \frac{\dot{E}}{G} - \frac{2}{R} (M_{\text{gas}} + N m_{\text{BH}}) (\dot{M}_{\text{gas}} + N \dot{m}_{\text{BH}}) \right) \frac{R^2}{(M_{\text{gas}} + N m_{\text{BH}})^2}$$

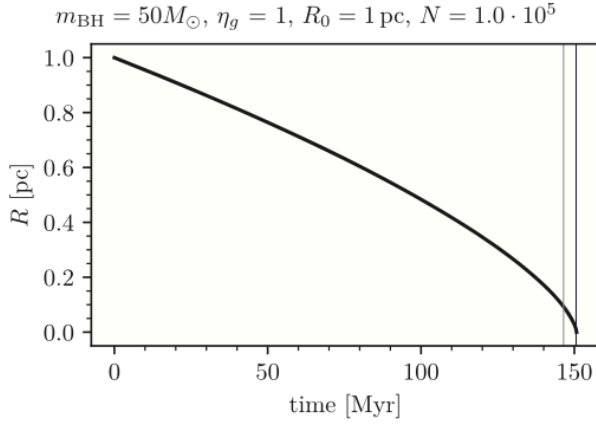
with  $\dot{E} = \dot{E}_{\text{diss}} + \dot{E}_{\text{bin,heat}}$

binding energy change through gas drag and binary heating through BH-BH binaries.

## Evolution of BH cluster as gas infalls

(Kroupa, Subr, Jerabkova, Wang 2020)

$$\eta_g \equiv \frac{M_{\text{gas}}}{N m_{\text{BH}}}$$



**Figure 5.** The evolution of the cluster radius,  $R(t)$ , for  $\eta_g = 1.0$ ,  $m_{\text{BH}} = 50 M_{\odot}$ ,  $M_{\text{BH},0} = 5 \times 10^6 M_{\odot}$ , and  $R_0 = 1$  pc. The cluster of BHs contracts because gas drag outweighs binary heating. See Fig. 6 for the ratio of the rates of energy change due to gas drag and binary heating. The vertical thin grey line represents the time,  $t_{\text{crit}}$ , when binary heating ceases to be relevant (equation 17) and the vertical thick line shows the time,  $t_{\text{rel}}$ , when the BH cluster reaches the relativistic state (equation 20).

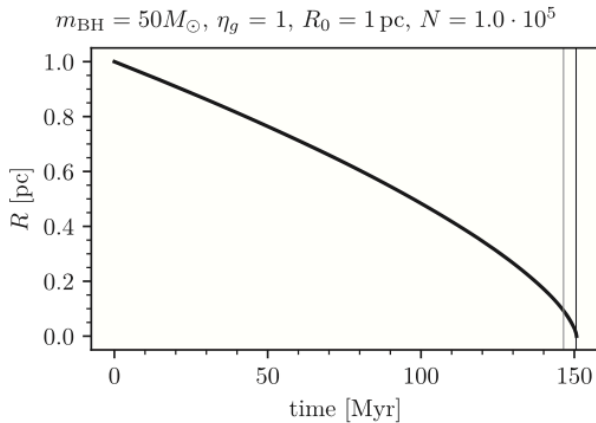
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## Evolution of BH cluster as gas infalls

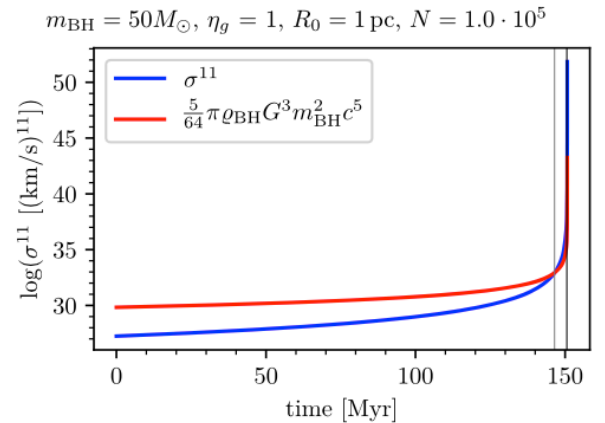
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*Quasars and SMBHs* 5663



**Figure 7.** The evolution of the velocity dispersion (equation 24, blue line) and of the condition when binaries cease to be a heating source (equation 17, red line) for the parameters as in Fig. 5. The velocity dispersion increases as the cluster plus gas cloud shrinks. When the two lines intersect (the left vertical line), binary heating ceases to be active. The vertical lines have the same meaning as in Fig. 5. Note that  $\log = \log_{10}$ .

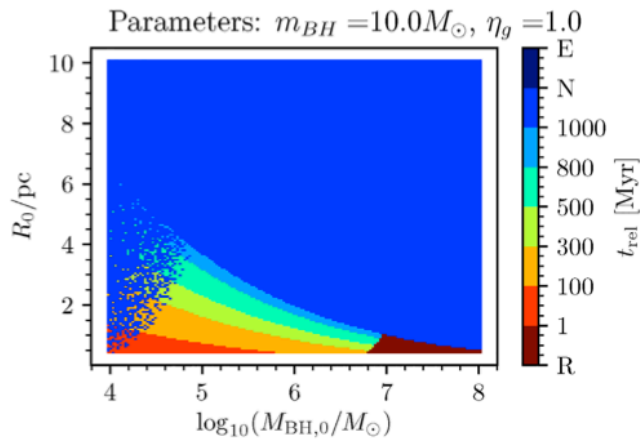
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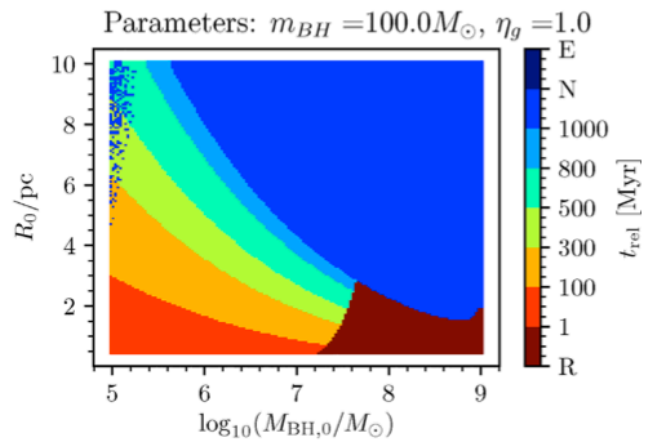
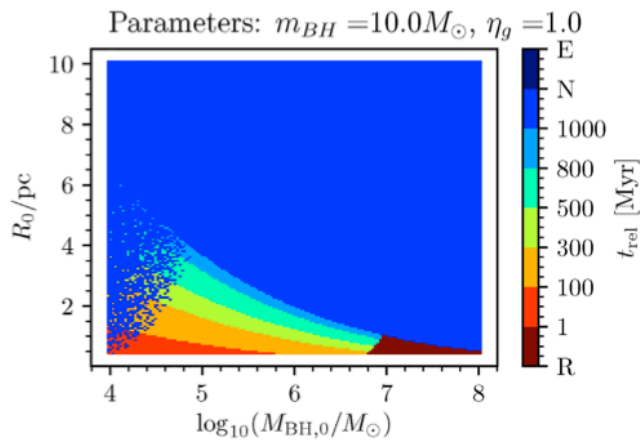
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(Kroupa, Subr, Jerabkova, Wang 2020)

