

How many explosions does one need? Quantifying supernovae in globular clusters from iron abundance spreads

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Introduction



Figure: NGC 3201, obtained with the WFI instrument on the ESO/MPG 2.2-m telescope at La Silla, Credit:ESO

Introduction

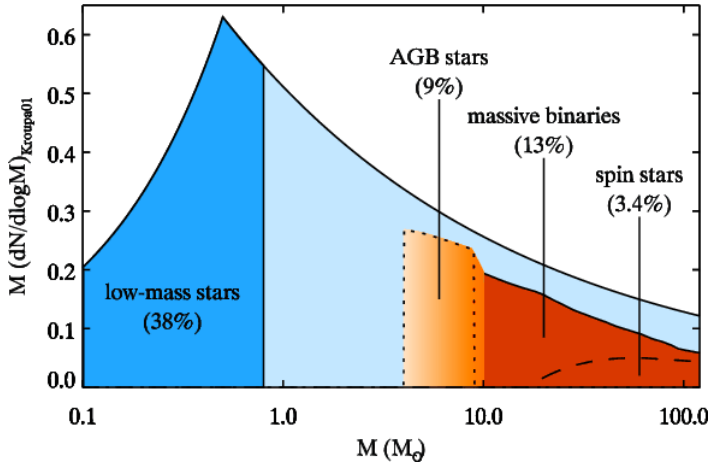


Figure: The IMF with different polluters and their mass fractions (Cottrell & Da Costa, 1981; Decressin et al., 2007; D’Ercole et al., 2008; de Mink et al., 2009; Wang et al., 2020).

Iron in globular clusters

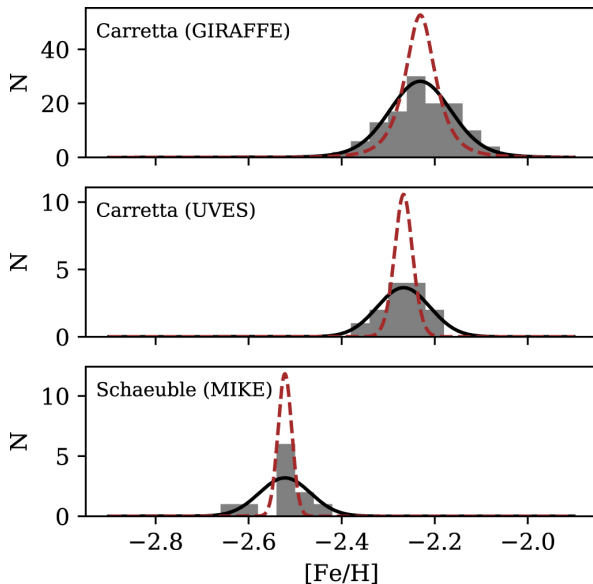


Figure: The iron abundances of stars in NGC 4590 from three different surveys (Bailin, 2019).

Iron in globular clusters

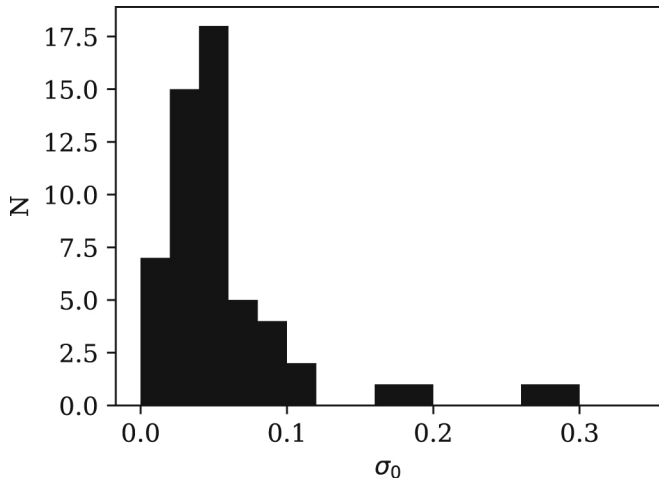


Figure: The iron abundance spread for 55 Milky Way GCs (Bailin, 2019).

The number of SNe

Wirth et al. (2021):

$$M_{\text{iron}} = p_{\text{iron},\odot} \left(10^{[Fe/H] + \sigma_{[Fe/H]}} - 10^{[Fe/H] - \sigma_{[Fe/H]}} \right) \times M_{\text{ini}} \left(\frac{1}{\epsilon} - 1 \right)$$

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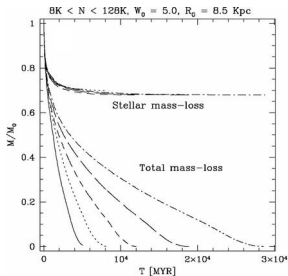
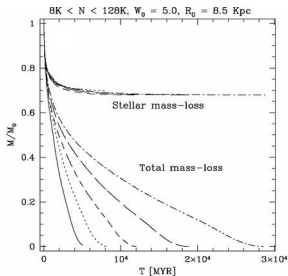


Figure: Mass loss of GCs based on N-Body simulations (Baumgardt & Makino, 2003).