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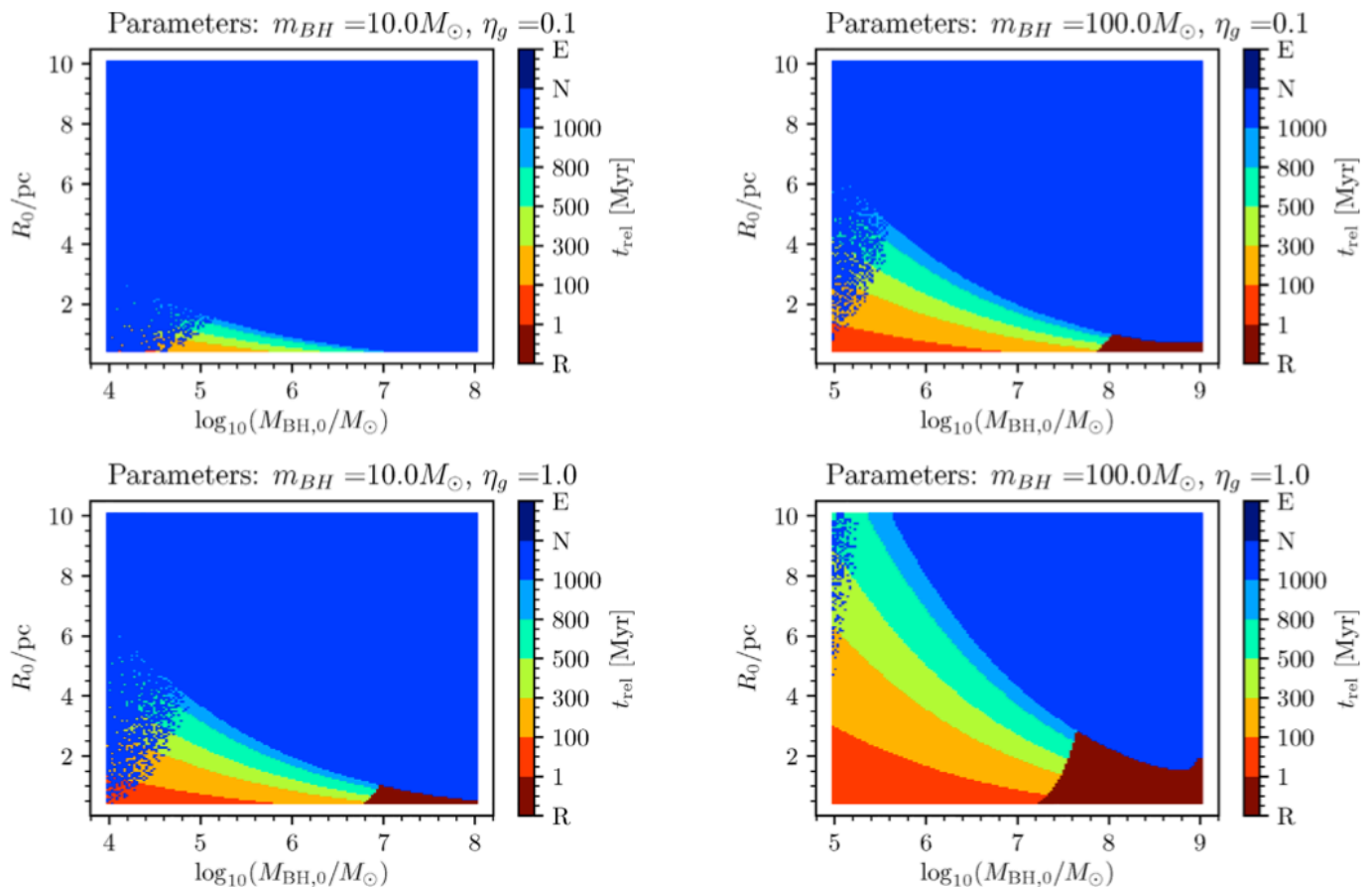
50

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## Evolution of BH cluster as gas infalls

(Kroupa, Subr, Jerabkova, Wang 2020)



shrinkage to relativistic regime ( $\sigma_{\text{rel}} \equiv 3000 \text{ km/s}$ )  
within 200 Myr of BH cluster formation (250 Myr after  
1st star forms).

then *collapse of >5%* of BH cluster to SMBH seed  
through gravitational wave energy loss essentially  
*instantaneous* (see also Lee 1993; Kuper et al. 2006 for Nbody).

A SMBH seed weighing  $>5\%$  of the BH cluster  
is possible within 200-300 Myr of the formation  
of the first stars.

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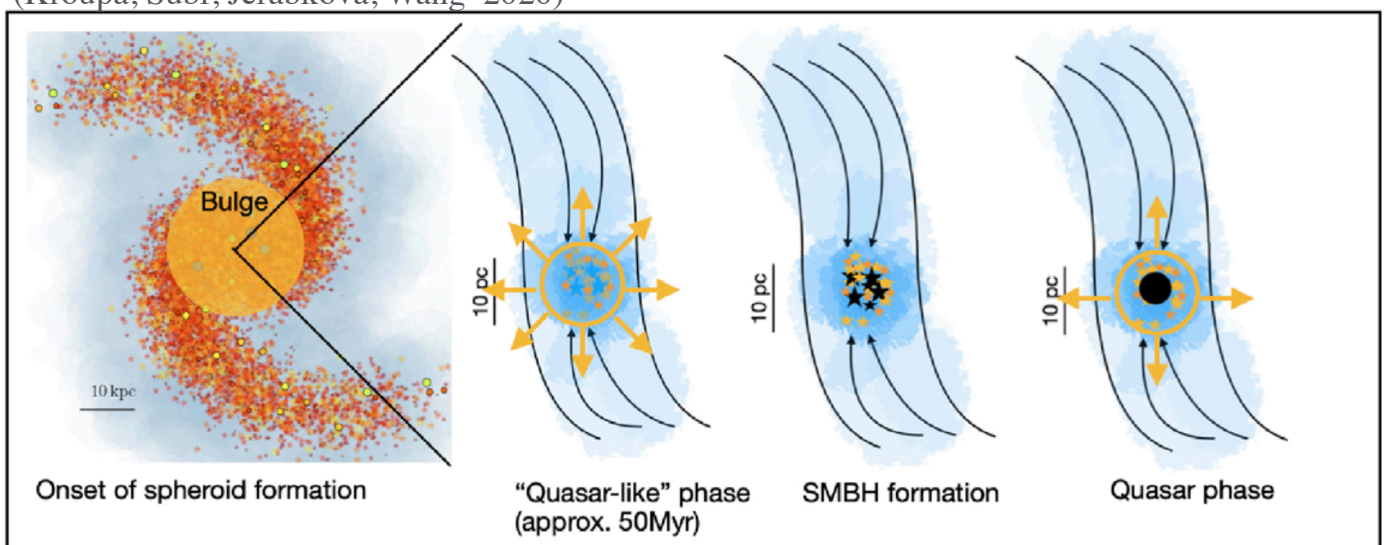
# Implications for early nucleosynthesis

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## Remember/Summary

(Kroupa, Subr, Jerabkova, Wang 2020)



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## Evolution of BH cluster as gas infalls

(Kroupa, Subr, Jerabkova, Wang 2020)

During the squeeze millions of neutron stars  
are squashed together



Strong flux of elements before any CCSN ?

Strong flux of neutrons ?

To intergalactic distances ?

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Within 11 Mpc there are  
about 140 galaxies  
more massive than  $10^9 M_{\text{sun}}$   
i.e.  
140 SMBHs

First star formation about 200Myr after Big Bang

i.e. at redshift  $z=20$

the Universe was  $1/21$  its present size

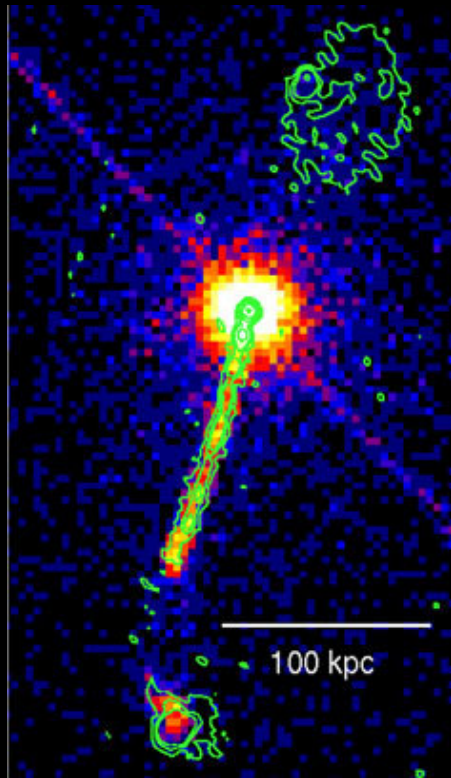
i.e. there were 140 forming SMBHs within 500kpc of "us"

Jets from quasars can reach lengths of 100s kpc

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A Chandra X-ray image of the quasar 3C19.44. The overlaid contours show the radio emission (the dimension 100kpc corresponds to 329,000 light-years; the extremely bright core produces a line of bright pixels as an artifact).

Credit: NASA/Chandra VLA and Harris et al

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Enrichment by heavy elements  
(even r-process ?)  
within a Myr after Big Bang  
to distances of 100s of kpc,  
i.e.  
\_all\_ of space  
?

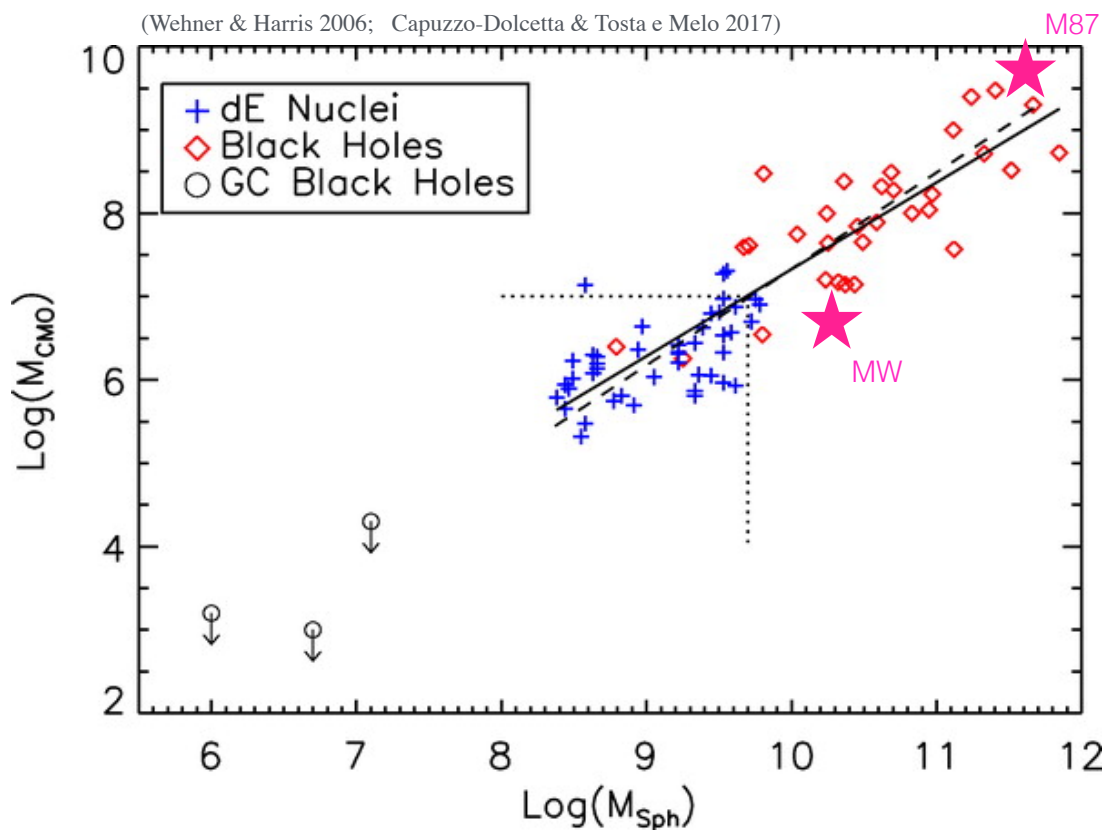
this is likely to be non-homogeneous  
i.e. more r-process "here" vs more s-process "there"  
etc.

What about  
the correlation between  
the SMBH  
and  
host galaxy  
mass?

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**Remember: SMBH mass vs host galaxy mass** (spheroid component)



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Need to ensure that enough gas  
falls into the central region  
of a forming galaxy.

This is not possible in disk galaxies,  
they form too slowly.