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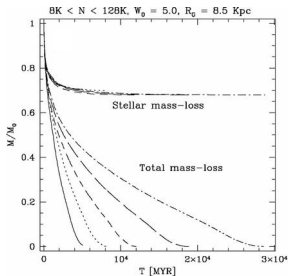
$$\rightarrow 0 = \beta \left[\frac{\frac{M_{\text{ini}}}{\langle m \rangle}}{\ln(\gamma \frac{M_{\text{ini}}}{\langle m \rangle})} \right]^x \frac{R_{\text{ap}}}{\text{kpc}} (1 - e) \frac{1 - \frac{M(t)}{PSE M_{\text{ini}}}}{\frac{t}{\text{Myr}}} - 1$$

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Maoz & Graur (2017):

$$m_{\text{SN}} = 0.074 M_{\odot}$$

Figure: Mass loss of GCs based on N-Body simulations (Baumgardt & Makino, 2003).

The number of SNe

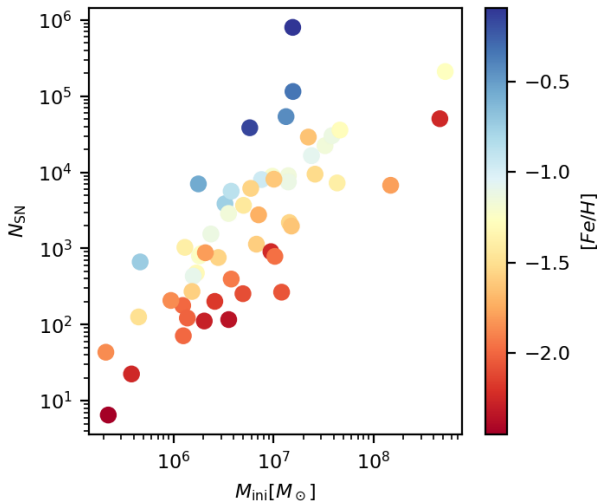


Figure: The number of SNe needed over the initial, color-coded for the mean iron abundance (Wirth 2022 in submission).

The time SF ends

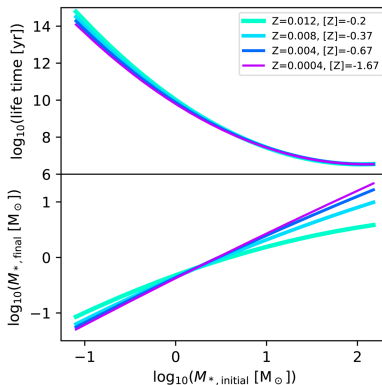


Figure: The life time and remnant mass of stars based on their initial mass (Yan et al., 2019).

The time SF ends

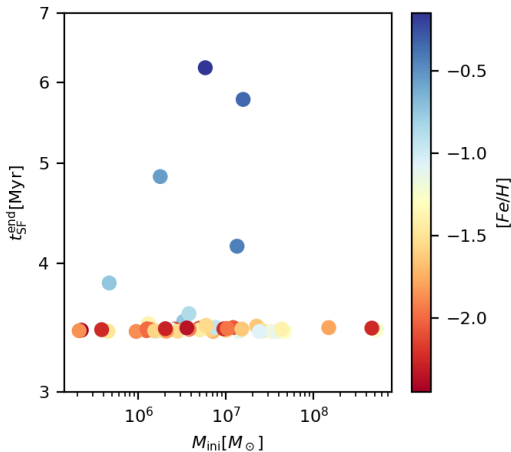


Figure: The time after which SF ends (Wirth et al. 2022 in submission). The empty dots are the solution using the canonical IMF the filled ones assume a top-heavy one.

Summary

- multiple populations of stars with different metallicities exist in GCs
- iron abundance spreads exist in some of them
- up to 10^5 SNe per GC (excluding Terzan 5)
- SF ends after $\sim 3.5 - 4$ Myr

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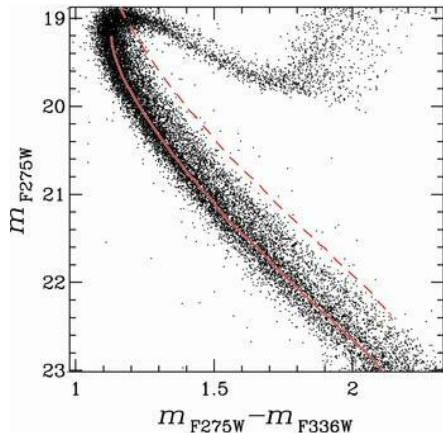


Figure: HR-diagram of the main sequence of 47 Tuc (Milone et al., 2012).

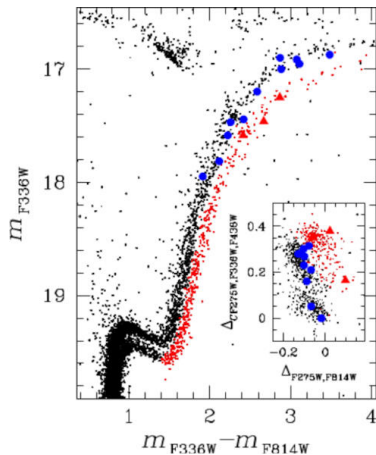


Figure: HR-diagram and Chromosome map of the red giant branch NGC 1851 (Marino et al., 2019).

Backup

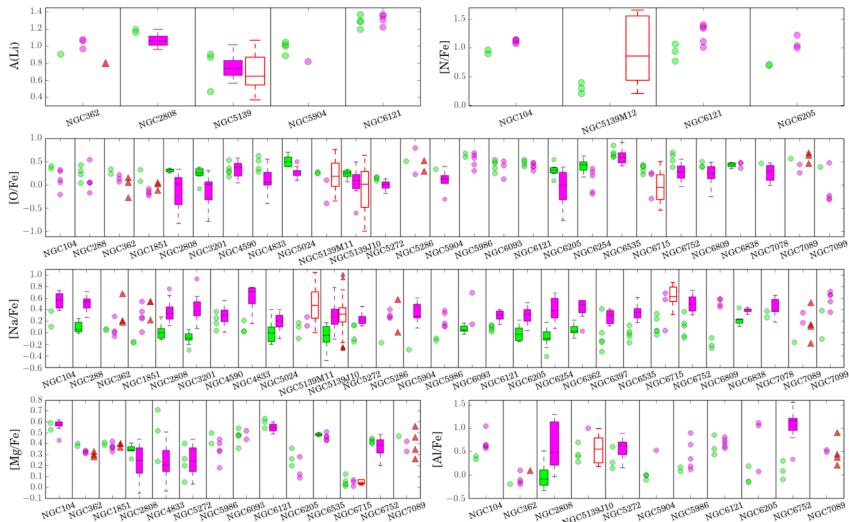


Figure: Different light element abundances for different GCs (Marino et al., 2019).

Backup

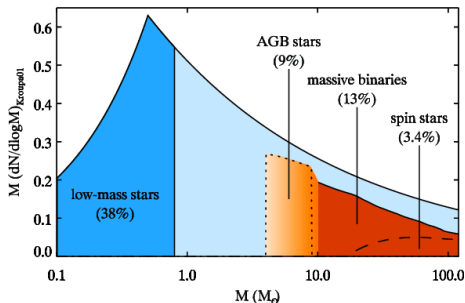


Figure: Different polluters and their mass fractions (Cottrell & Da Costa, 1981; Decressin et al., 2007; D’Ercole et al., 2008; de Mink et al., 2009; Wang et al., 2020).

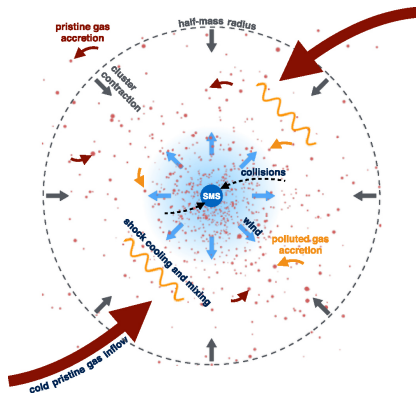


Figure: A supermassive star polluting the surrounding stars (Gieles et al., 2018)

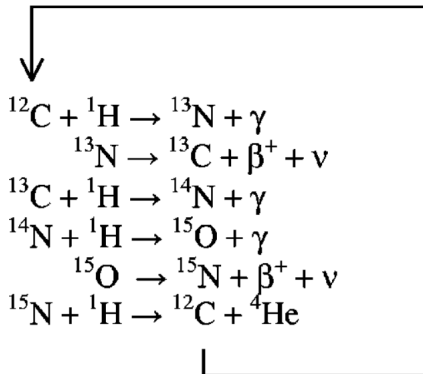


Figure: The CNO cycle (Nesaraja et al., 2001).

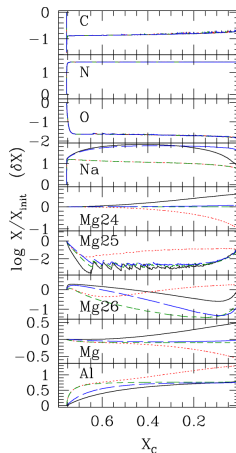


Figure: The evolution of central abundances in a $60 M_{\odot}$ rotating star (Decressin et al., 2007).