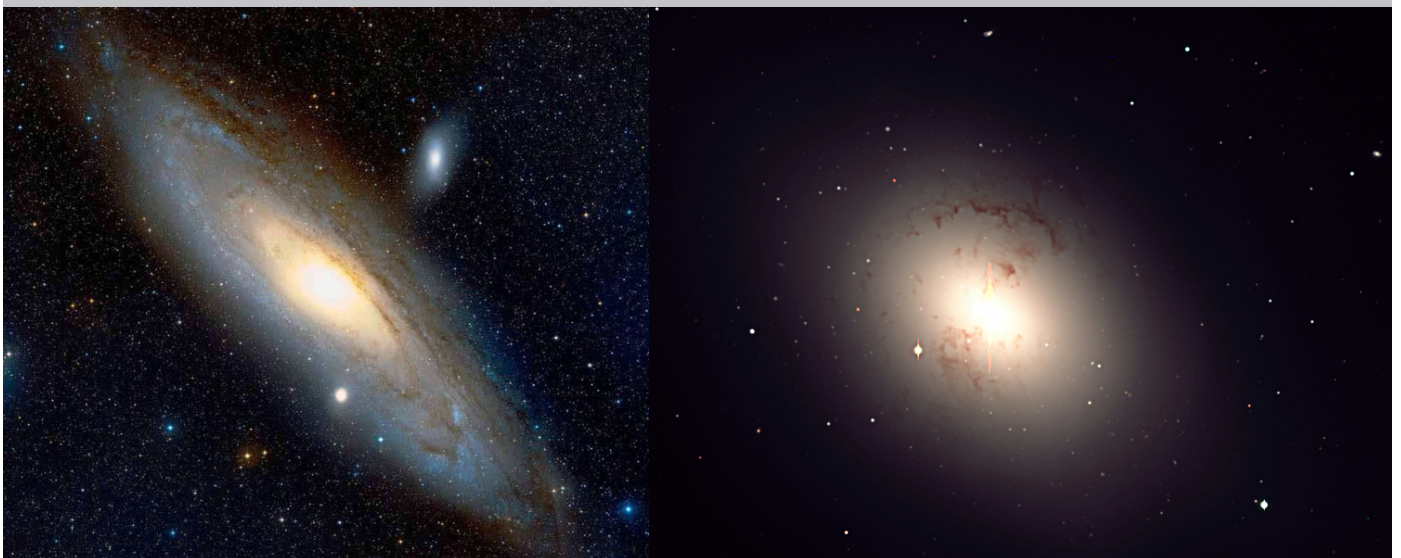
EWASS 2019

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Halve of all disk galaxies have bulges,  
and a few percent of all galaxies  
are huge bulges = elliptical galaxies

These galaxy spheroids form rapidly after Big Bang,  
vast quantities of gas collapsed rapidly.



<https://ned.ipac.caltech.edu/level5/Sept14/Kormendy/Kormendy7.html>

ESO

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Need to calculate the  
most massive forming  
star cluster ( $M_{\text{ecl,max}}$ )  
in a galaxy with a  
global star-formation rate  
( $SFR$ )

$$SFR = \frac{\text{mass of galaxy spheroid}}{\text{time to form galaxy}}$$

$$SFR = \frac{M_{\text{i,gal}}}{\Delta\tau} \approx \frac{M_{\text{p,gal}}}{\Delta\tau}$$

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**What about the correlation between  
the SMBH and host galaxy mass ?**

Easy : use IGIMF theory (Kroupa & Weidner 2003; Kroupa et al. 2013;  
Yan, Jerabkova et al. 2017; Jerabkova, Yan et al. 2018)

The total mass in stars formed in a galaxy over time  $\delta t$  is  $M_{\text{tot}} = SFR \times \delta t$

But 
$$M_{\text{tot}} = \int_{M_{\text{ecl,min}}}^{M_{\text{ecl,max}}} \xi_{\text{ecl}}(M_{\text{ecl}}) M_{\text{ecl}} dM_{\text{ecl}}$$

For  $M_{\text{ecl,min}} = 5 M_{\odot}$  and with 
$$1 = \int_{M_{\text{ecl,max}}}^{M_{\text{ecl,max}*}} \xi_{\text{ecl}}(M_{\text{ecl}}) dM_{\text{ecl}}$$

where  $M_{\text{ecl,max}*} = 10^{10} M_{\odot}$

Thus  $M_{\text{ecl,max}} = \text{fn}(SFR)$  as observed (Weidner et al. 2004; Randriamanakoto et al. 2013)

**What is  $\delta t$  ?**

The time-scale on which the interstellar medium spawns a complete population of new star (Egusa et al. 2004; 2009; Fukui et al. (2010); Meidt et al. 2015; Leisawitz 1989).



$$\delta t \approx 10 \text{ Myr}$$

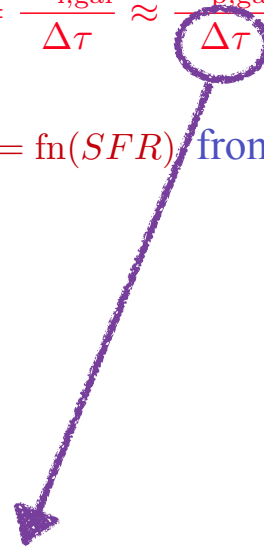
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The mass of this cluster,  $M_{\text{ecl,max}}$ , strongly correlates with later host galaxy mass,  $M_{\text{p,gal}}$ , through

$$SFR = \frac{M_{\text{i,gal}}}{\Delta\tau} \approx \frac{M_{\text{p,gal}}}{\Delta\tau}$$

via  $M_{\text{ecl,max}} = \text{fn}(SFR)$  from above

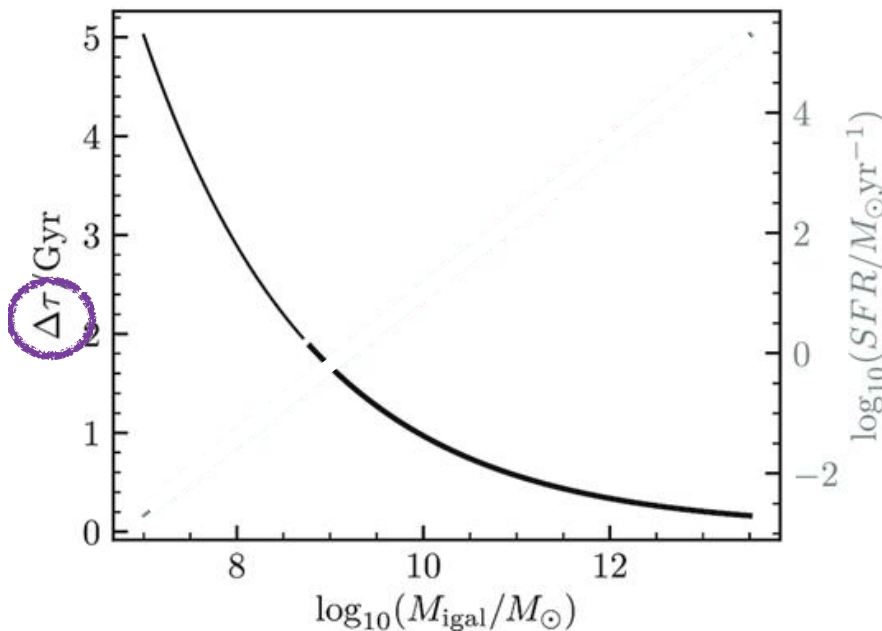


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The "downsizing" or "Thomas time"  $\Delta\tau$

ages,  $Z$ ,  $\left[\frac{\alpha}{\text{Fe}}\right]$  values for 124 early-type galaxies  
(Thomas et al. 2005; Recchi et al. 2009)



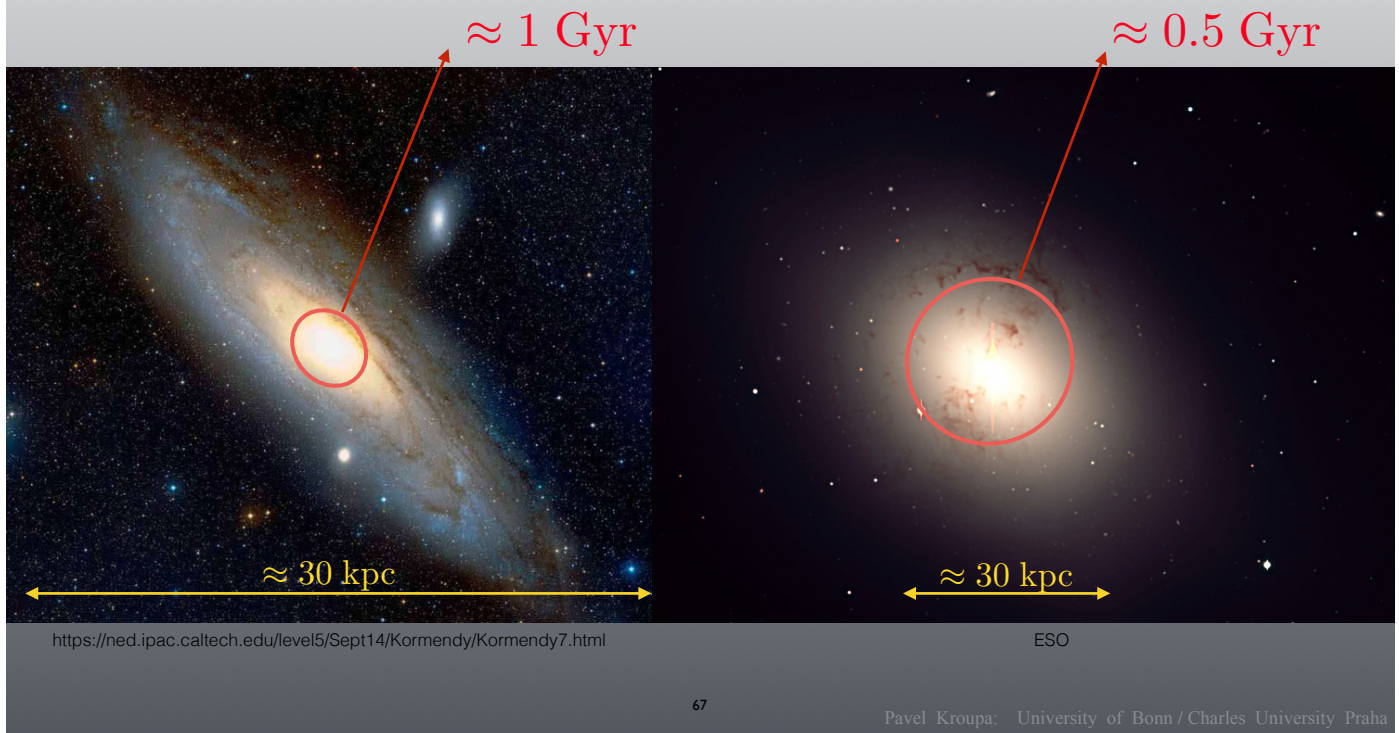
confirmed by  
de la Rosa et al. 2011;  
McDermid et al. 2015;  
Martin-Navarro et al. 2018;  
Salvador-Rusinol et al. 2020  
Yan, Jerabkova et al. 2021

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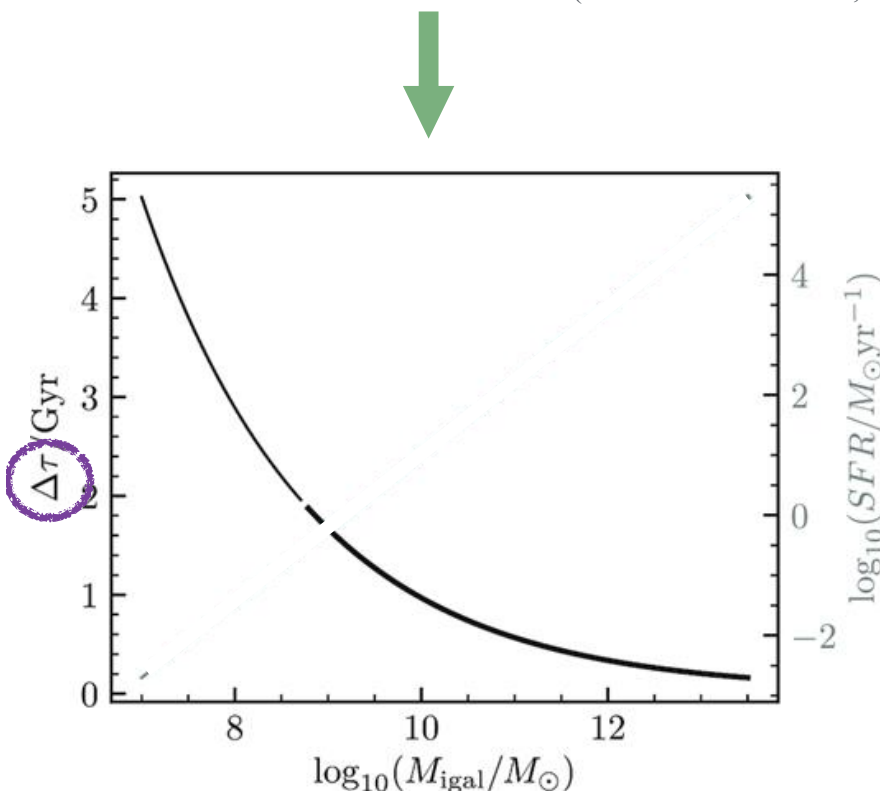
These galaxy spheroids form rapidly after Big Bang, vast quantities of gas collapsed rapidly.

These more massive, the faster it formed = "downsizing".