Baumgardt & Makino (2003); Wirth et al. (2021):

$$0 = \beta \left[\frac{\frac{M_{\text{ini}}}{\langle m \rangle}}{\ln(\gamma \frac{M_{\text{ini}}}{\langle m \rangle})} \right]^x \frac{R_{\text{ap}}}{\text{kpc}} (1 - e) \frac{1 - \frac{M(t)}{p_{\text{SE}} M_{\text{ini}}}}{\frac{t}{\text{Myr}}} - 1$$

$$p_{\text{SE}} = -0.61 + 0.52\alpha_3$$

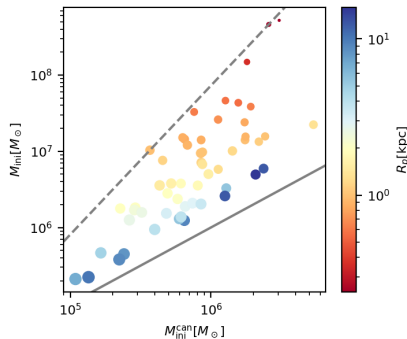


Figure: The initial masses computed using the canonical IMF compared to the ones assuming a top-heavy IMF (Wirth et al. 2022 in submission). The dashed grey line is

$$\frac{M_{\text{ini}}}{M_{\odot}} = 1.4 \times 10^{-4} \left(\frac{M_{\text{ini}}^{\text{can}}}{M_{\odot}} \right)^{2.0}.$$

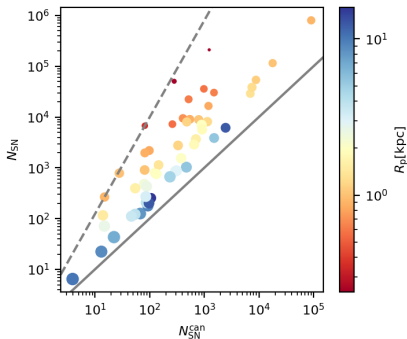


Figure: The initial masses computed using the canonical IMF compared to the ones assuming a top-heavy IMF (Wirth et al. 2022 in submission). The dashed grey line is $N_{\text{SN}} = 1.5 (N_{\text{SN}}^{\text{can}})^{1.9}$.

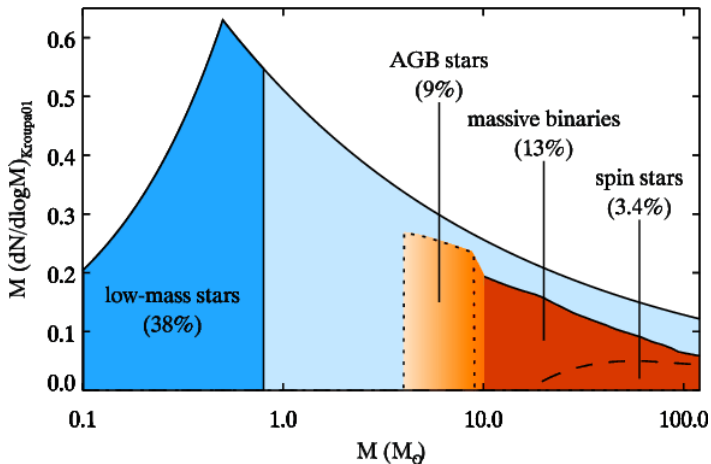


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Kroupa (2001)

$$dN = \xi(m) dm$$

$$\xi(m) = k_i m^{-\alpha_i}$$

$$\alpha_1 = 1.3,$$

$$\alpha_2 = 2.3,$$

$$0.08 \leq \frac{m}{M_{\odot}} \leq 0.5,$$

$$0.5 < \frac{m}{M_{\odot}}.$$

Yan et al. (2021)

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$$\alpha_1 = 1.3 + Z_{\odot} \Delta\alpha (10^{[Z/H]_{\text{ini}}} - 1), \quad 0.08 \leq \frac{m}{M_{\odot}} \leq 0.5,$$

$$\alpha_2 = 2.3 + Z_{\odot} \Delta\alpha (10^{[Z/H]_{\text{ini}}} - 1), \quad 0.5 \leq \frac{m}{M_{\odot}} \leq 1,$$

$$\alpha_3 = \begin{cases} 2.3, & y < -0.87, \\ -0.41y + 1.94, & y \geq -0.87, \end{cases} \quad 1 < \frac{m}{M_{\odot}},$$

$$y = -0.14[Z/H]_{\text{ini}} + 0.99 \log_{10} (\rho_{\text{gas}} / (10^6 M_{\odot} \text{pc}^{-3})).$$

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