The "downsizing" or "Thomas time"  $\Delta\tau$

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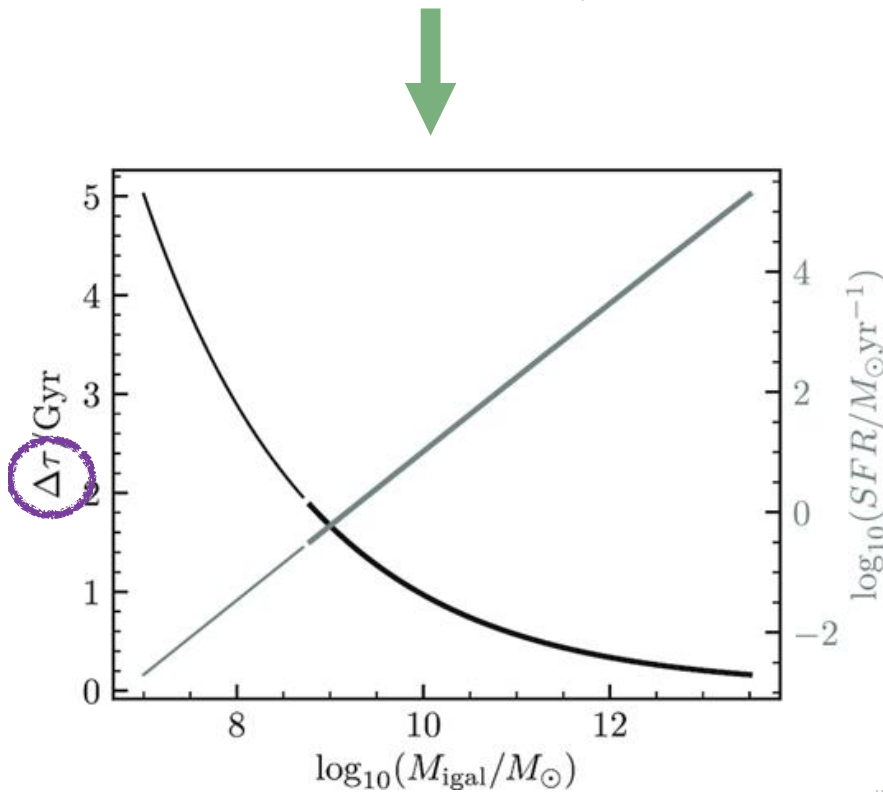


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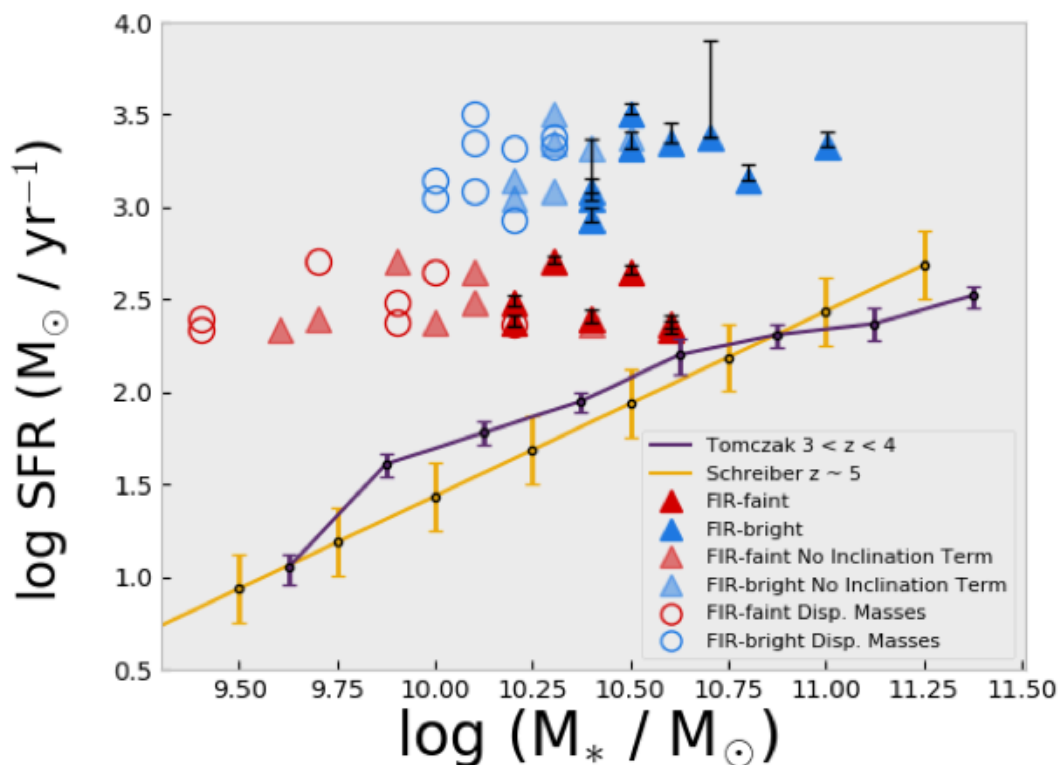
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Yan, Jerabkova et al. 2021

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## ALMA Observations of Quasar Host Galaxies at $z \approx 4.8$

Nguyen, Lira, Trakhtenbrot et al. 2020

$t \approx 1.2$  Gyr after Big Bang

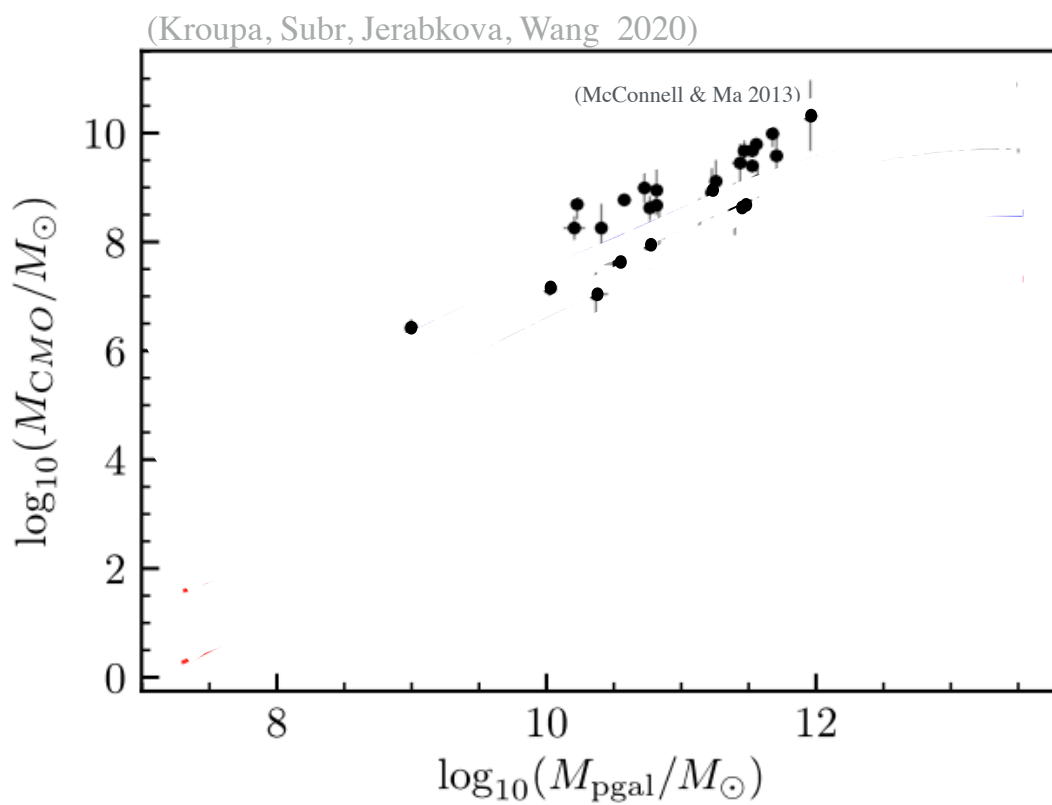


Thus we obtain

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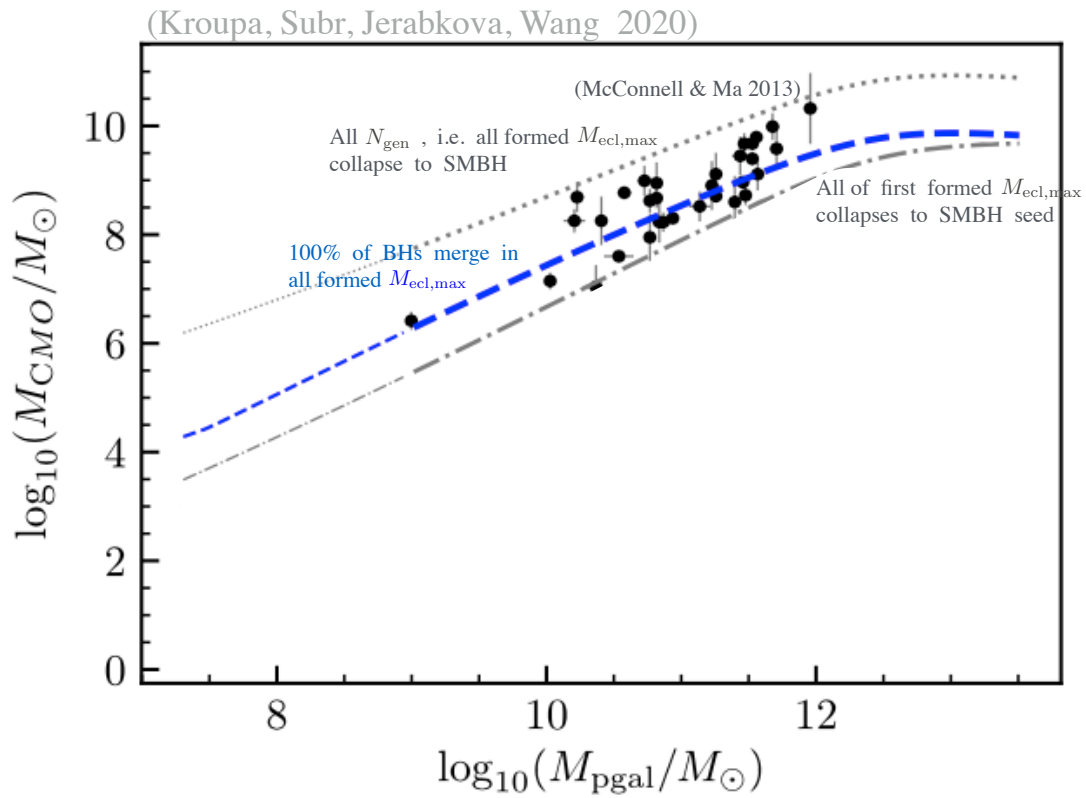
Thus we obtain



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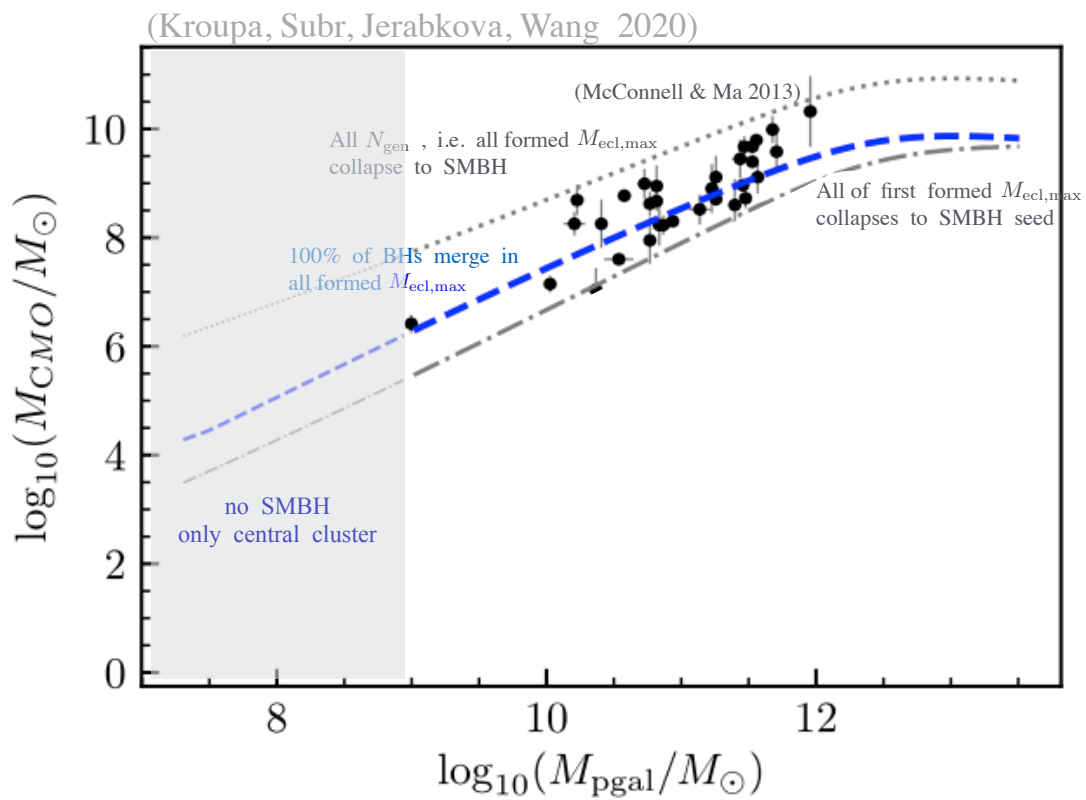
Thus we obtain



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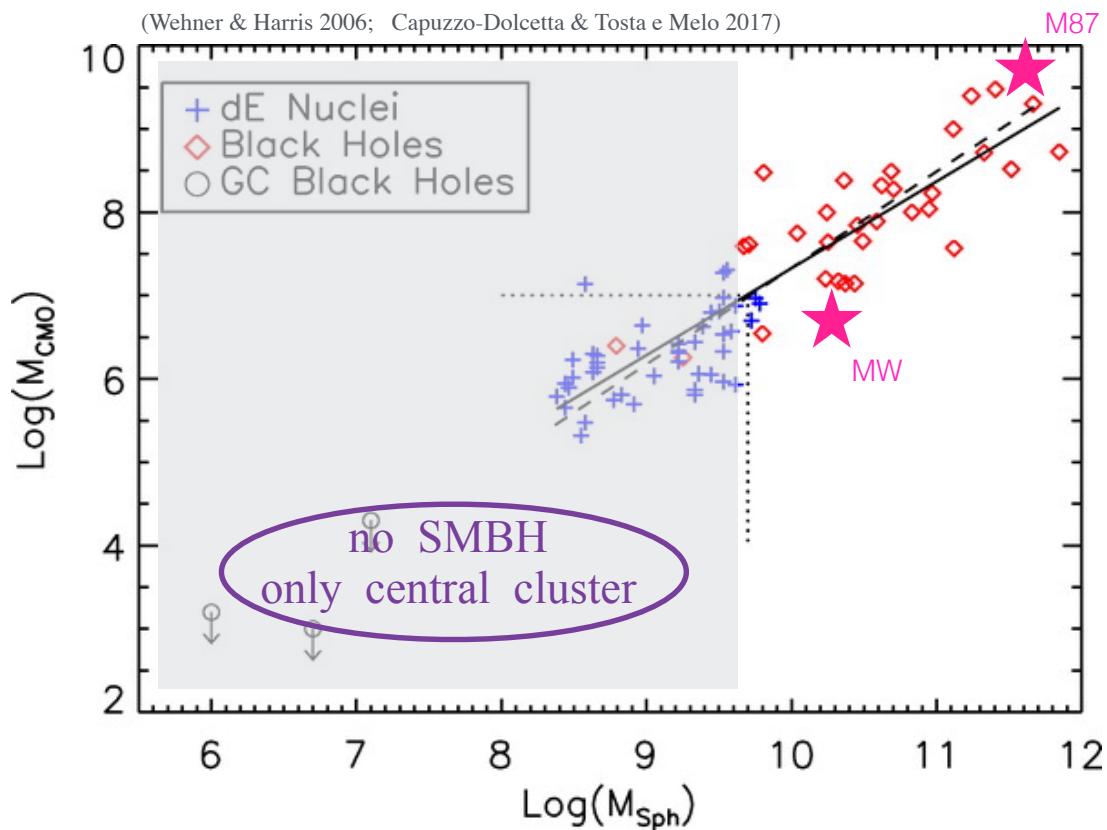
Thus we obtain



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## SMBH mass vs host galaxy mass (spheroid component)



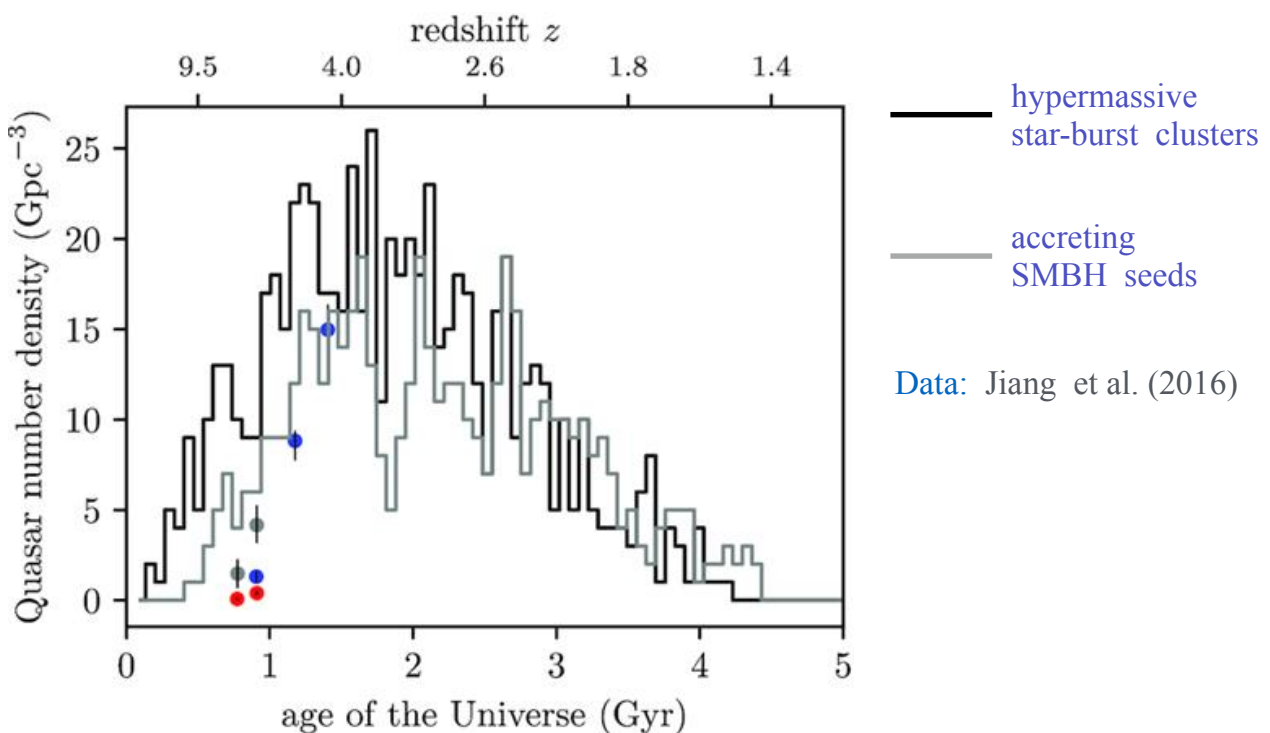
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## The appearance of the first quasars

(Kroupa, Subr, Jerabkova, Wang 2020)

Based on the *empirical* galaxy-formation times scales of Thomas et al. (2005)



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# The Conclusions



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## Solutions to the three problems:

### I) How can SMBHs even form ?

*Primarily through coalescence of  $> 10^4$  stellar BHs  
(driven by gas-infall onto the central BH cluster)*

### II) Why do SMBH masses correlate with the mass of the hosting galaxy ?

*Essentially through the downsizing (Thomas) time and  
via the IGIMF theory.*

### III) How can SMBHs form within a few 100 Myr after the Big Bang ?

*The highest- $z$  quasars are hypermassive star-burst clusters  
with top-heavy IMF (Jerabkova objects).*

### IV) $10^8$ quasars / SMBHs exist per co-moving Gpc<sup>3</sup>

### V) Thus rapid enrichment everywhere (even if patchy) ?

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## Essentially :

Given

- (i) the standard properties of normal matter
- (ii) the observed downsizing (Thomas) time
- (iii) the correlations of the stellar population with the downsizing (Thomas) time

quasars *must* appear about 200Myr after BigBang as *hypermassive star-burst clusters* (Jerabkova objects) and SMBHs *must* correlate with host galaxy.

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END